

VO Rendering SS 2010

Unit 3: Surface Models



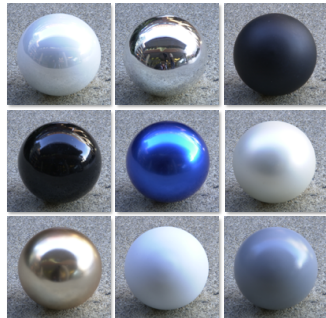
Sources:

What gives a material its appearance?



Surface Reflectance

- These spheres look different because they have different **surface reflectance properties**.



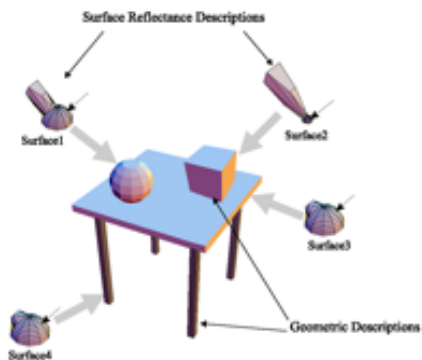
Surface - Light Interaction

- Key term of the equation for today:

$$\rho(x, x', x'')$$

- Encodes how light from a given direction is modified upon reflection from a surface
- Has to be answerable for all directions and surface points in a scene

Surfaces in a Scene



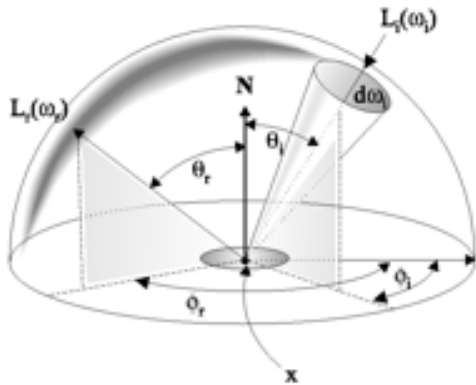
Definition

$$f_r(\omega_i \rightarrow \omega_r) \equiv \frac{L_r(\omega_r)}{L_i(\omega_i) \cos \theta_i d\omega_i}$$

- BRDF - Bi-directional Reflectance Distribution Function
- Hemispherical function
- 6 - dimensional (location, 4 angles, wavelength)
- Unit: sr⁻¹
- Determines fraction of incident energy scattered in each direction



BRDF Geometry



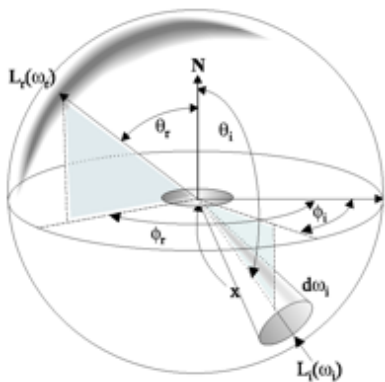
BTDF, BSDF



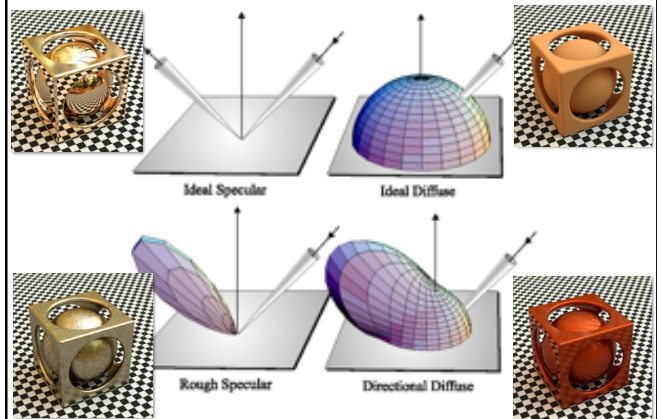
- Bi-directional Transmission Distribution Function
- Similar to BRDF, but for rays that point into the material
- Combination of BTDF & BRDF: BSDF
- Bi-directional Scattering Distribution Function
- Defined over entire sphere
- Rarely used



BSDF Geometry



BRDF Specimens



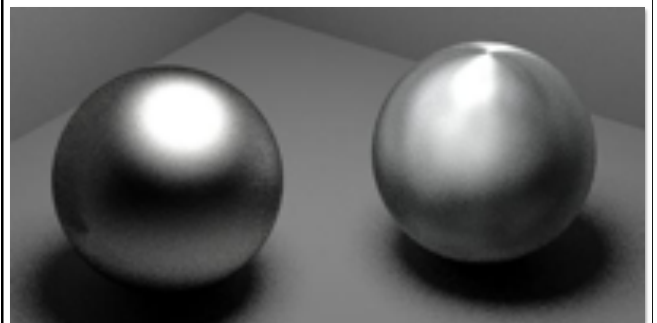
BRDF: Isotropy vs. Anisotropy



- Isotropy
 - ◆ Rotational invariance
 - ◆ Holds for a large number of surfaces
 - ◆ Reduces the number of variables by one
 - ◆ No alignment needed
$$f_r(\theta_i, \phi_i + \Delta\phi, \theta_r, \phi_r + \Delta\phi) = f_r(\theta_i, \phi_i, \theta_r, \phi_r)$$
- Anisotropy
 - ◆ Reflectance properties exhibit change with respect to rotation of the surface around the normal vector



Example Isotropic vs. Anisotropic



BRDF Requirements



- BRDF representations ought to:
 - ◆ use reasonable amounts of storage
 - ◆ faithfully capture the key features of the reflection characteristics
 - ◆ permit fast and easy sampling by Monte Carlo methods
 - Apart from perfectly diffuse surfaces and perfect mirrors, reflection properties are basically only tractable through MC rendering
 - Possibility of casting of rays according to distribution function is crucial



BRDF Data Sources



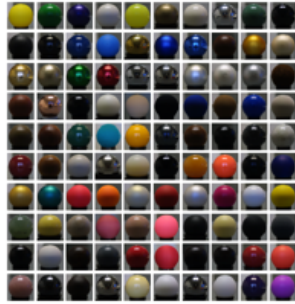
- Two fundamental approaches to the problem of representing BRDFs exist:
 - ◆ Explicit storage of tabulated measurements or simulation results
 - ◆ Approximation through analytical functions



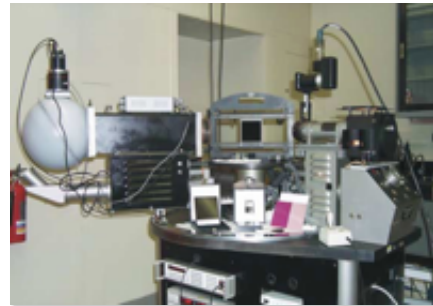
BRDF Datasets



- Very memory - intensive when naively stored as full set of finely spaced samples (16 x 90 x 360 x 90 x 360 ...)
- Compression essential
- Hard and time-consuming to measure accurately
- Bad stochastic sampling characteristics (rejection sampling)
- Necessary for verification purposes



Gonioreflectometer @ NIST



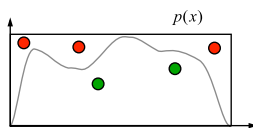
- Expensive, hard to maintain and operate
- Generates huge amounts of data



Sampling of Measured BRDFs



- Bad stochastic sampling characteristics
 - ◆ Analysing data in advance or
 - ◆ Rejection sampling
 - Propose a sample, accept it if it passes a certain test
 - Efficiency depends on the acceptance rate



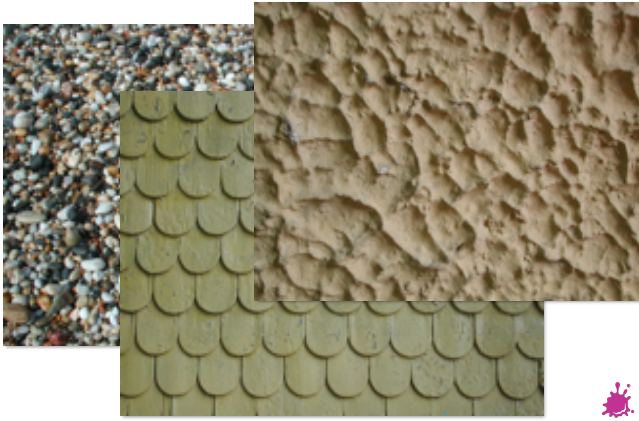
BTF



- Bi-directional Texture Function
- Similar to BRDF, only for entire textures (carpets, wood grain, cloth)
- Adds positional information to combine individual BRDF datasets
- Active research area with several problematic areas
 - ◆ Acquisition of samples
 - ◆ Generation of seamless textures from BTF data



BTF Examples



Requirements for Analytical BRDFs



- Reciprocity
 - ◆ Sampling directions can be interchanged
 - ◆ Due to Helmholtz reciprocity principle – a fundamental law of physics

$$f_r(\omega_i \rightarrow \omega_r) = f_r(\omega_r \rightarrow \omega_i)$$

- Energy conservation
- Fast evaluation
- Expressivity
- Easy stochastic sampling



Analytical BRDFs



- Empirical models
 - ◆ Lambert, Phong, Blinn, Lafortune
 - ◆ Superposition of different components
- Physically based models
 - ◆ Torrance-Sparrow, Cook-Torrance, Kajiya, He-Sillion-Torrance-Greenberg (HTSG)
 - ◆ Physical material constants needed



Empirical Models



- **Lambert**: only diffuse component
- **Phong**: generalized cosine lobe
- **Ward**: anisotropic
- Can be combined for higher realism
- Energy conservation dependent on coefficients and combination (esp. for Phong)
- Easy to sample
- Generalizations possible



Perfectly Diffuse



- Reflect the incoming light equally in all directions over the hemisphere
- Viewing direction independent
- E.g.
 - ◆ Lambert
 - ◆ Oren-Nayar
 - ◆ ...



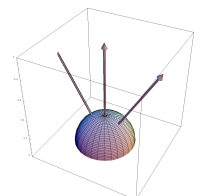
Lambert Surface



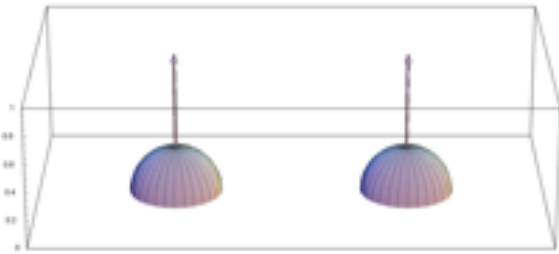
- Perfectly diffuse surface
- Light that leaves a surface is proportional to the cosine of the incident angle
- Colour defined by wavelength-dependent diffuse absorption coefficient k_d

$$f_r(\lambda) = \frac{1}{\pi} \cdot k_d(\lambda)$$

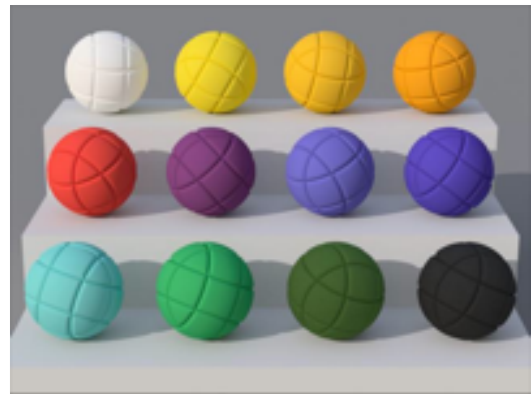
$$pdf(\theta_i, \lambda) = \frac{\cos \theta_i}{\pi}$$



Lambert BRDF Shape & Size



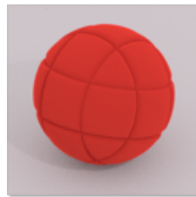
Lambert Surfaces



Oren-Nayar Surface



- Microfacet-based diffuse surface
- Identical to Lambert's cosine model for $\sigma = 0$
- More and more retro-reflective for increasing σ



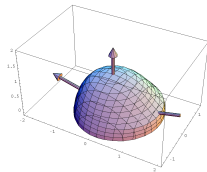
$$f_r(\omega_i, \omega_o) = \frac{\rho}{\pi} (A + B \max(0, \cos(\phi_i - \phi_o)) \sin \alpha \tan \beta)$$

$$A = 1 - \frac{\sigma^2}{2(\sigma^2 + 0.33)}$$

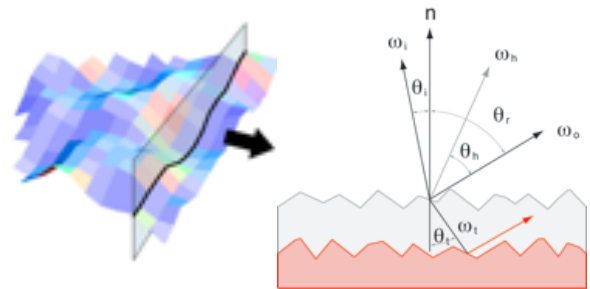
$$B = \frac{0.45\sigma^2}{\sigma^2 + 0.09}$$

$$\alpha = \max(\theta_i, \theta_o)$$

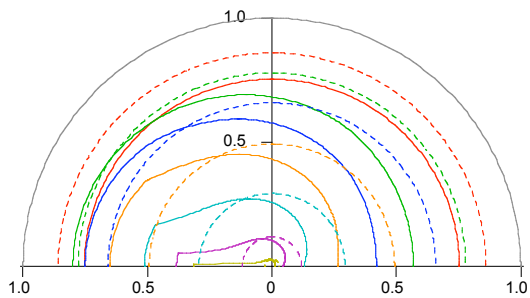
$$\beta = \min(\theta_i, \theta_o)$$



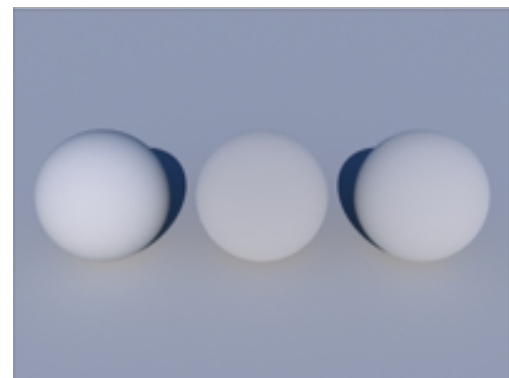
Microfacet Surfaces



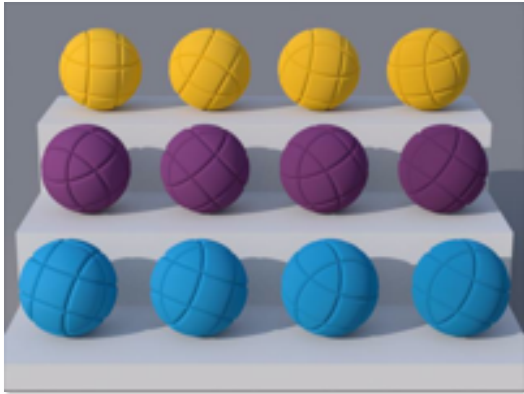
Medium vs. Rough Oren-Nayar



Oren-Nayar Example



Oren-Nayar Surface Example



Rough Specular



- Reflect light not only in the ideal direction
- „Highlight“
- Some of the light is reflected slightly off from the ideal specular angle.
- E.g. Phong: Size of the highlight can be changed with exponent



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32



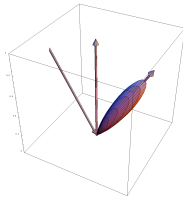
Phong Surface



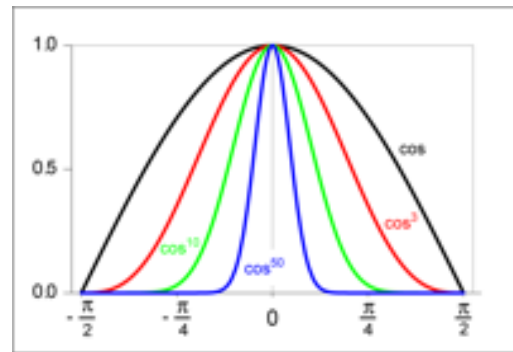
- Adds specular highlight

$$f_r(\omega_i, \omega_o) = \frac{\rho_d}{\pi} + \rho_s \frac{n+2}{2\pi} \cos(\omega_i \cdot R(\omega_o, \mathbf{n}))^n$$

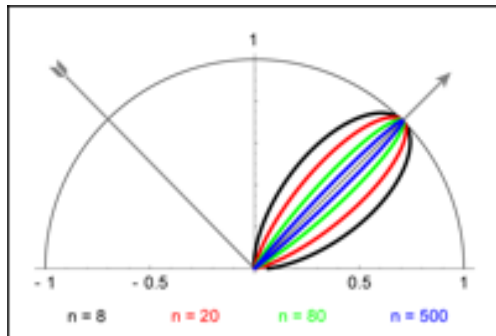
$$pdf(\omega_i, \omega_o) = \frac{n+1}{2\pi} \cos(\omega_i \cdot R(\omega_o, \mathbf{n}))^n$$



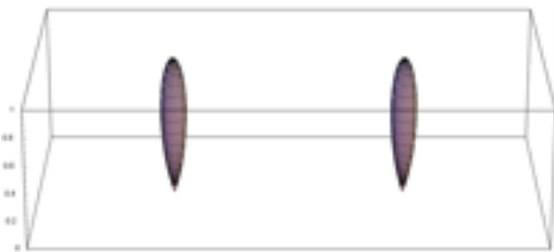
Cosine to the Nth



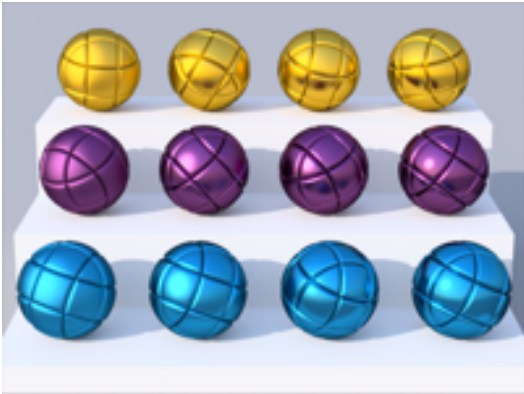
Cosine



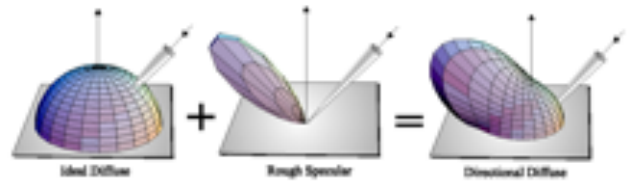
Plain Phong Lobe



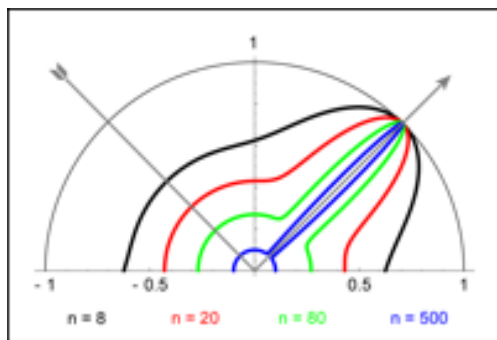
Plain Phong



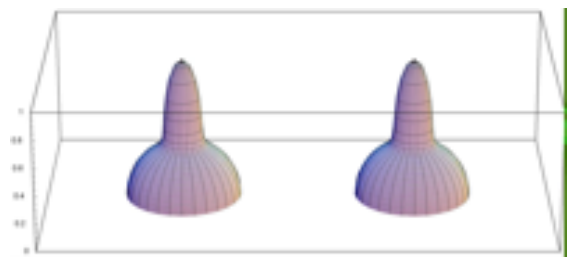
Superposition of BRDFs



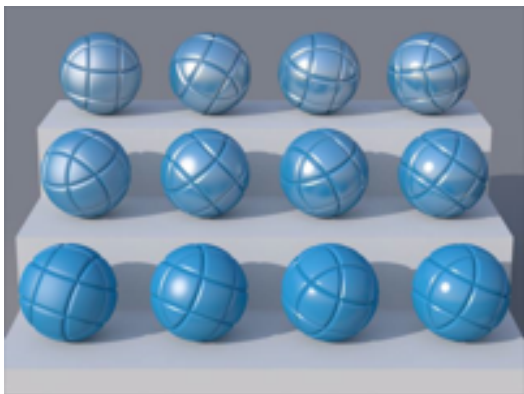
Cosine + Diffuse



Combined Phong Lobe



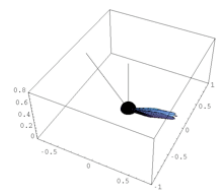
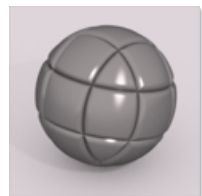
Phong Surface Example



Ward's BRDF Model



- Based on elliptical Gaussian distribution
- Physically based
- Energy conserving
- Based on real measurements with a gonioreflectometer
- Analytically invertible



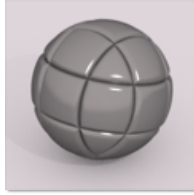
Ward BRDF Formulae



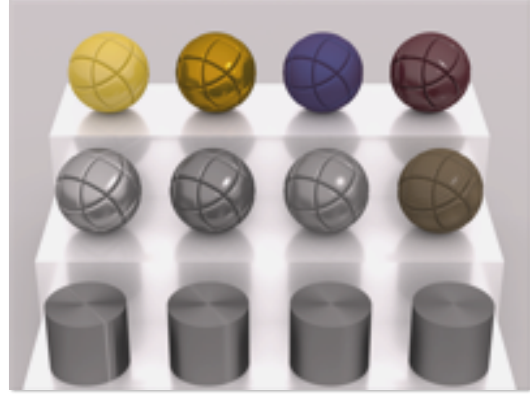
- Versions for isotropic and anisotropic surfaces

$$f_{iso}(\theta_i, \phi_i, \theta_o, \phi_o) = \frac{\rho_d}{\pi} + \rho_s \frac{\exp(-\tan^2 \frac{\delta}{\alpha^2})}{4\pi\alpha^2 \sqrt{\cos\theta_i \cos\theta_o}}$$

$$f_{an}(\theta_i, \phi_i, \theta_o, \phi_o) = \frac{\rho_d}{\pi} + \rho_s \frac{\exp(-\tan^2 \delta(\frac{\cos^2 \phi_i}{\alpha_1^2} + \frac{\sin^2 \phi_i}{\alpha_2^2}))}{4\pi\alpha_x \alpha_y \sqrt{\cos\theta_i \cos\theta_o}}$$



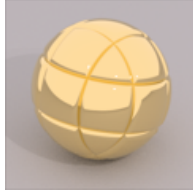
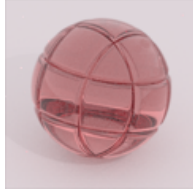
Wards BRDF: Example



Perfectly Specular



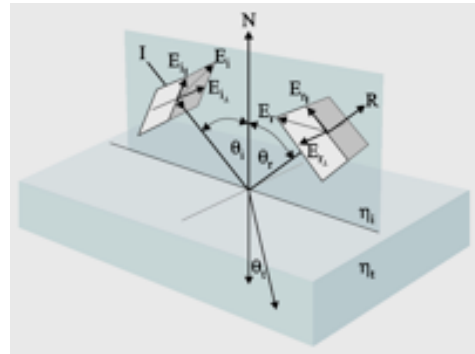
- Do not exist in reality
- Only one outgoing direction
- Incoming angle equals outgoing angle
- Used to simulate smooth glass / metallic surfaces
- For realistic materials: Fresnel coefficients



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46

Fresnel Geometry



Fresnel Surface (Conductors)



- Interface between two materials with complex index of refraction
- Polarization information usually not used in renderer
- (n, κ) : complex-valued index of

$$r_{\perp} = \frac{a^2 + b^2 - 2a \cos \theta_i + \cos^2 \theta_i}{a^2 + b^2 + 2a \cos \theta_i + \cos^2 \theta_i}$$

$$r_{\parallel} = \frac{a^2 + b^2 - 2a \sin \theta_i \tan \theta_i + \sin^2 \theta_i \tan^2 \theta_i}{a^2 + b^2 + 2a \sin \theta_i \tan \theta_i + \sin^2 \theta_i \tan^2 \theta_i}$$

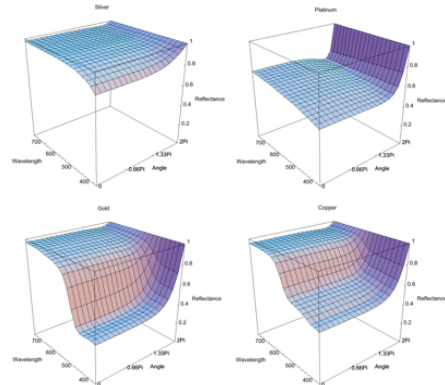
$$2a^2 = \sqrt{(\eta^2 - \kappa^2 - \sin^2 \theta_i)^2 + 4\eta^2 \kappa^2} + (\eta^2 - \kappa^2 - \sin^2 \theta_i)$$

$$2b^2 = \sqrt{(\eta^2 - \kappa^2 - \sin^2 \theta_i)^2 + 4\eta^2 \kappa^2} - (\eta^2 - \kappa^2 - \sin^2 \theta_i)$$

$$f_r(p, \omega_i, \omega_o) = F_r(\omega_o) \frac{\delta(\omega_i - R(\omega_o, \mathbf{n}))}{|\cos \theta_i|}$$



Conductors: Spectral Reflectivity



Reflection from Conductors



Fresnel Surface (Dielectrics)



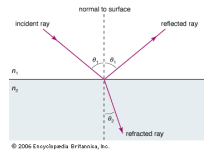
- Interface between two materials with real index of refraction
- No absorption k

$$r_{\parallel} = \frac{\eta_t \cos \theta_i + \eta_i \cos \theta_t}{\eta_t \cos \theta_i - \eta_i \cos \theta_t}$$

$$r_{\perp} = \frac{\eta_t \cos \theta_i + \eta_i \cos \theta_t}{\eta_t \cos \theta_i - \eta_i \cos \theta_t}$$

$$R = \frac{1}{2} \left(\frac{\sin(\theta_i - \theta_t)}{\sin(\theta_i + \theta_t)} \right)^2 \left[1 + \left(\frac{\cos(\theta_i + \theta_t)}{\cos \theta_i - \theta_t} \right)^2 \right]$$

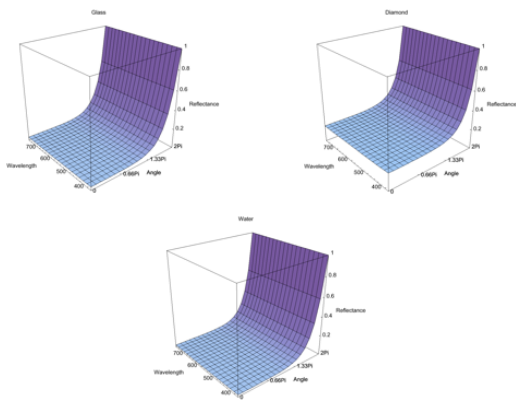
$$f_t(p, \omega_i, \omega_t) = \frac{\eta_o^2}{\eta_i^2} (1 - F_r(\omega_o)) \frac{\delta(\omega_i - T(\omega_i, \mathbf{n}))}{|\cos \theta_i|}$$



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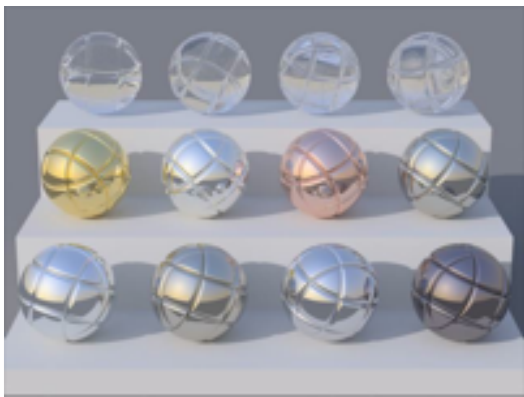
Dielectrics: Spectral Reflectivity



Transparent Dielectrics



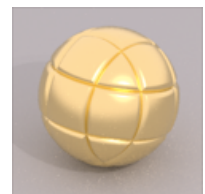
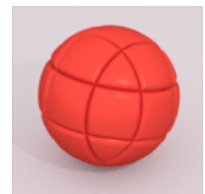
Fresnel Surface Example



Directional Diffuse



- Combination of a rough specular reflector and an ideal diffuse reflector
- Eg.
 - ◆ Cook-Torrance
 - ◆ Ward
 - ◆ He
 - ◆ ...



Torrance-Sparrow Surface (1)



- Physically plausible BRDF model three main components:
 - Microfacet model
 - Fresnel term for reflectance
 - Roughness term
- Requires material constants to be known

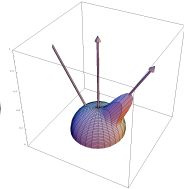


$$f_r(p, \omega_i, \omega_o) = \frac{D(\omega_h)G(\omega_i, \omega_o)F(\omega_o)}{4 \cos \theta_i \cos \theta_o}$$

$$D(\omega_h) = \frac{e+2}{2\pi} (\omega_h \cdot \mathbf{n})^e$$

$$G(\omega_i, \omega_o) = \min \left(1, \min \left(\frac{2(\omega_h \cdot \mathbf{n})(\omega_o \cdot \mathbf{n})}{\omega_h \cdot \omega_o}, \frac{2(\omega_h \cdot \mathbf{n})(\omega_i \cdot \mathbf{n})}{\omega_h \cdot \omega_o} \right) \right)$$

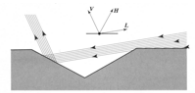
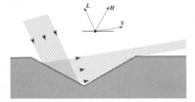
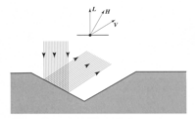
$$pdf(\omega_h, \omega_i, \omega_o) = \frac{(n+2) \cos^n \theta_h}{4(\omega_h \cdot \omega_o)}$$



Geometric Factor



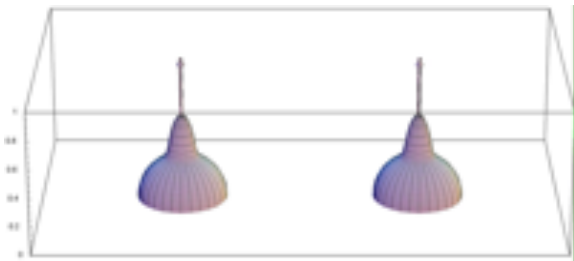
- Randomly oriented facets are perfect reflectors except for geometrical attenuation due to
 - self-shadowing
 - masking



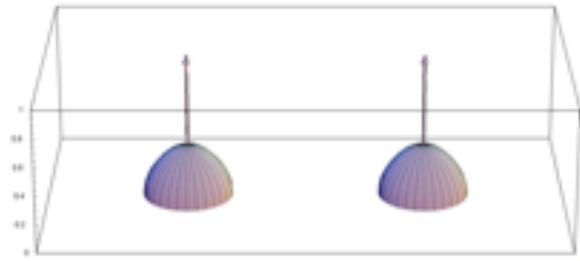
$$G = \min \left(1, \frac{2(\mathbf{N} \cdot \mathbf{H})(\mathbf{N} \cdot \mathbf{V})}{\mathbf{V} \cdot \mathbf{H}}, \frac{2(\mathbf{N} \cdot \mathbf{H})(\mathbf{N} \cdot \mathbf{L})}{\mathbf{V} \cdot \mathbf{H}} \right)$$



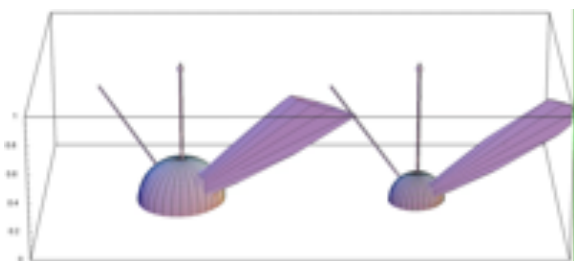
Specular Torrance-Sparrow



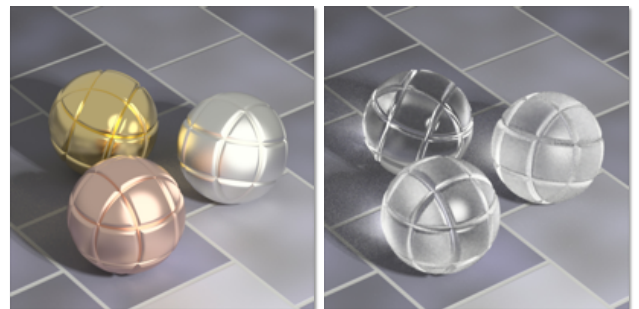
Rough Torrance-Sparrow



Constant Angle, Varying Roughness



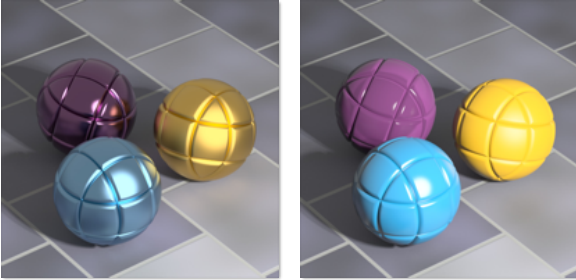
Rough Metallic/Glass Surface



Reflection Colour



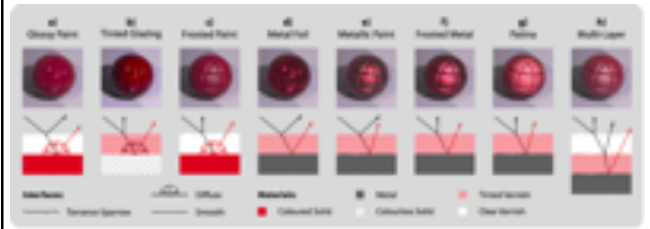
- Conductors: coloured highlight



- Dielectrics: white highlight



Torrance-Sparrow Surface Types



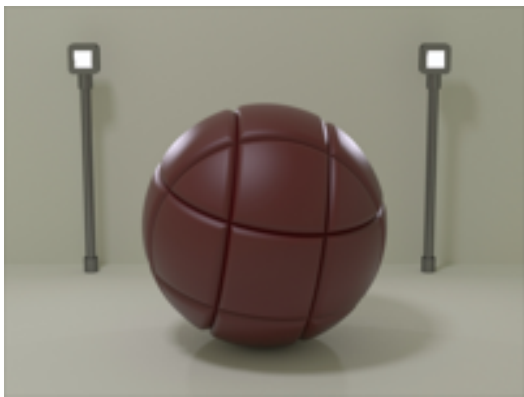
Torrance-Sparrow: Glossy Paint



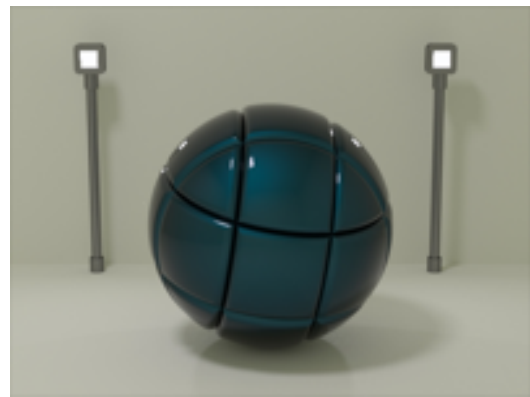
Torrance-Sparrow: Tinted Glass



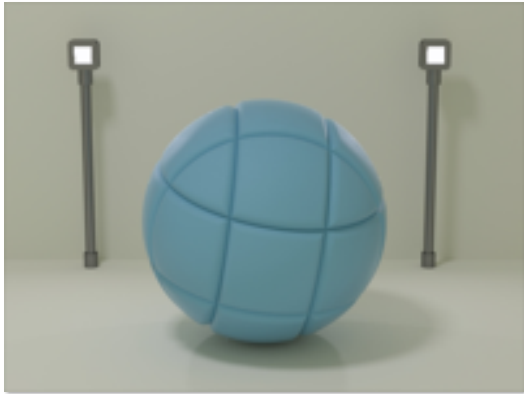
Torrance-Sparrow: Frosted Paint



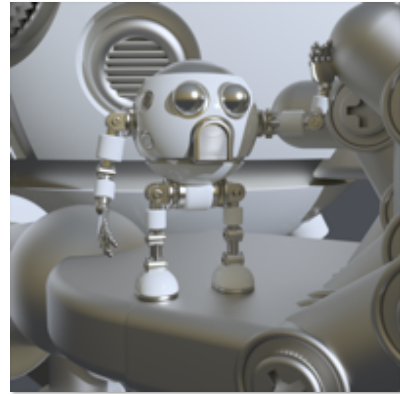
Torrance-Sparrow: Metallic Paint



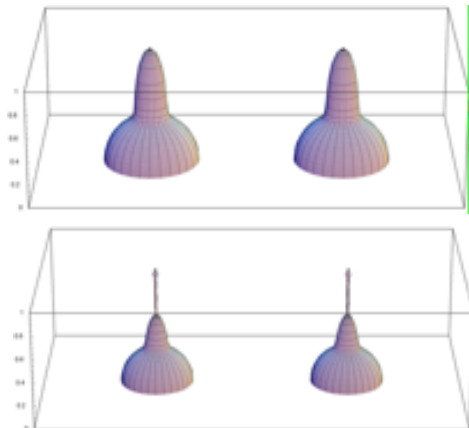
Torrance-Sparrow: Multi-Layer



Torrance-Sparrow Scene



Phong vs. Torrance-Sparrow



Torrance-Sparrow vs. Phong



Torrance-Sparrow



Phong



Torrance-Sparrow: Evaluation



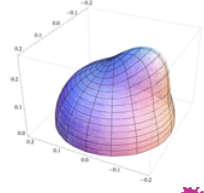
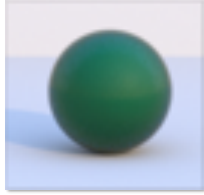
- Plus:
 - ◆ physically correct
 - ◆ excellent results
- Minus:
 - ◆ hard to sample
 - ◆ hard to code
 - ◆ depends on material constants



He, Torrance, Sillion, Greenberg



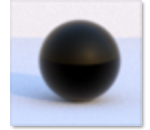
- Based on wave optics and diffraction theory, can take polarization into account
- Additional split between diffuse and directional diffuse term
- Expensive to compute
- Input: auto-correlation τ , variance of surface height σ , IOR



He Implementation



- Specular component
 - ◆ Dirac impulse
- Directional diffuse component
 - ◆ Solve z_0 with Newton-Raphson
 - ◆ Infinity sum should have at least 250 terms \rightarrow precomputation possible
 - ◆ Sampling: ???
- Uniform diffuse component
 - ◆ Cosine sampling



Beyond Normal BRDFs



- Some surfaces that cannot be characterized through standard BRDFs:
 - Phosphorescent paint
 - Fluorescent paint
 - Metallic paint
 - Pearlescent paint
 - BSSRDFs



Rendering VO Unit 3



The End
Thank you for your attention!

