



Rendering: Spatial Acceleration Structures

Bernhard Kerbl

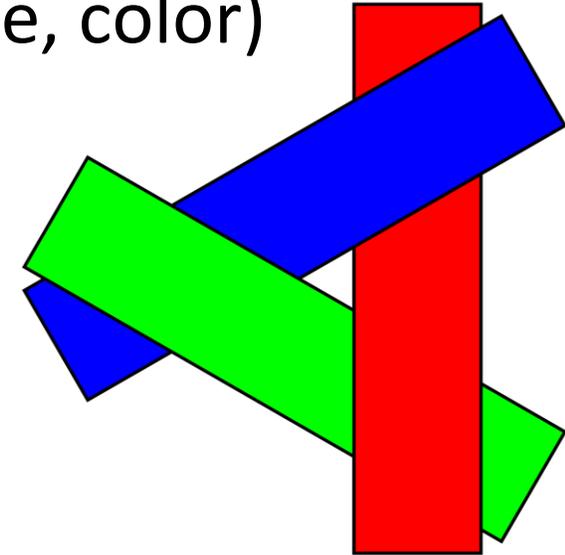
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Institute of Visual Computing & Human-Centered Technology
TU Wien, Austria

With slides based on material by Jaakko Lehtinen, used with permission



- A good image needs realistic *intensity* and *visibility*
 - **Intensity** creates stimulus of optic nerve (black, white, color)
 - **Visibility** makes sure that objects adhere to depth

How would you process the scene on the right to make sure the rendered output image is correct?



Source: Wojciech Mula, Wikipedia "Painter's algorithm"

- (Naïve) Ray-Casting Render Loop
 - Shoot a ray through **each** pixel into the scene
 - Iterate over **all** objects and test for intersection
 - Record the **closest** intersection (*visibility*)
 - Compute color and write to pixel (*intensity*)



```
void render(Camera cam)
{
    for(Pixel& pix : pixels)
    {
        pix.Color = background;

        Intersection closest;
        closest.Distance = INFINITY;

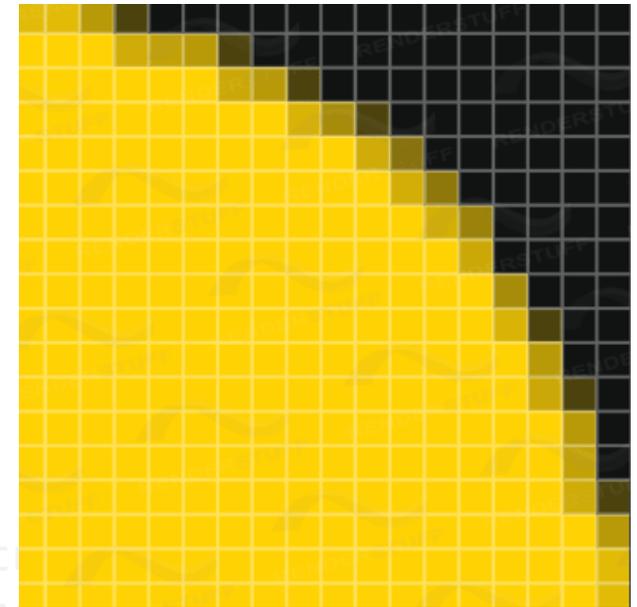
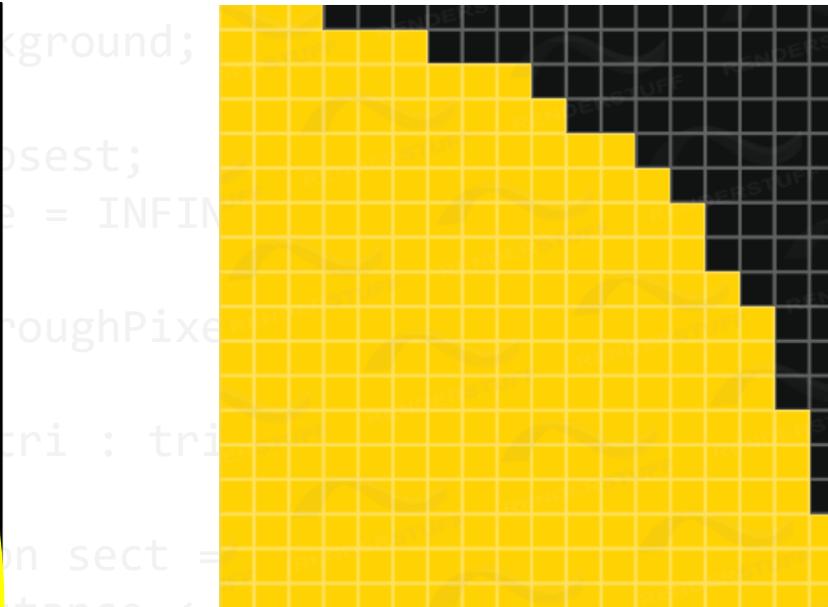
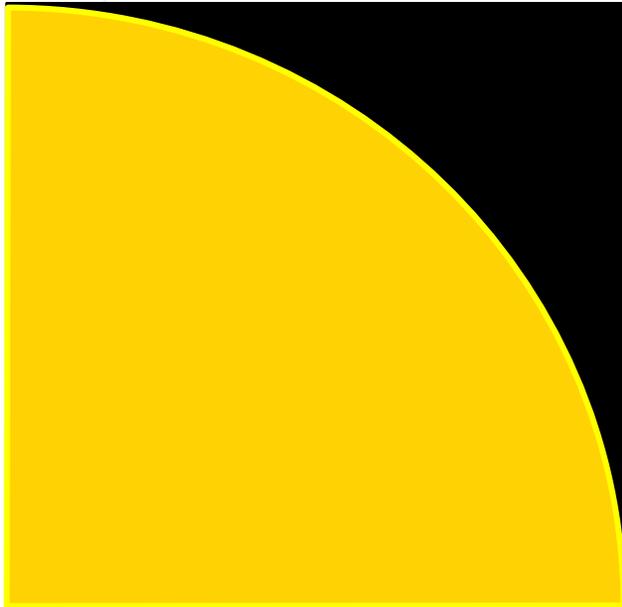
        Ray ray = rayThroughPixel(cam, pix);

        for (Triangle& tri : triangles)
        {
            Intersection sect = findClosestIntersection(ray, tri);
            if(sect.Distance < closest.Distance) { closest = sect; }
        }

        if(closest.Distance != INFINITY) { pix.Color = computeColor(closest); }
    }
}
```



```
void render(Camera cam)
{
    for(Pixel& pix : pixels)
    {
```



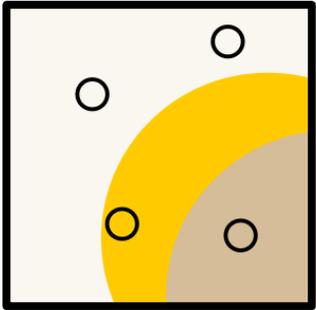
Source: renderstuff.com/



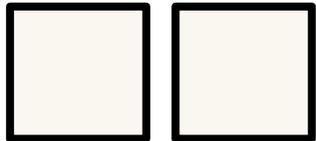
Those are your dad's pixels!



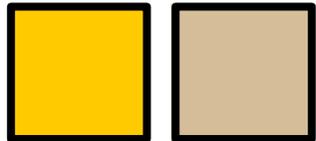
- Instead of a single ray through each pixel, use multiple „samples“



Pixel with sampling positions



Sampled colours



Average = displayed colour

Source: Parcly Taxel, Wikipedia "Supersampling"



```
void render(Camera cam)
{
```

```
    for(Pixel& pix : pixels)
```

```
    {
        background;
```

```
        closest;
```

```
        e = INFIN
```

```
        roughPixe
```

```
        tri : tri
```

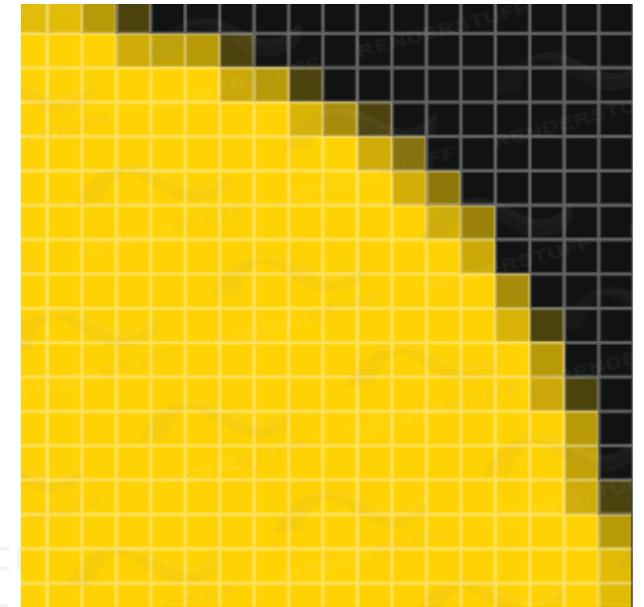
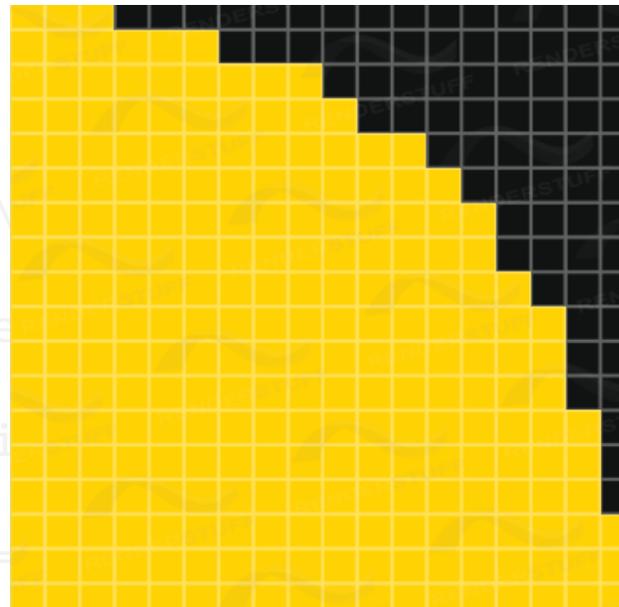
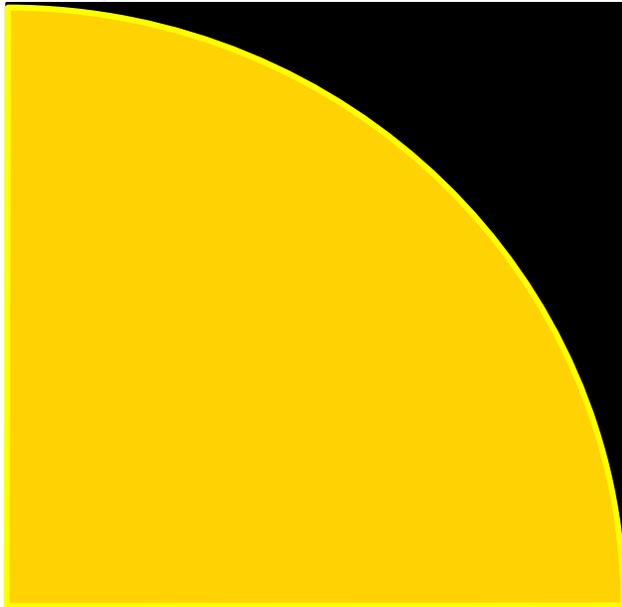
```
        on sect =
```

```
        if(sect.Distance < closest.Distance) { closest = sect; }
```

```
        if(closest.Distance != INFINITY) { pix.Color = computeColor(closest); }
```

```
    }
```

```
}
```



Source: renderstuff.com/



Antialiased



```
pix.Color = background;

Intersection closest;
closest.Distance = INFINITY;

for(int s = 0; s < NUM_SAMPLES; s++)
{
    SampleInfo sInfo = drawSample();
    Ray ray = rayThroughSample(cam, sInfo.Location);
    for (Triangle& tri : triangles)
    {
        Intersection sect = findClosestIntersection(ray, tri);
        if(sect.Distance < closest.Distance) { closest = sect; }
    }

    if(closest.Distance != INFINITY)
    {
        RGBColor sample = computeColor(closest);
        pix.Color += filter(sInfo.Filter, RGBWColor(sample, 1));
    }
}
pix.Color /= pixColor.w;
```



Updated Render Loop

```
pix.Color = background;
```

```
Intersection closest;  
closest.Distance = INFINITY;
```

```
for(int s = 0; s < NUM_SAMPLES; s++)  
{
```

```
    SampleInfo sInfo = drawSample();  
    Ray ray = rayThroughSample(cam, sInfo.Location);  
    for (Triangle& tri : triangles)
```

```
    {  
        Intersection sect = findClosestIntersection(ray, tri);  
        if(sect.Distance < closest.Distance) { closest = sect; }  
    }
```

```
if(closest.Distance != INFINITY)
```

```
{  
    RGBColor sample = computeColor(closest);  
    pix.Color += filter(sInfo.Filter, RGBWColor(sample, 1));  
}
```

```
}  
pix.Color /= pixColor.w;
```

Sampling

Color and Light

Rendering Equation

Filtering

Sample Integration



- Let's look at the basic runtime (single sample per pixel)

```
void render(Camera cam)
{
    for(Pixel& pix : pixels)
    {
        ...

        for (Triangle& tri : triangles)
        {
            ...
        }

        ...
    }
}
```



- Let's look at the basic runtime (single sample per pixel)

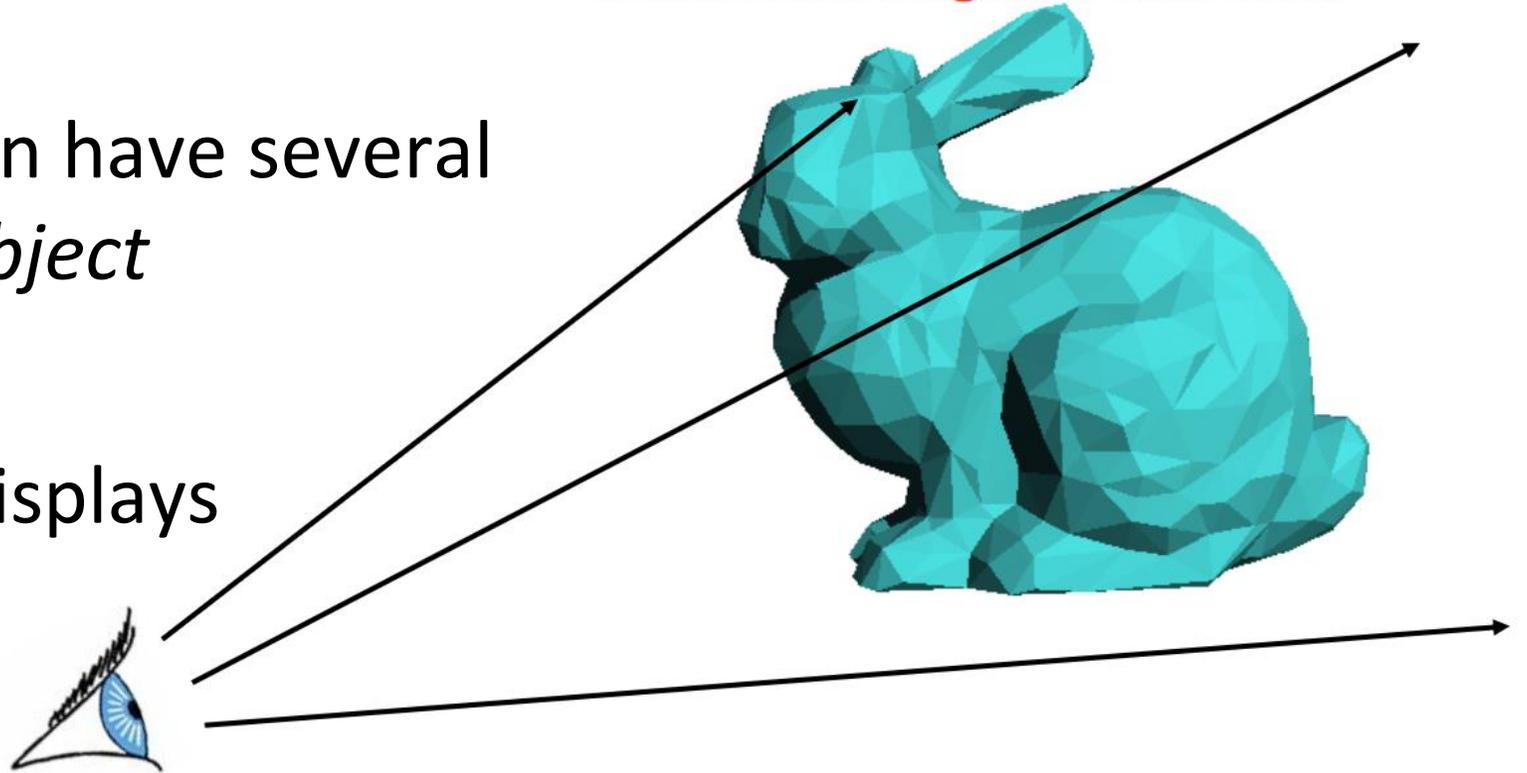
```
void render(Camera cam)
{
    for(Pixel& pix : pixels) ←  $N$ 
    {
        ...
        for (Triangle& tri : triangles) ←  $M$ 
        {
            ...
        }
        ...
    }
}
```

- This is $\mathcal{O}(N \cdot M)$, but even worse, it's $\Omega(N \cdot M)$!



- Run time complexity quickly becomes a limiting factor
- High-quality scenes can have several million triangles *per object*
- Current screens and displays are moving towards 4k resolution

What if this thing had 1B triangles and your ray tracer just walked through all of them?

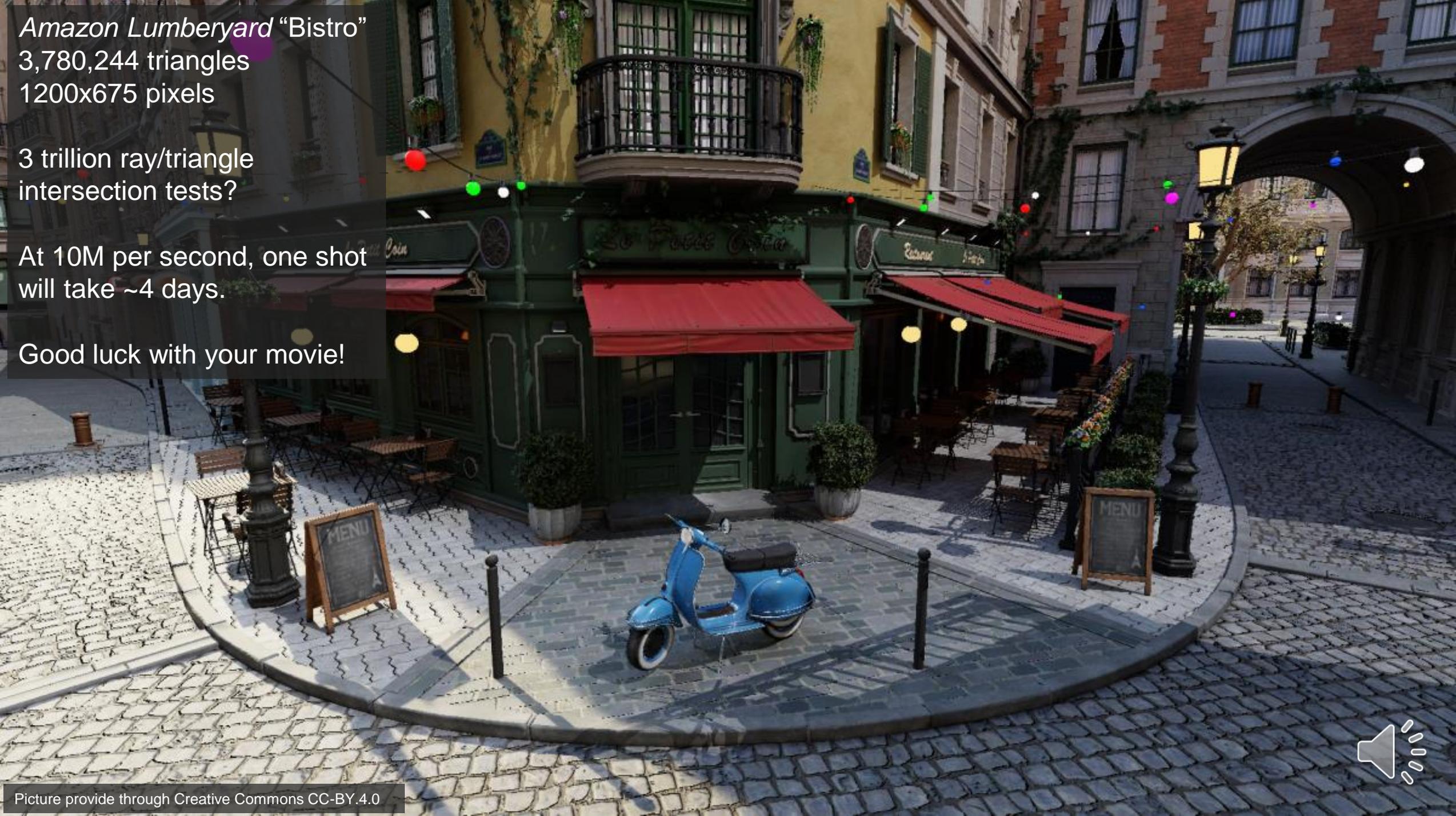


Amazon Lumberyard "Bistro"
3,780,244 triangles
1200x675 pixels

3 trillion ray/triangle
intersection tests?

At 10M per second, one shot
will take ~4 days.

Good luck with your movie!



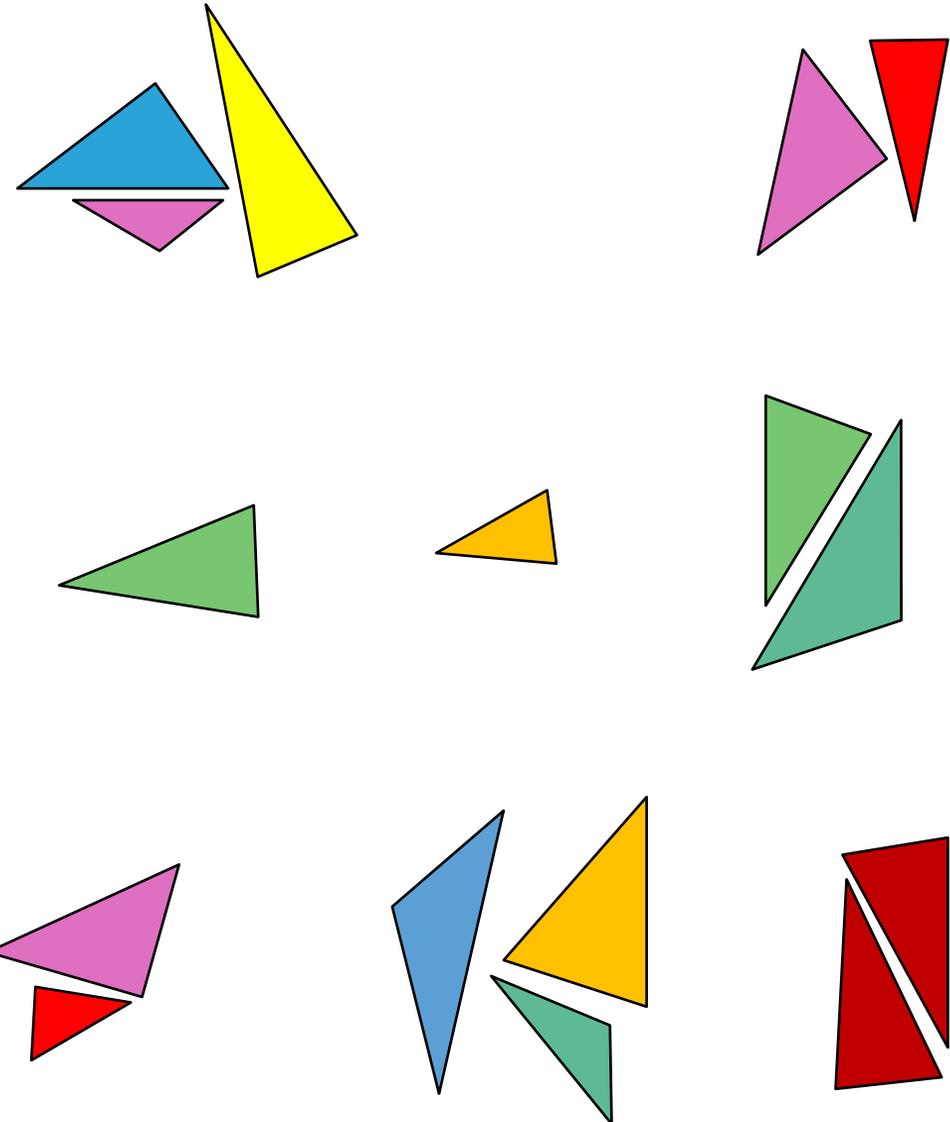
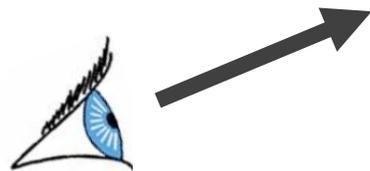
- For rendering, we will want to learn to run before we can walk
- Find ways to speed up the basic loop for visibility resolution
- Enter “spatial acceleration structures”
- Essentially, pre-process the scene geometry into a structure that reduces expected traversal time to something more reasonable



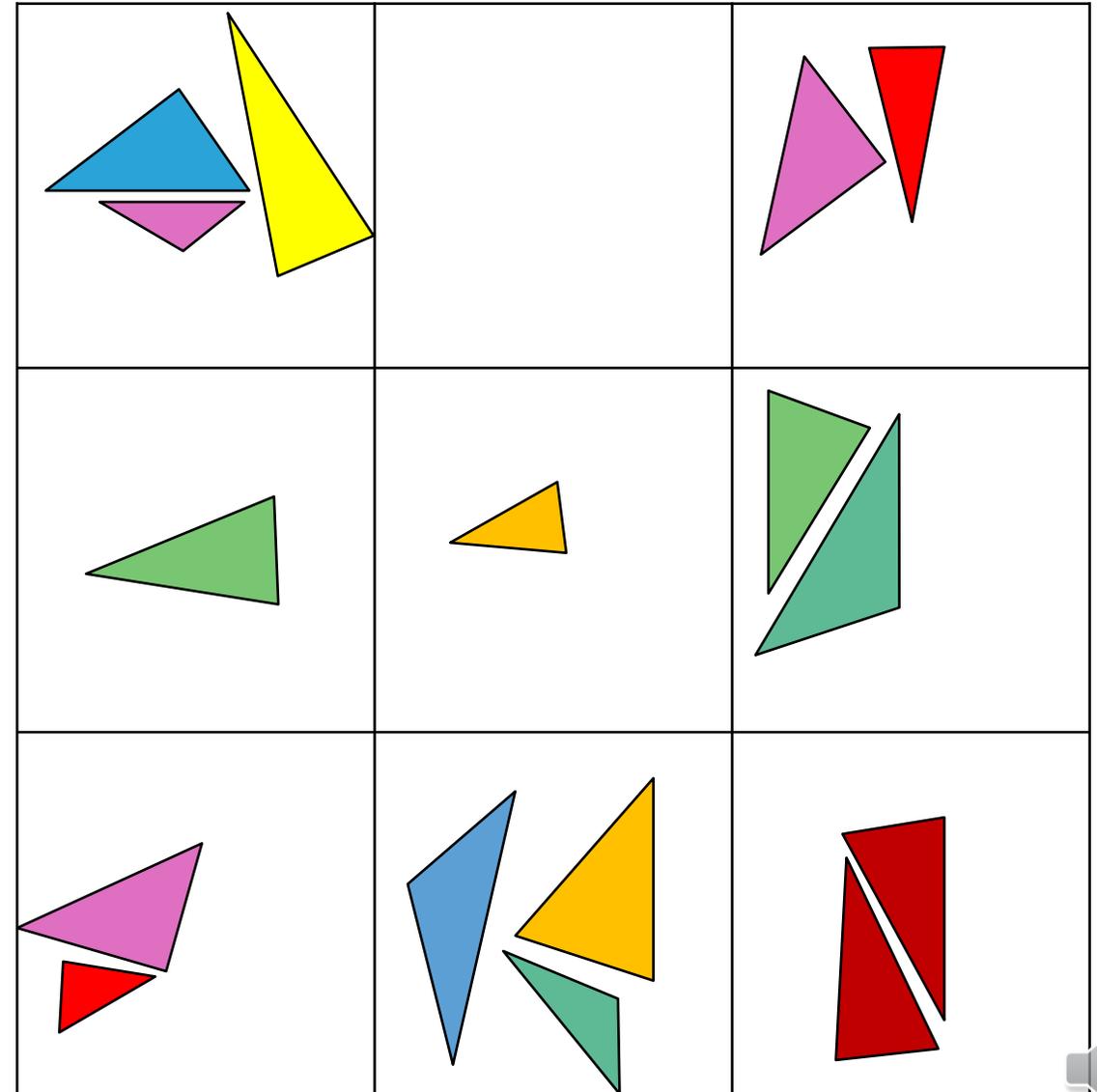
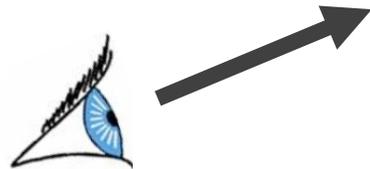
Structure	Additional Memory	Building Time	Traversal Time
none	none	none	abysmal



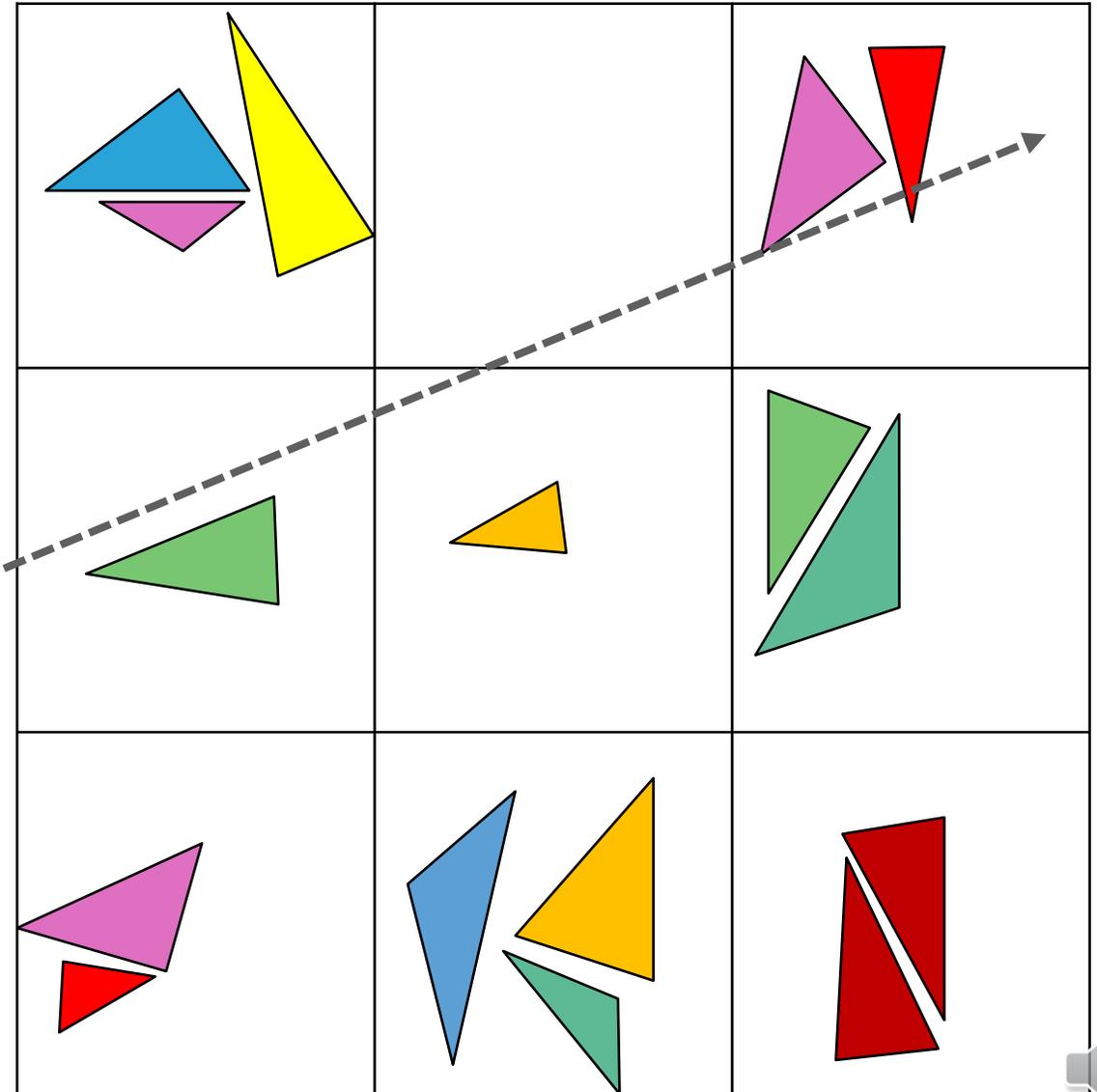
- Consider a group of triangles
- Which ones should we test?



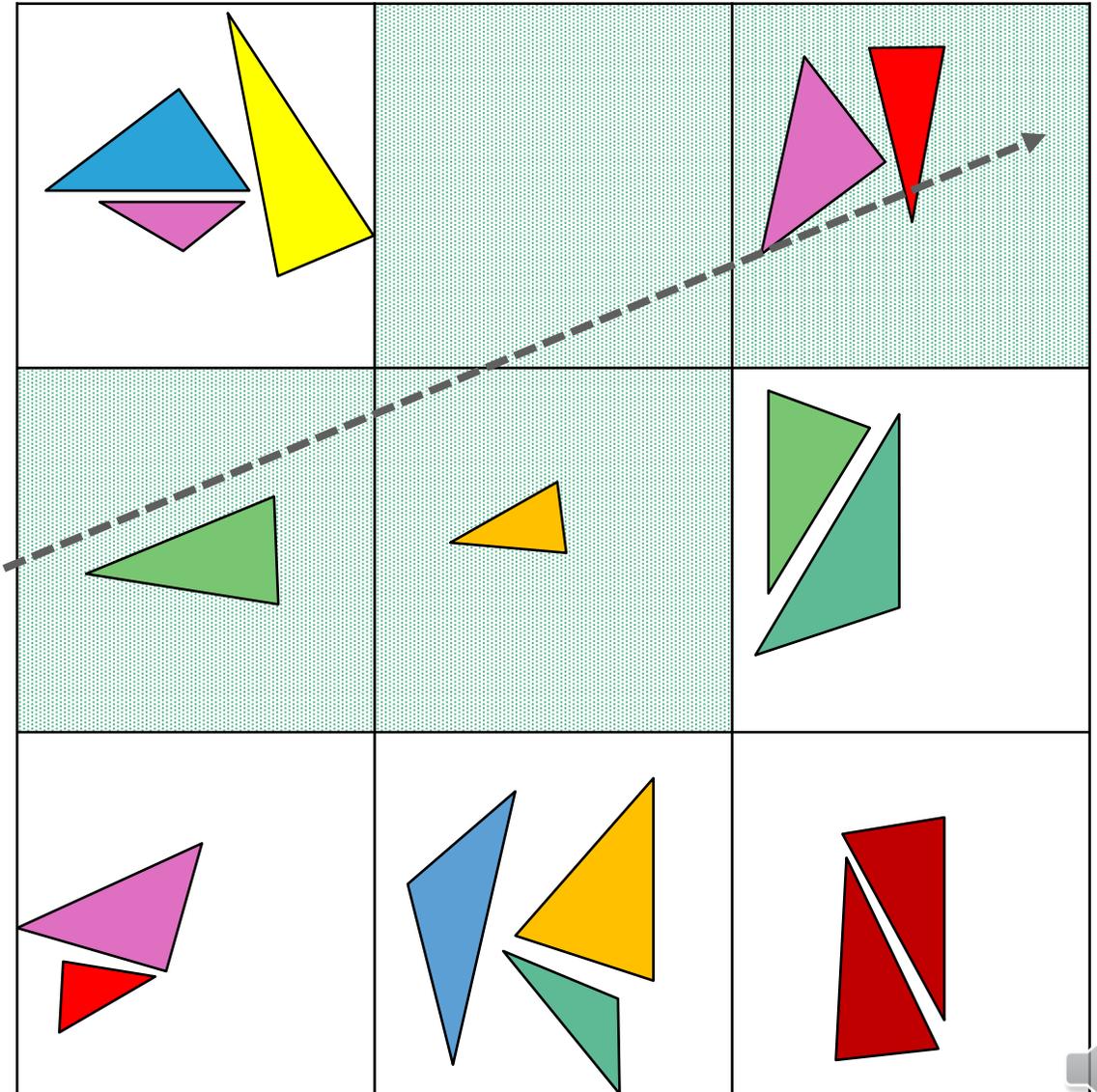
- Overlay scene with regular grid
- Sort triangles into cells
- Traverse cells and test against their contents



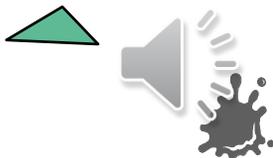
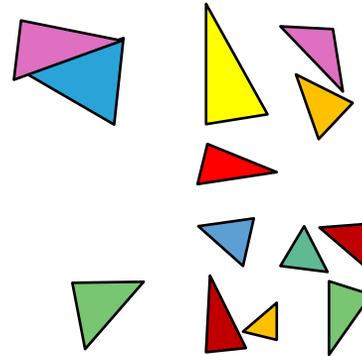
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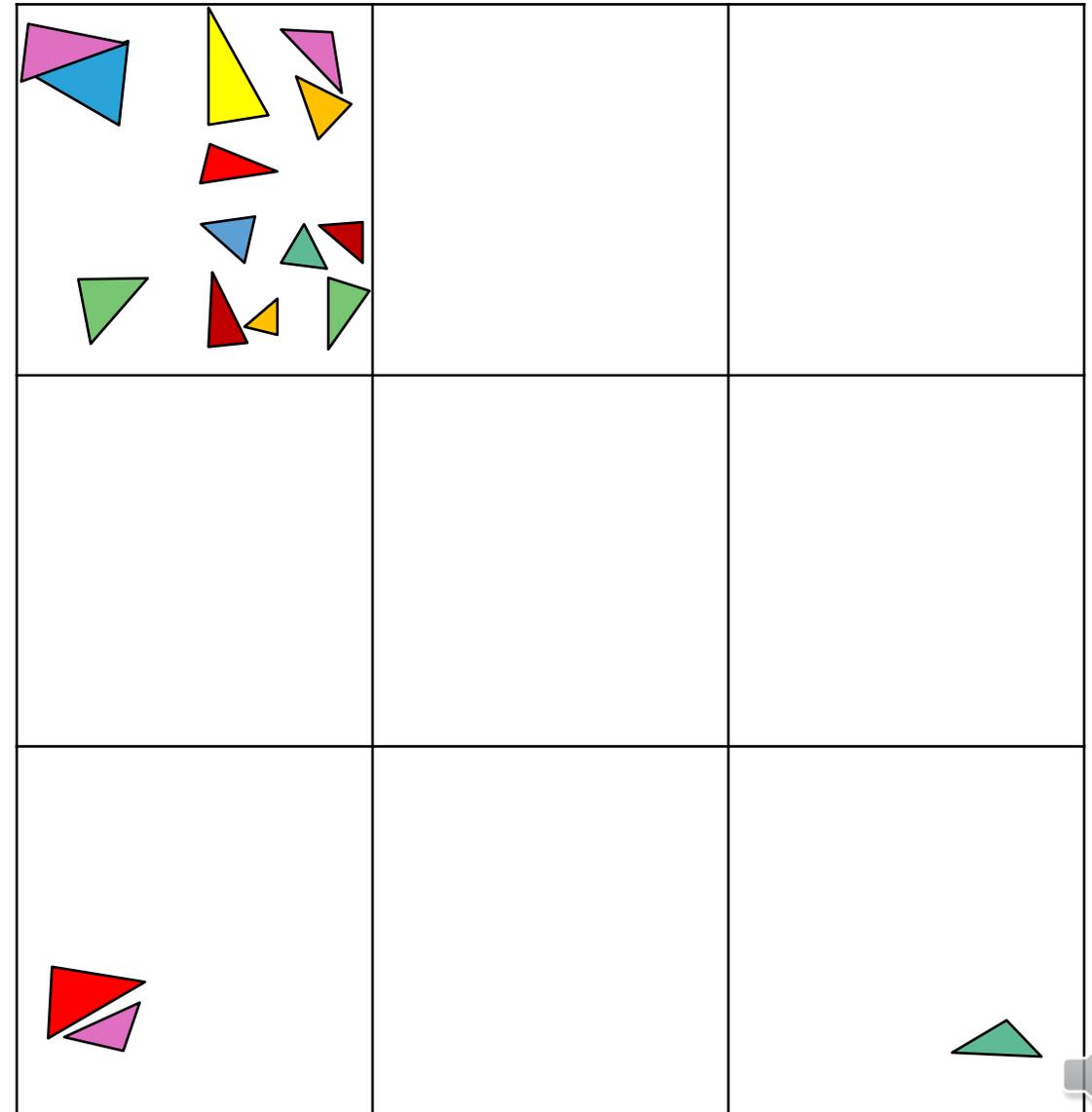
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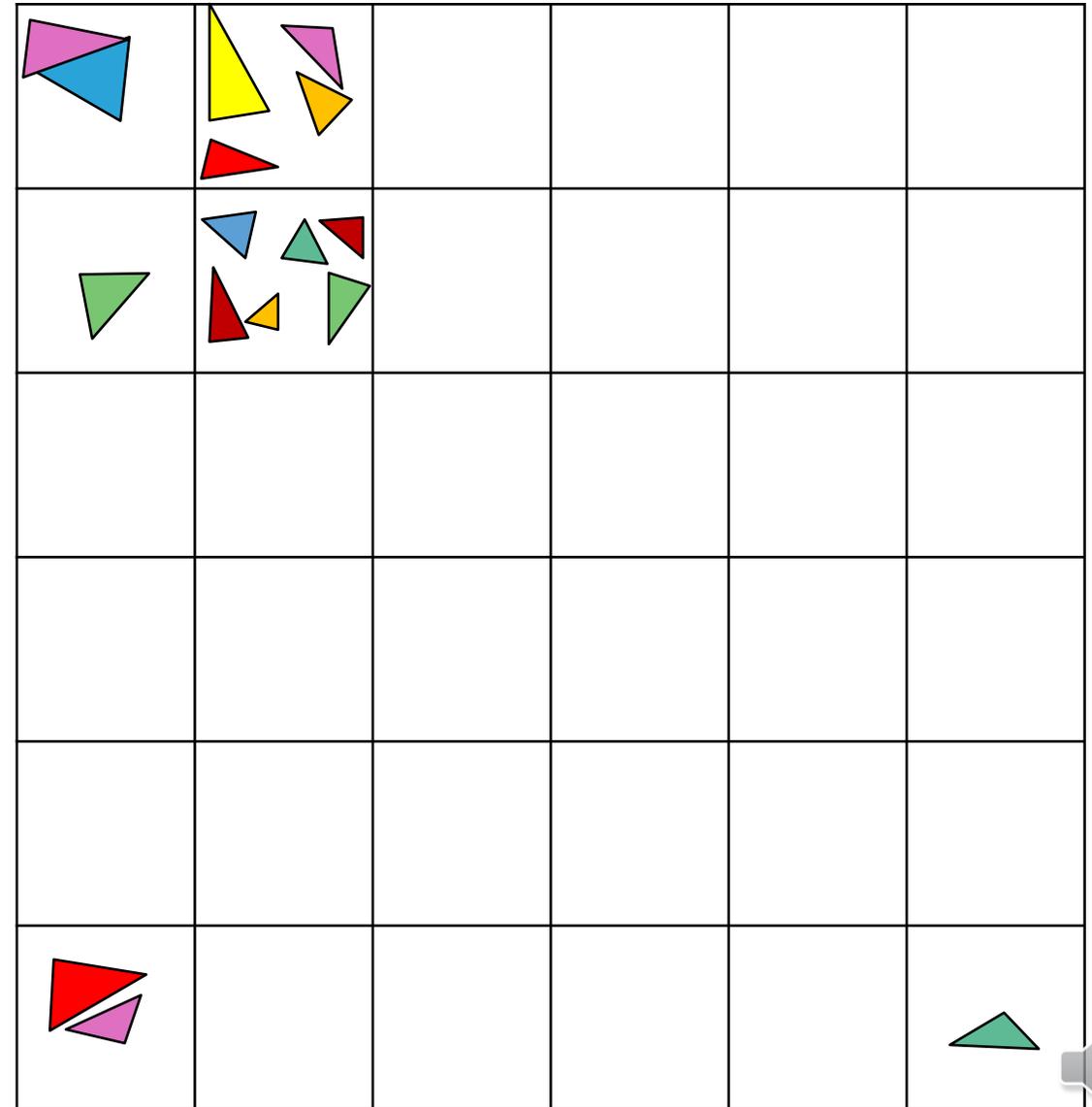
- Geometry is usually not uniform
- Comes in clusters (buildings, characters, vegetation...)



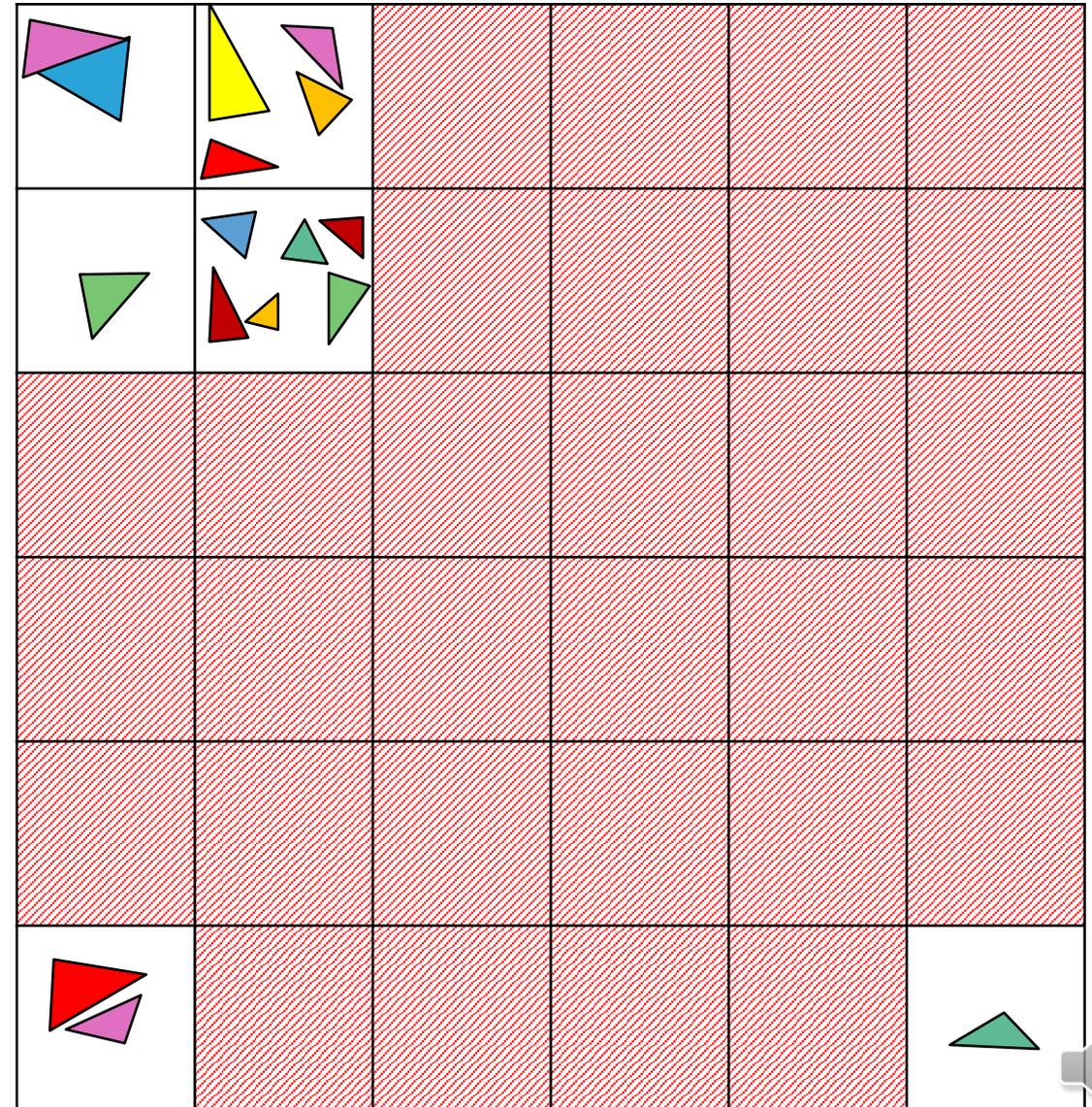
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- **Almost all triangles in one cell!
Hitting this cell will be costly!**



- Geometry is usually not uniform
- Comes in clusters (buildings, characters, vegetation...)
- ~~Almost all triangles in one cell!
Hitting this cell will be costly!~~
- Using a finer grid works



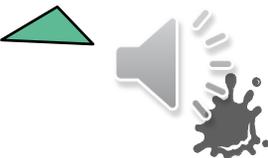
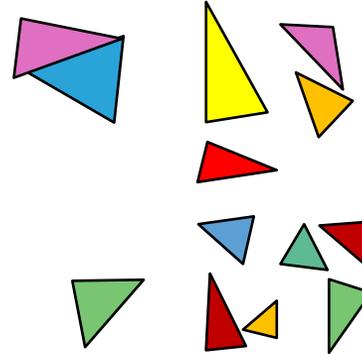
- Geometry is usually not uniform
- Comes in clusters (buildings, characters, vegetation...)
- ~~Almost all triangles in one cell!
Hitting this cell will be costly!~~
- Using a finer grid works, but **most of its cells are unused!**



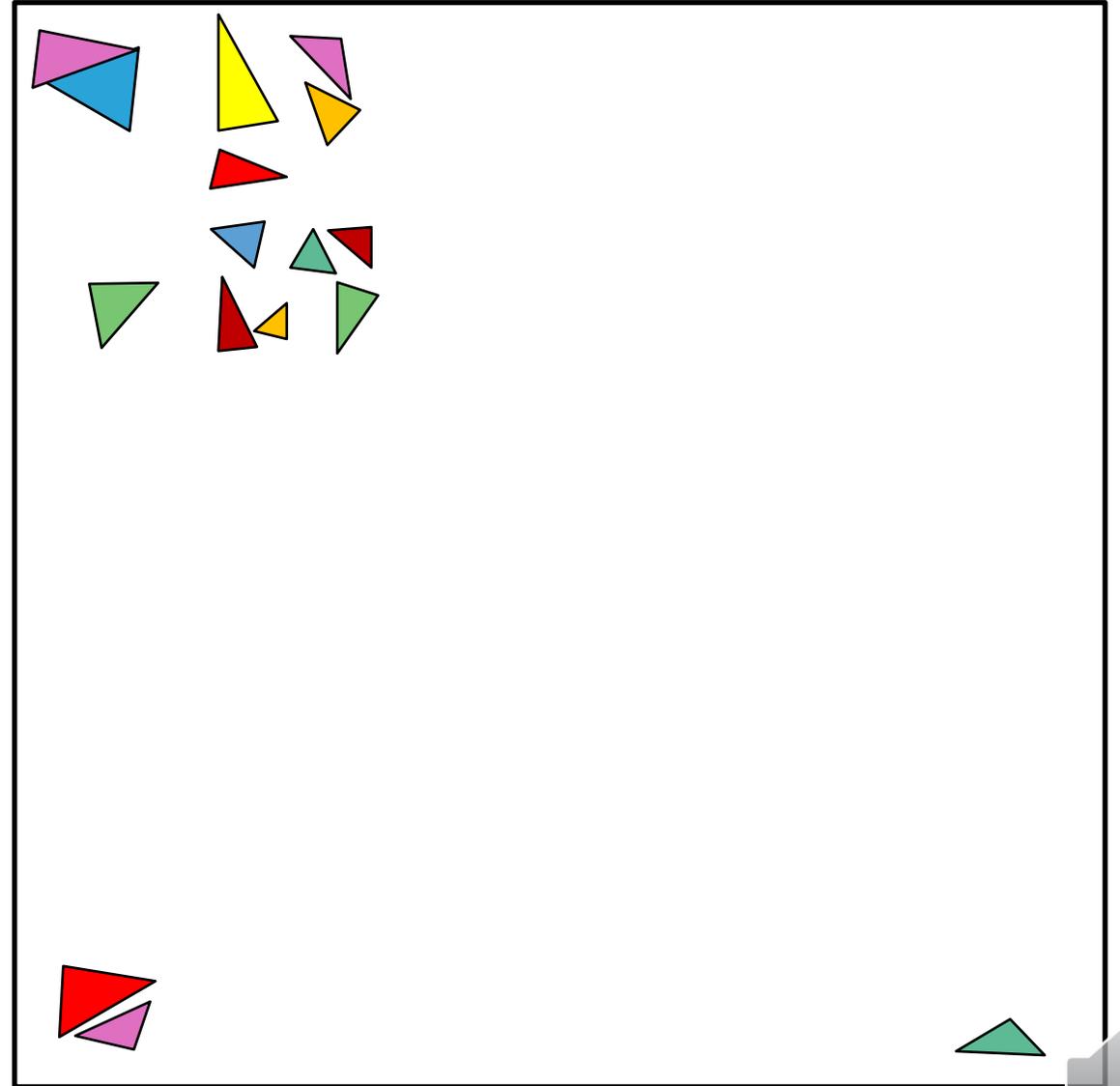
Structure	Memory Consumption	Building Time	(Expected) Traversal Time
none	none	none	abysmal
Regular Grid	low – high (resolution)	low	uniform scene: ok otherwise: bad



- Start with scene bounds, do finer subdivisions only if needed
- Define parameters S_{max} , N_{leaf}
- Recursively split bounds into *quadrants* (2D) or *octants* (3D)
- Stop after S_{max} subdivisions or if no cell has $> N_{leaf}$ triangles

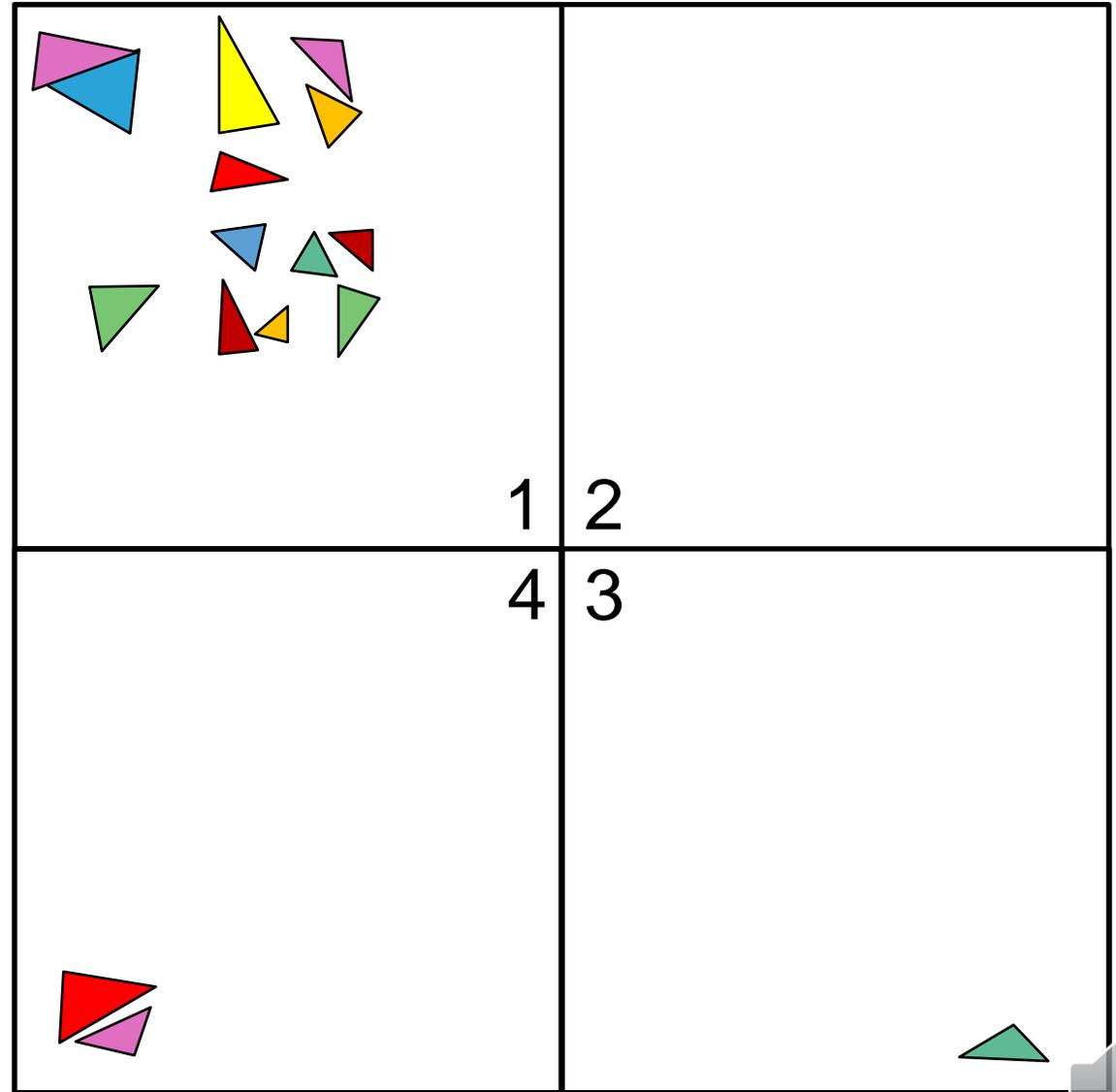


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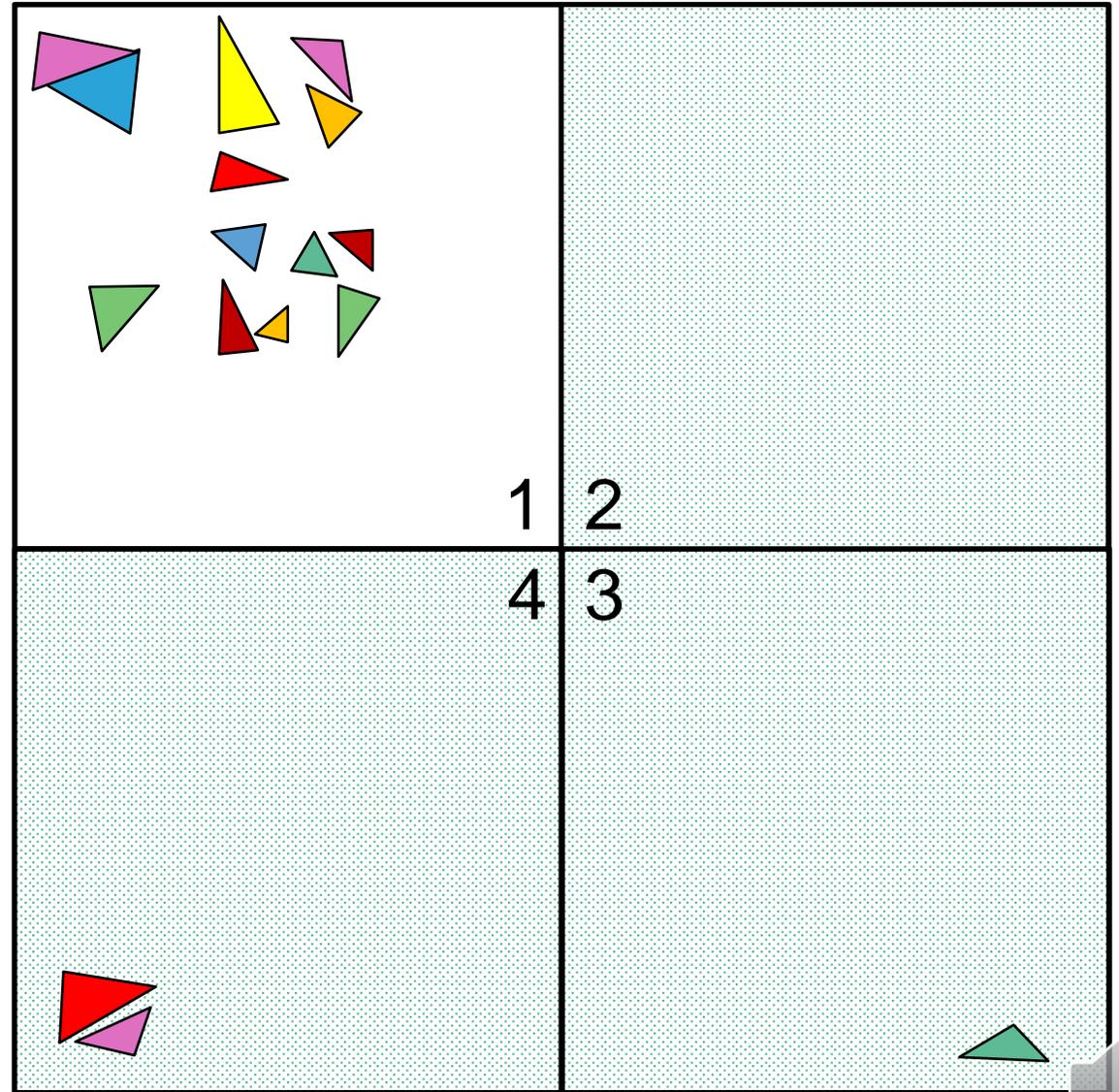
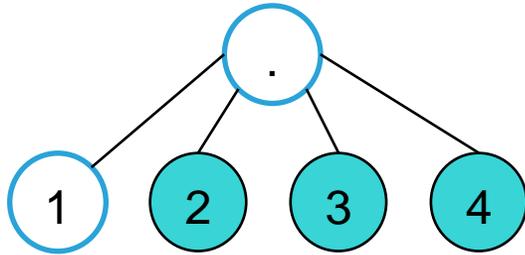


Quad and Octrees: $N_{leaf} = 4$

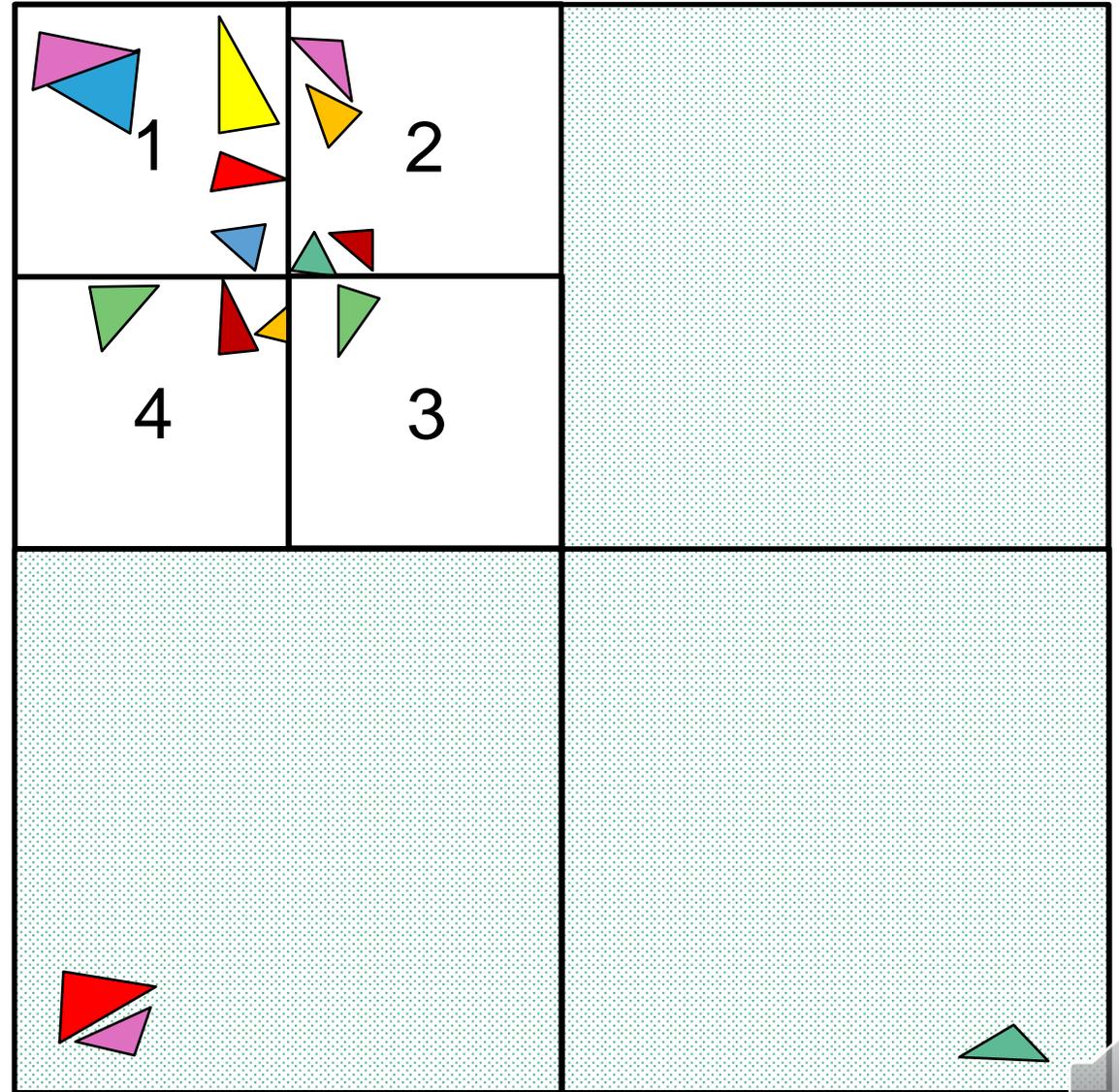
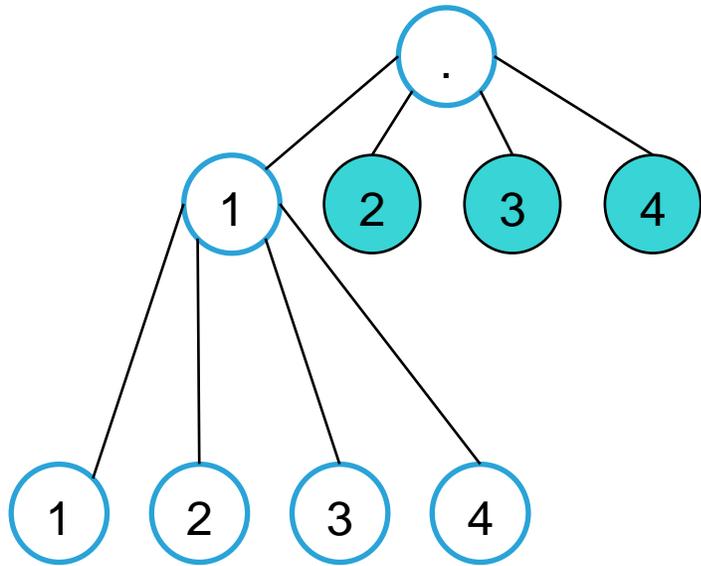
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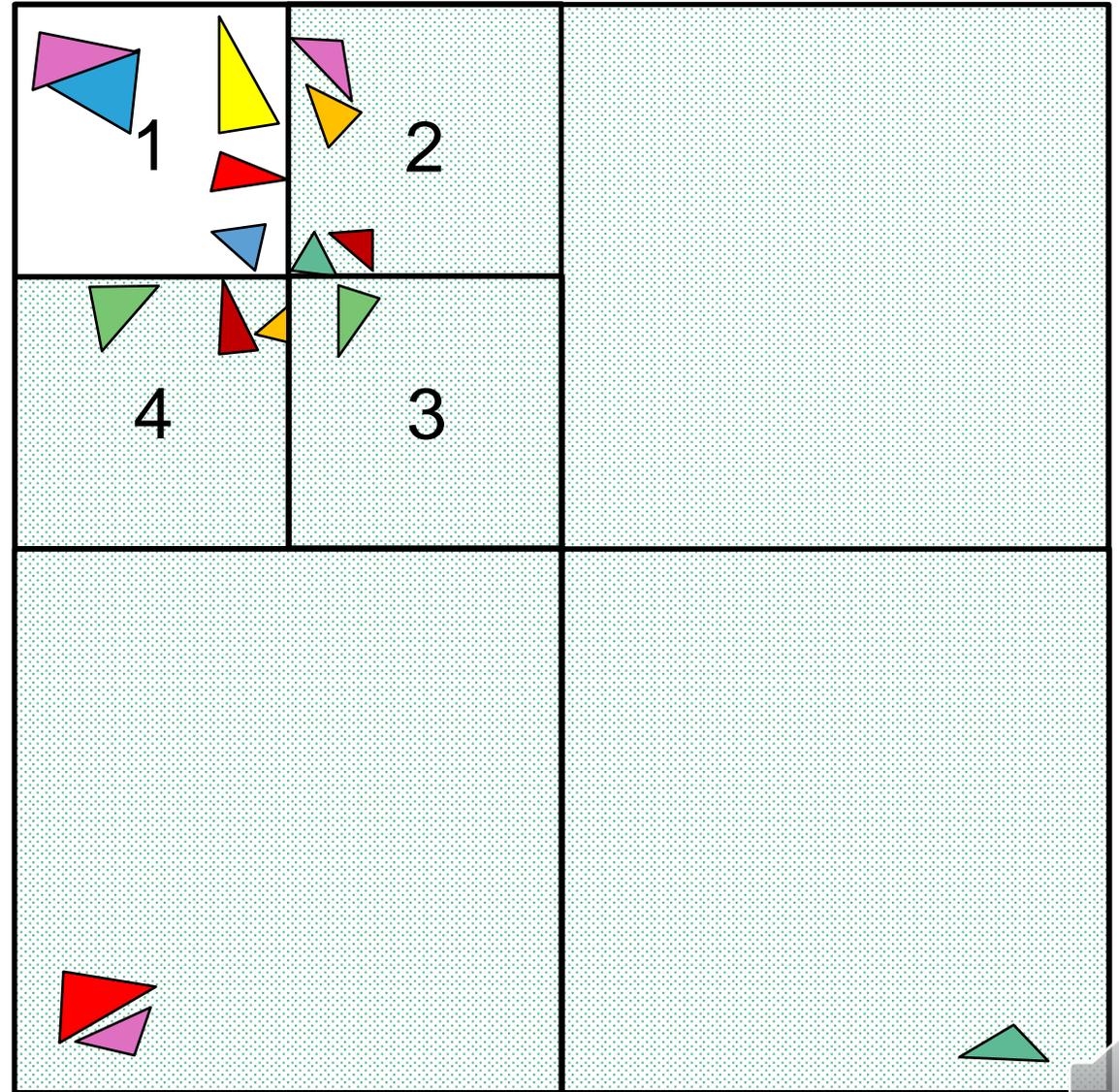
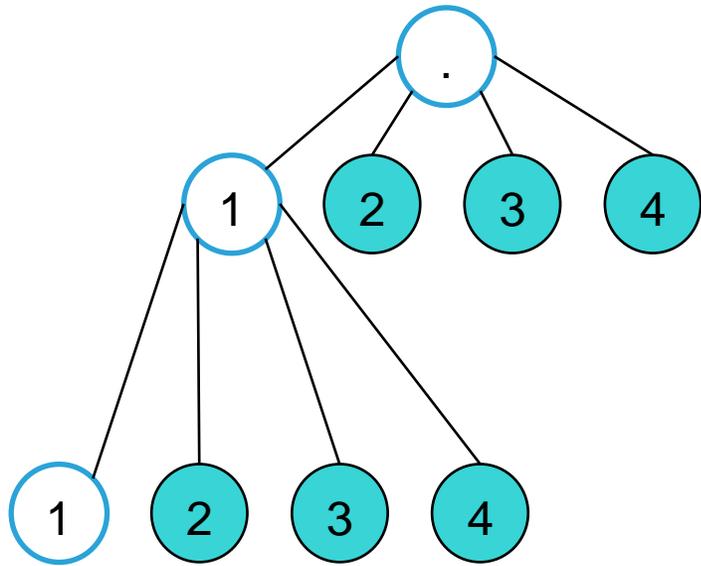
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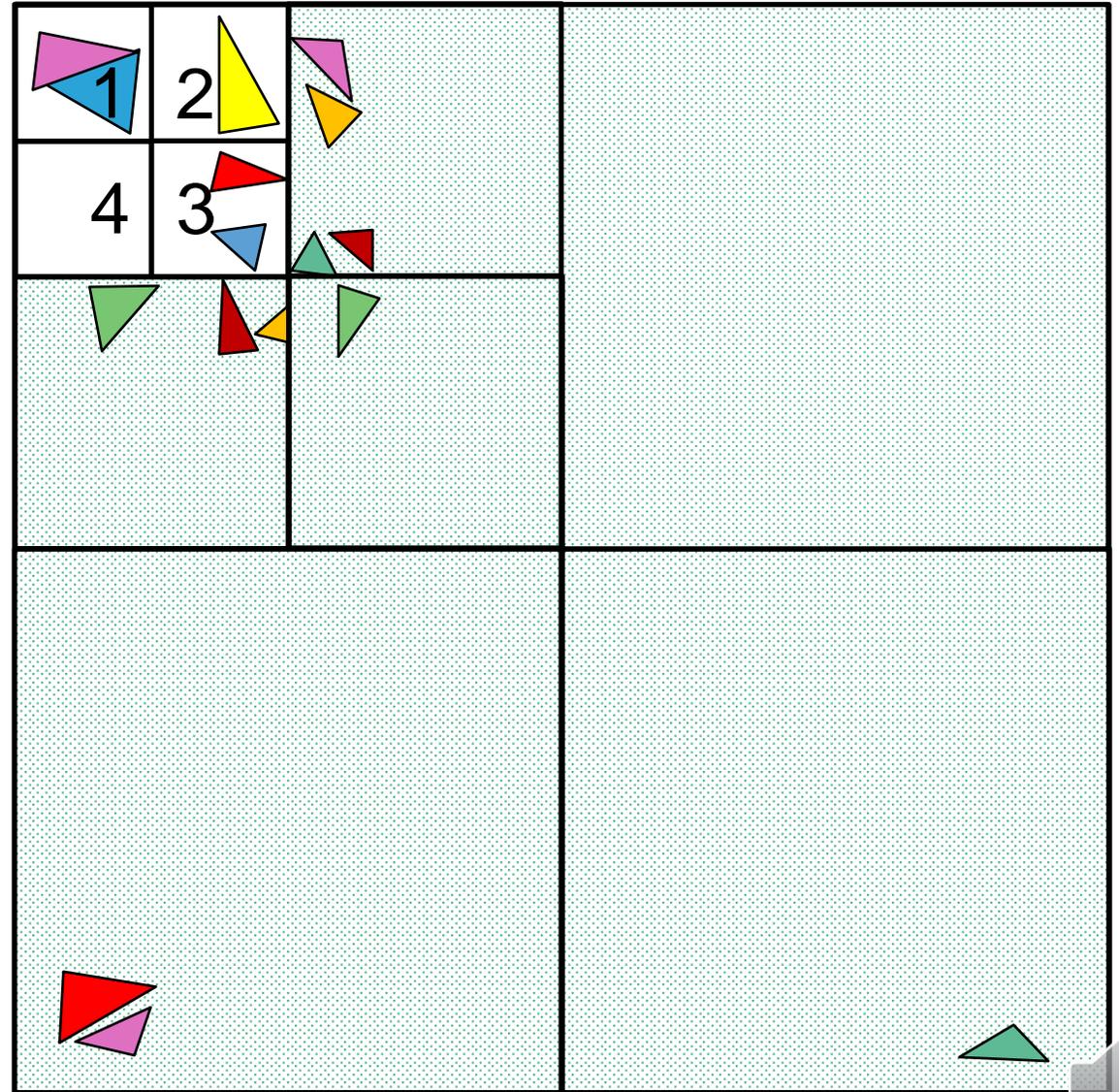
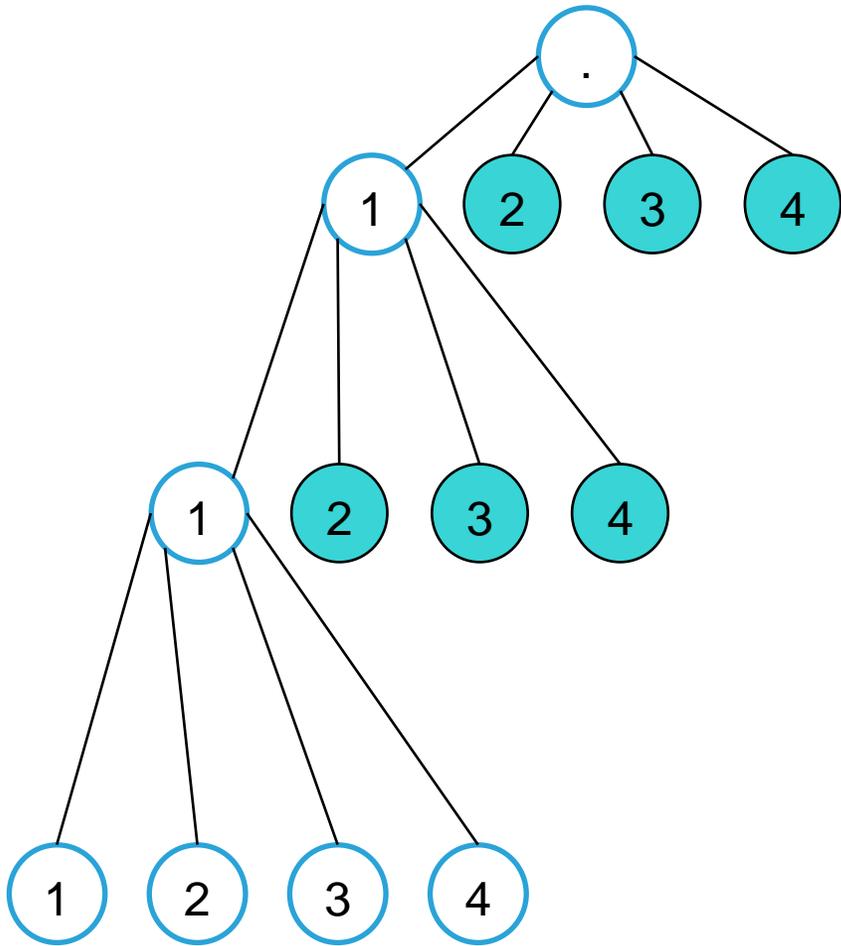
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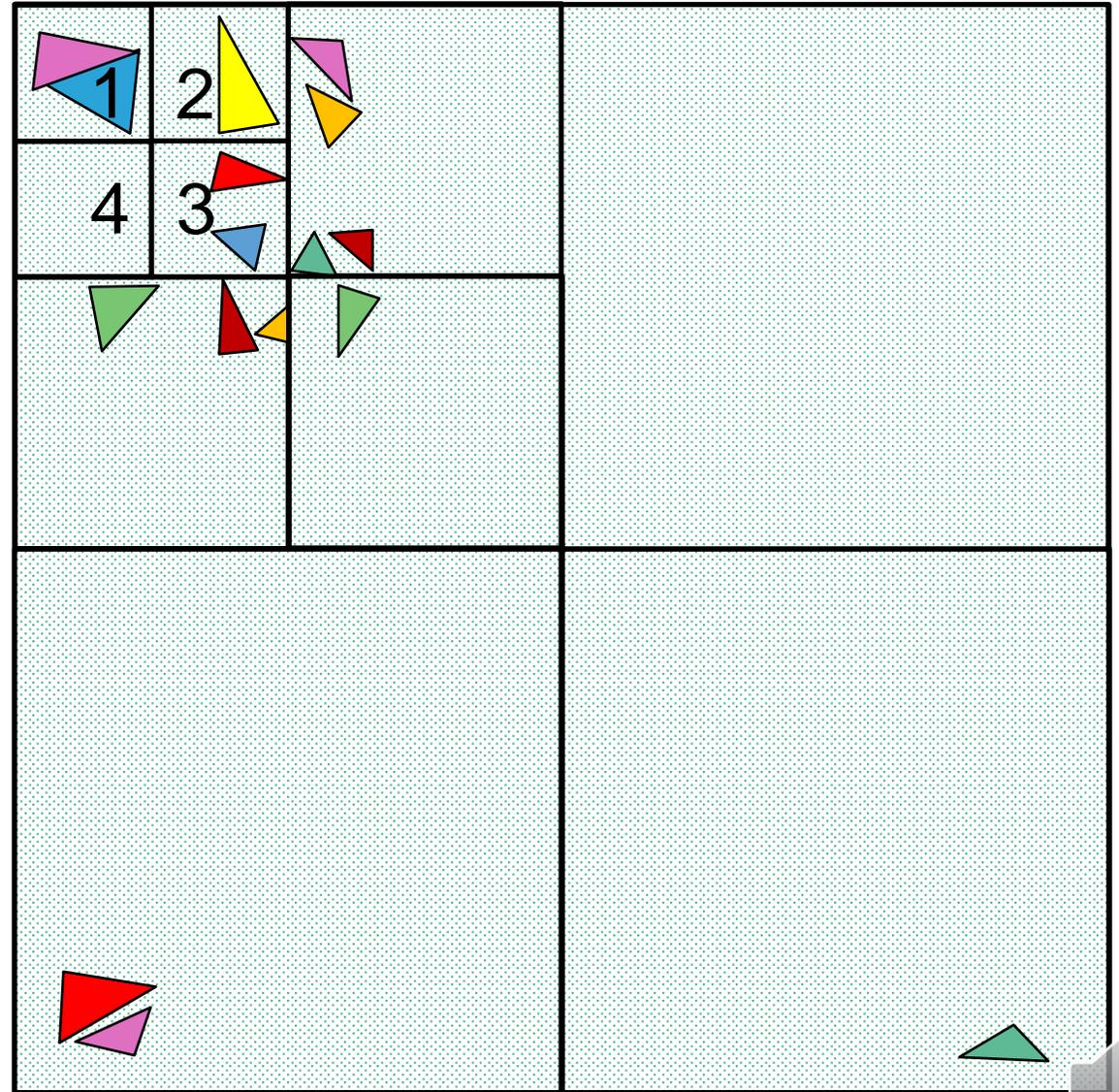
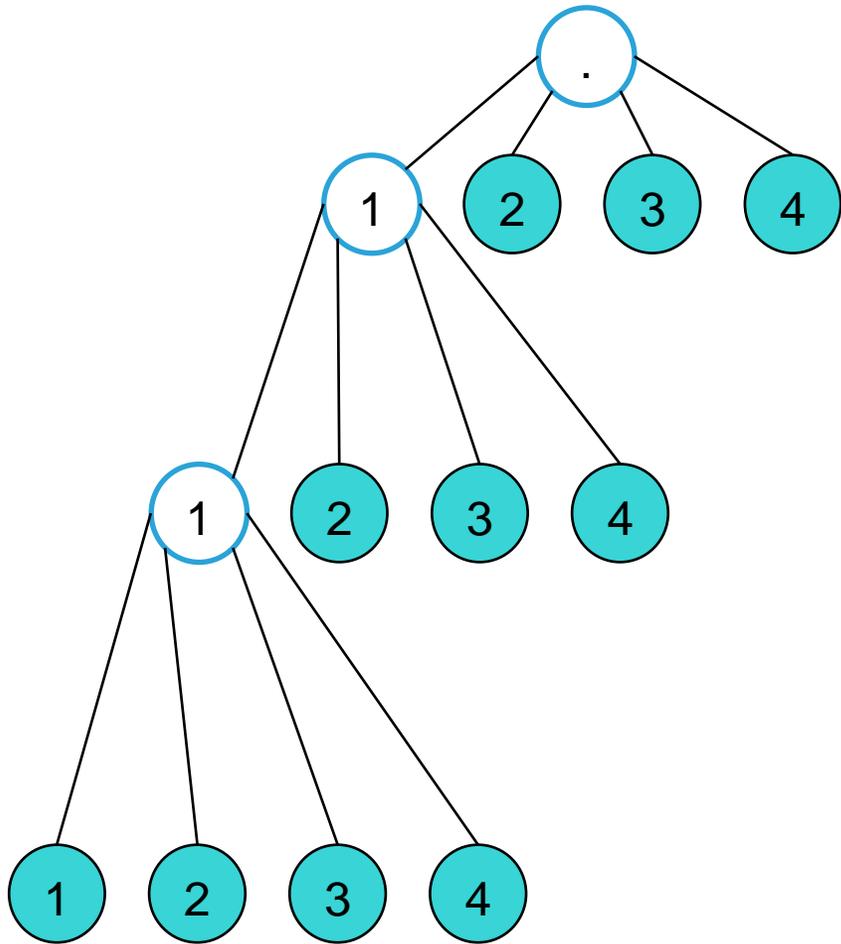
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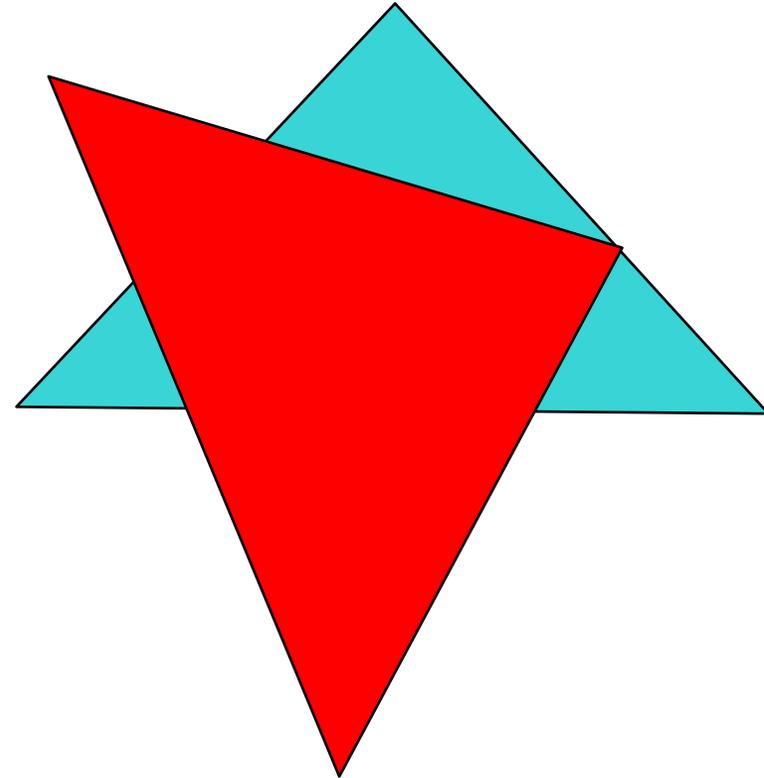
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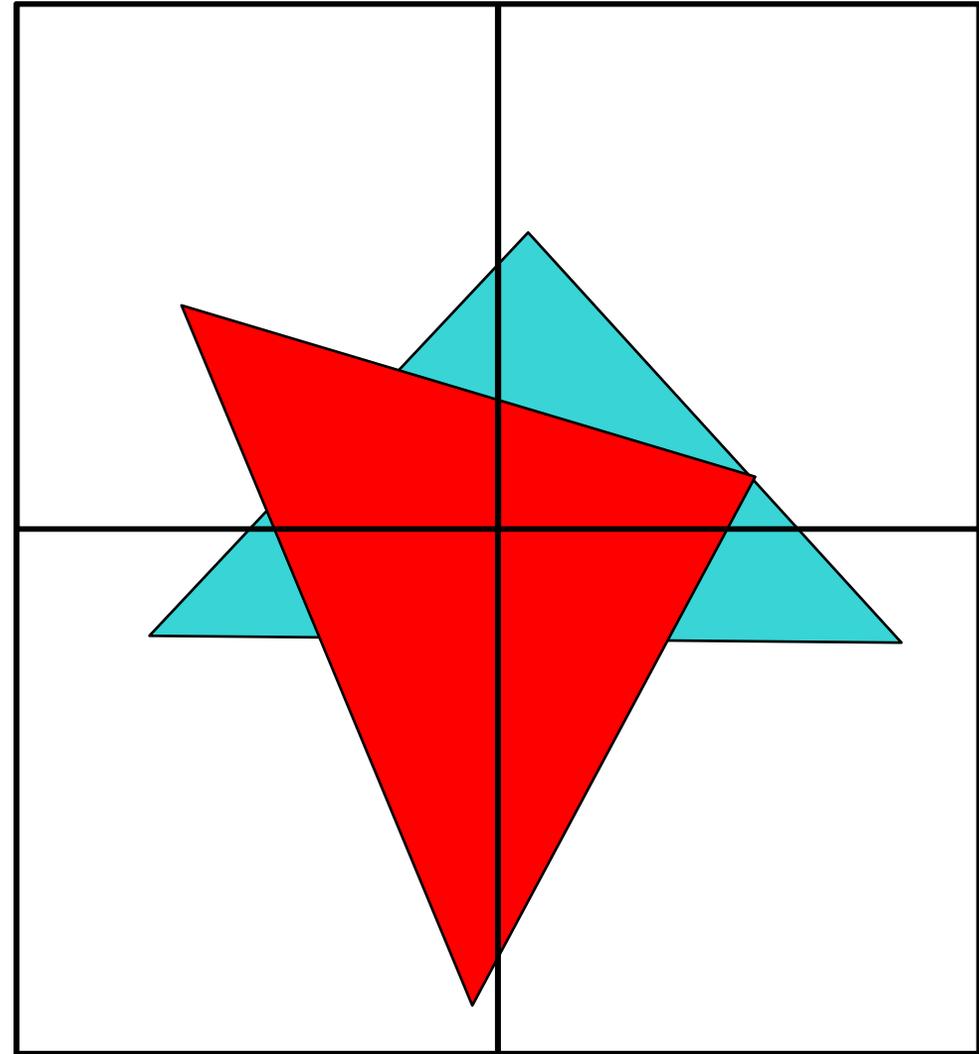
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- Triangles may not be contained within a quadrant or octant
- Triangles must be referenced in all overlapping cells or *split* at the border into smaller ones



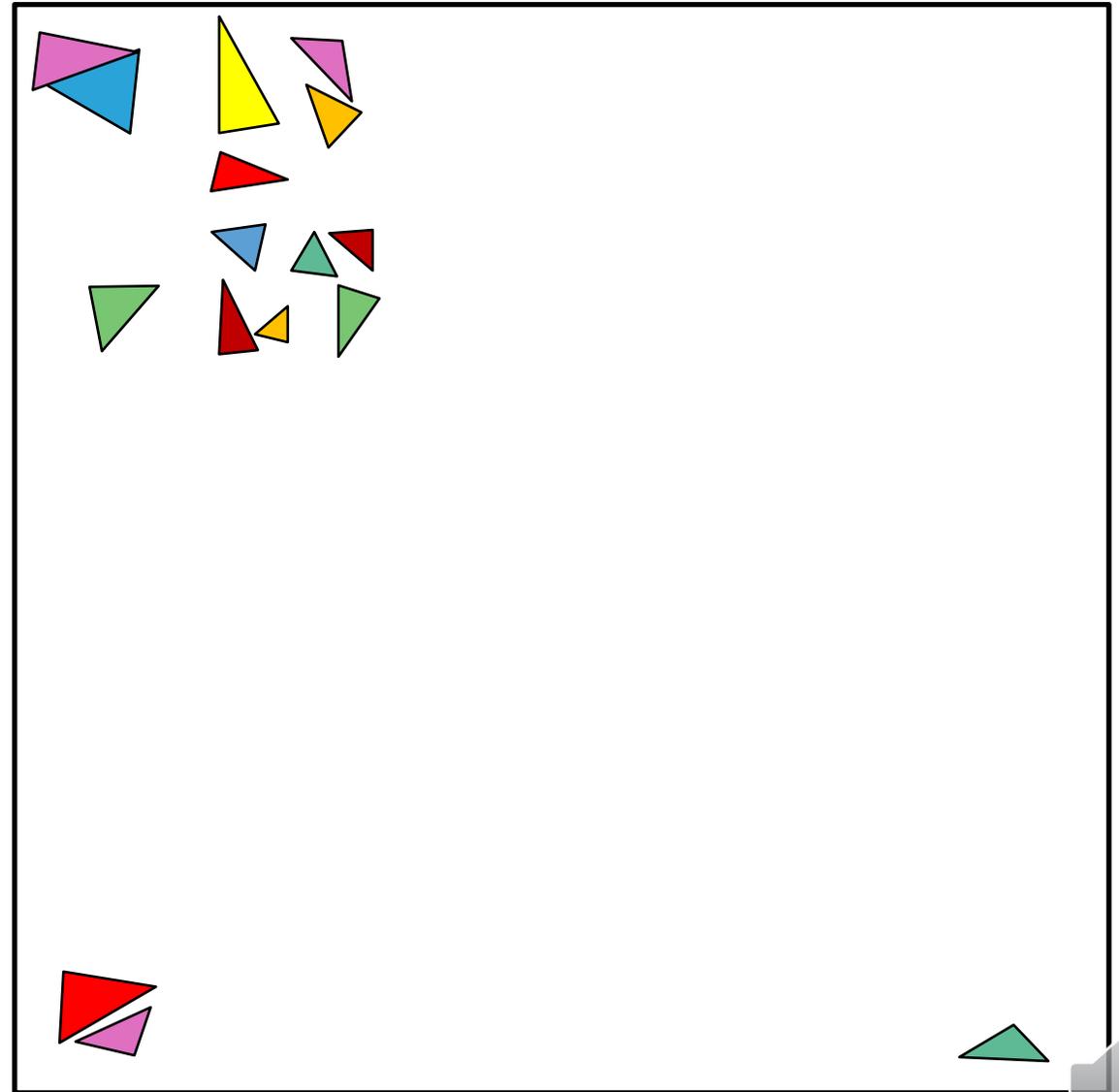
- Triangles may not be contained within a quadrant or octant
- Triangles must be referenced in all overlapping cells or *split* at the border into smaller ones
- Can drastically increase memory consumption!



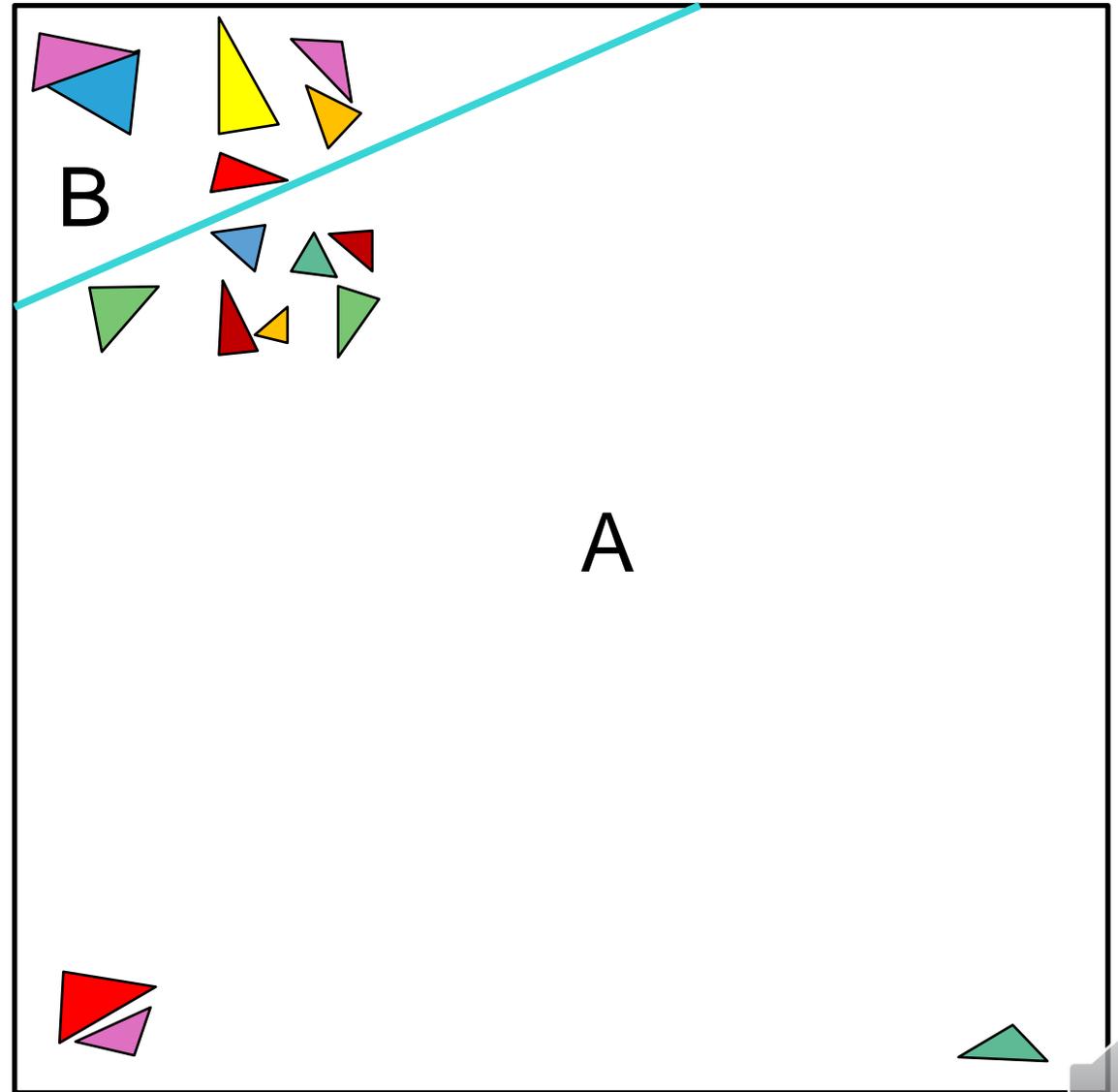
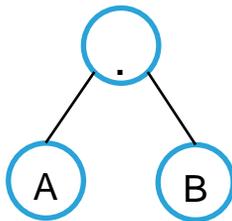
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Regular Grid	low – high (resolution)	low	uniform scene: ok otherwise: bad
Quadtree/Octree	low – high (overlap/uniformity)	low	good



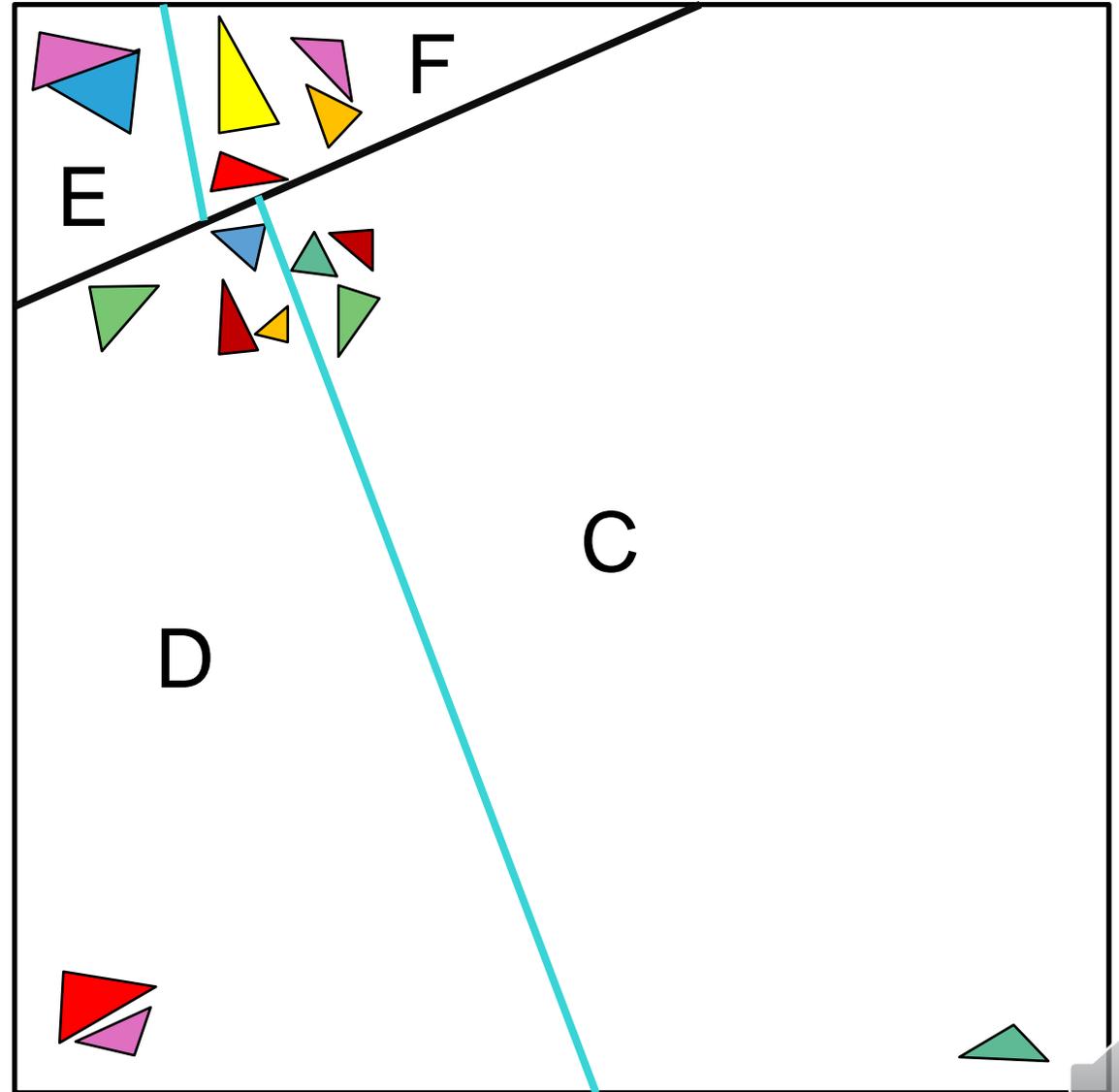
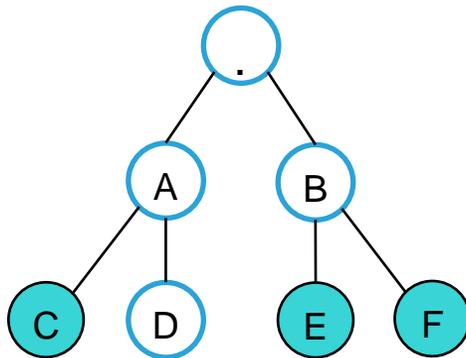
- Binary Space Partition Tree
 - Recursive split via *hyperplanes*
 - Left/right child nodes treat objects in each *half-space*
 - Splits can be arbitrary!



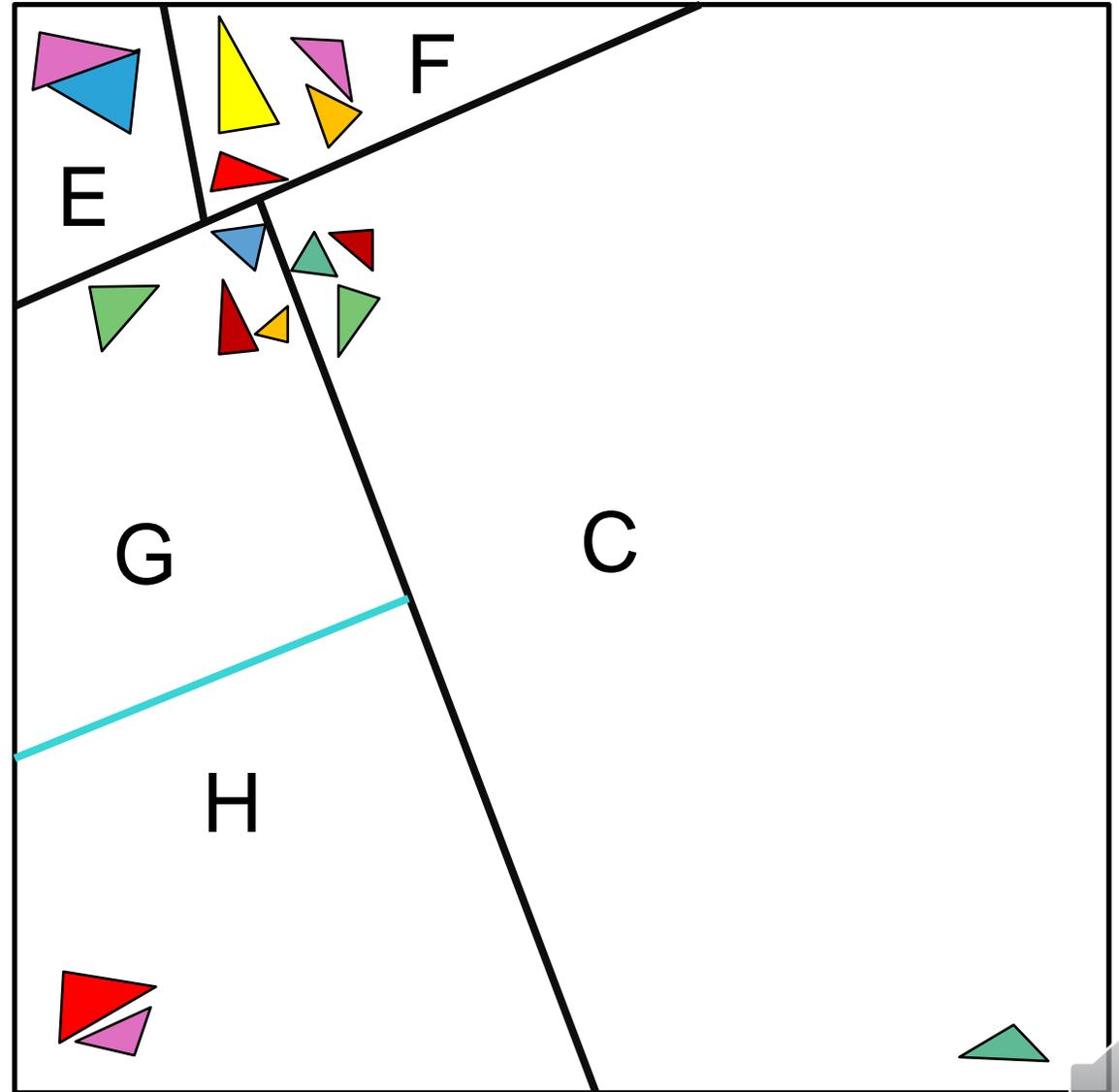
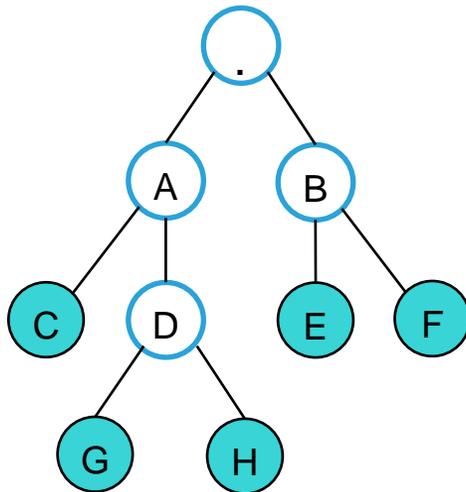
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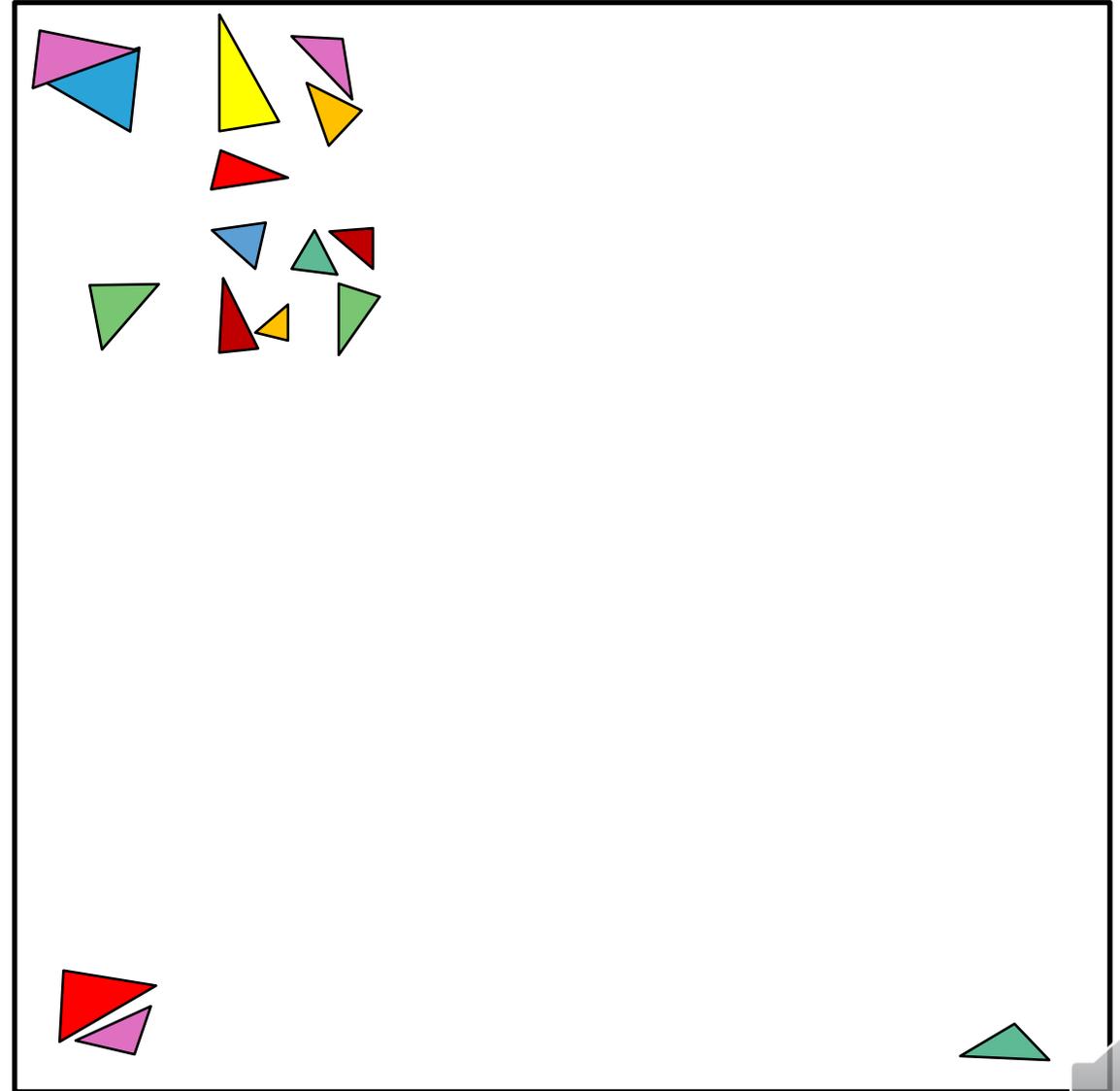
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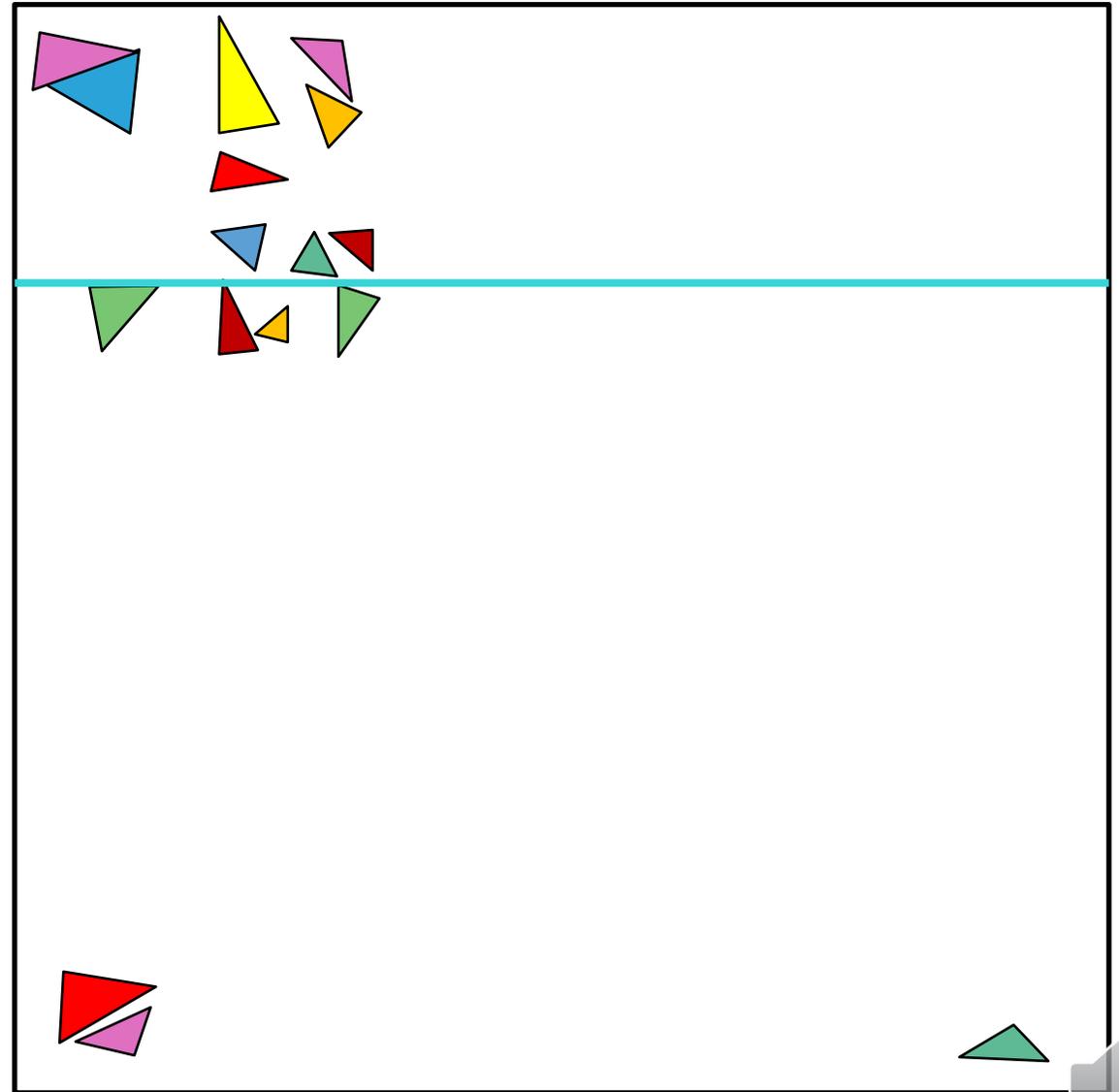
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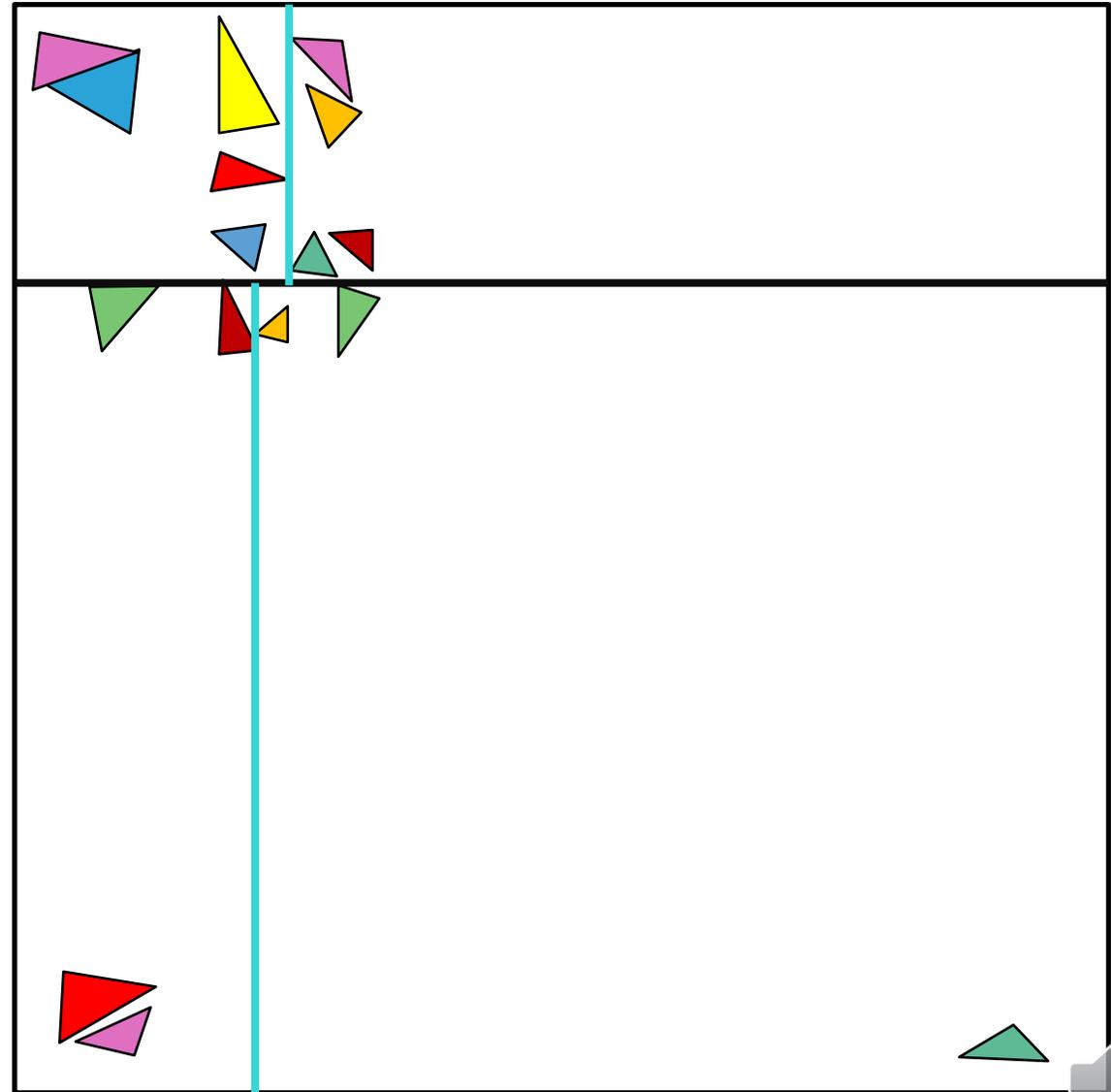
- Binary Space Partition Tree
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- K-dimensional (K-d) Tree
 - Every hyperplane must be perpendicular to a base axis
 - Limits search space for splits



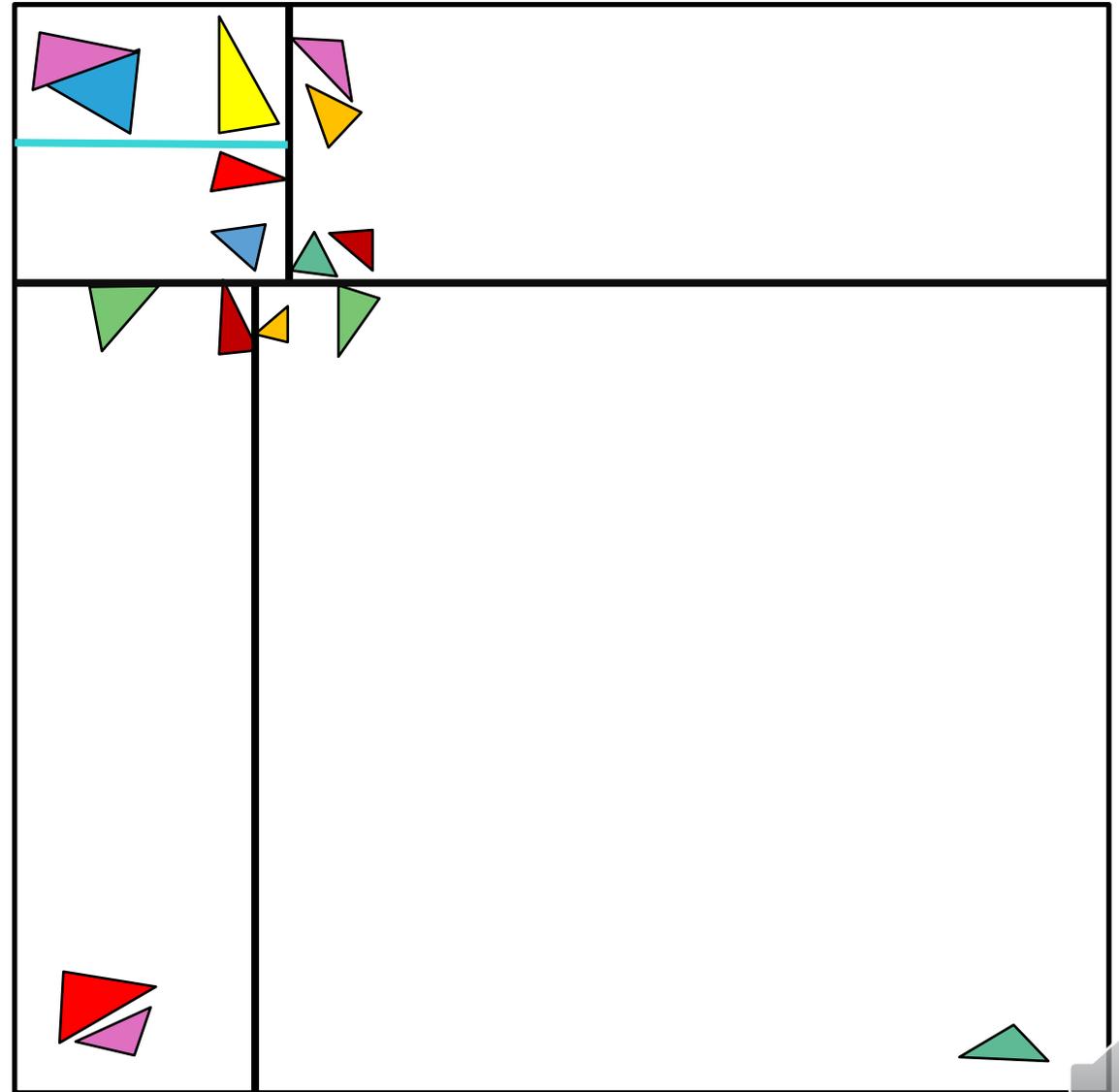
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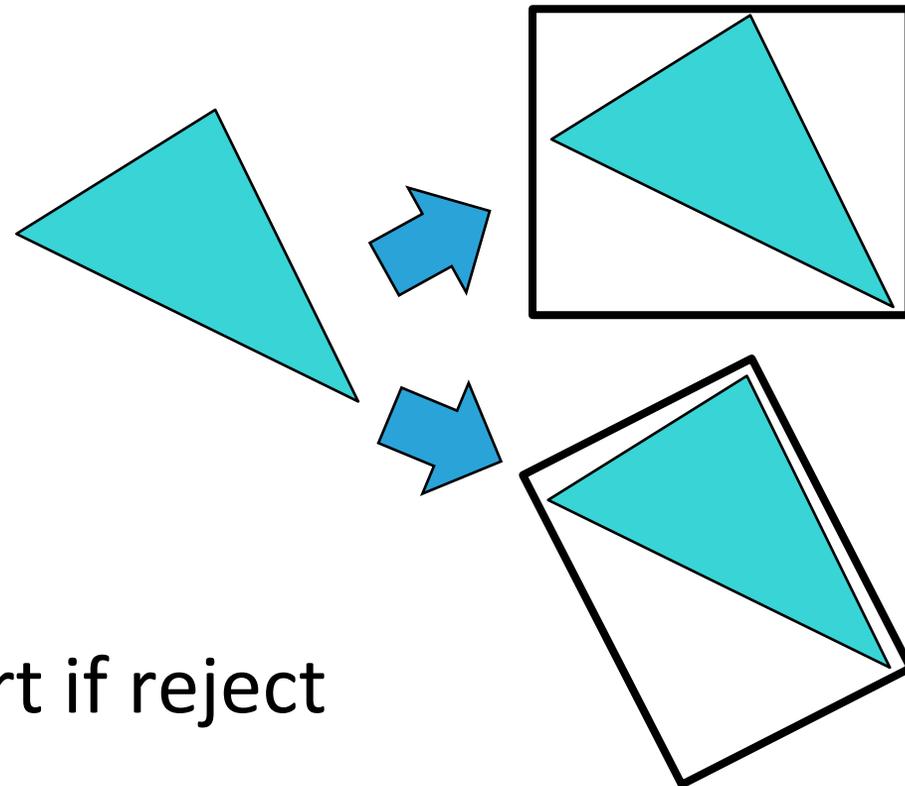
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Structure	Memory Consumption	Building Time	(Expected) Traversal Time
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Regular Grid	low – high (resolution)	low	uniform scene: ok otherwise: bad
Quadtree/Octree	low – high (overlap/uniformity)	low	good
K-d Tree	low – high (overlap)	low – high	good – excellent



- Find enclosing (“conservative”) volumes that are easier to test
- Ideally: tight, but easy to check for intersection with ray
- Common choices:
 - Bounding Spheres
 - Bounding Boxes
 - Axis-aligned (AABB)
 - Oriented (OBB)
- Saves on computational effort if reject

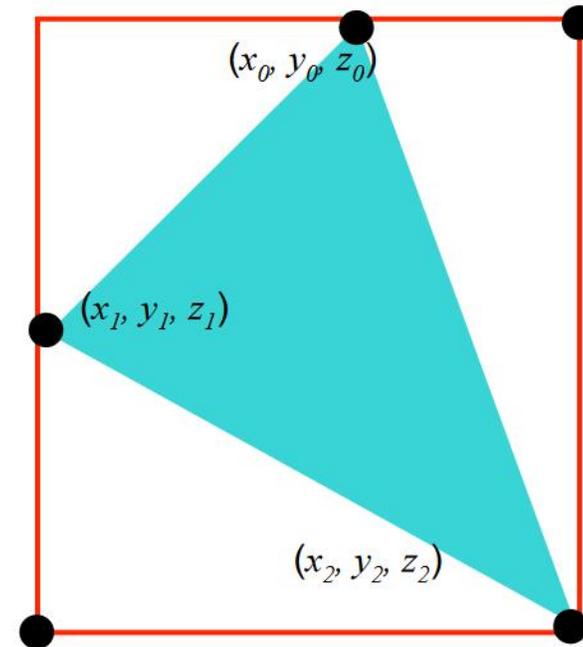


- AABBs are defined by their two extrema (min/max)

- Linear run time to compute

- Iterate over all vertices
- Keep min/max values for each dimension
- Done!

$$(x_{min} \ y_{min} \ z_{min})$$
$$= (\min(x_0, x_1, x_2),$$
$$\min(y_0, y_1, y_2),$$
$$\min(z_0, z_1, z_2))$$



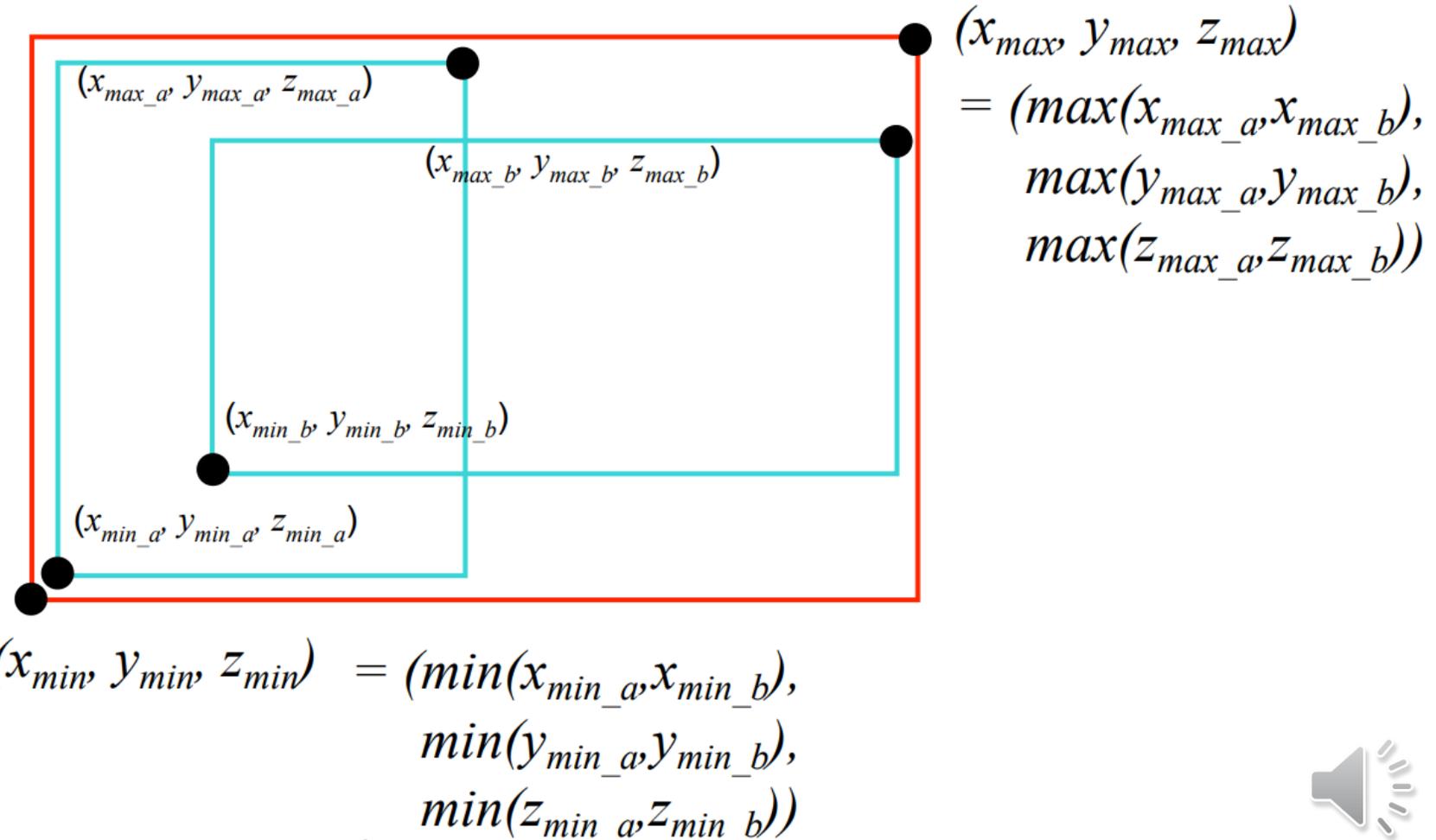
$$(x_{max} \ y_{max} \ z_{max})$$
$$= (\max(x_0, x_1, x_2),$$
$$\max(y_0, y_1, y_2),$$
$$\max(z_0, z_1, z_2))$$



- Find the AABB that encloses multiple, smaller AABBs

- Operates only on extrema of each smaller AABB

- Merging process is commutative



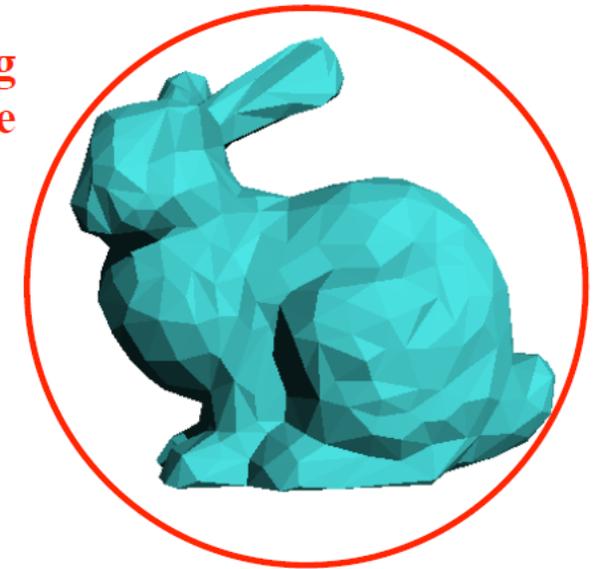
- Bounding spheres need a center \vec{c} and a radius r
- For \vec{c} , can pick the mean vertex position or center of AABB
- Once center is chosen, find vertex position \vec{v}_{max} farthest from it
- $r = |\vec{c} - \vec{v}_{max}|$

bounding
sphere



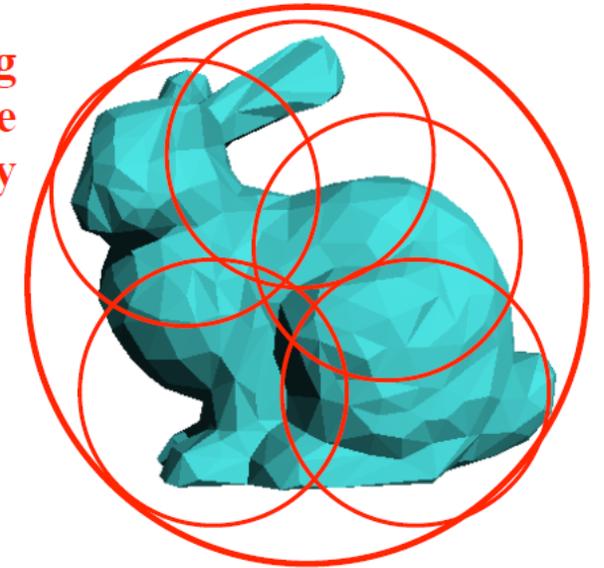
- Can also be applied to entire objects
- Reject entire object if volume is not hit
- Good start, but what if...
 - ...scene is not partitioned into objects?
 - ...objects are extremely large (terrain)?
 - ...objects are extremely detailed (characters)?
 - ...there are millions of objects with ~ 2 triangles each (leaves)?

bounding
sphere



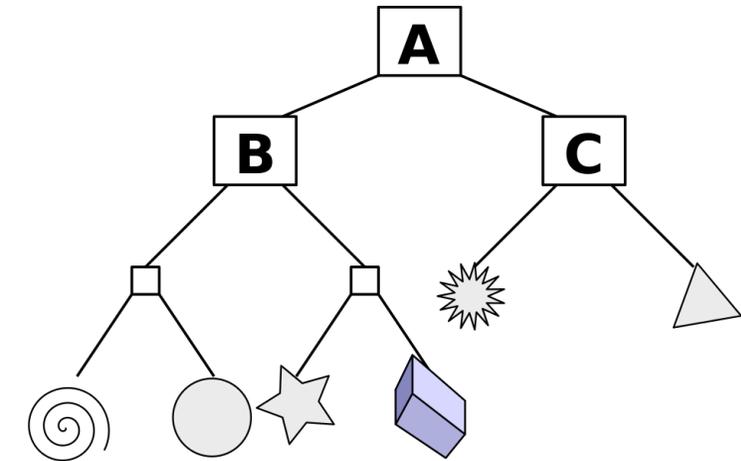
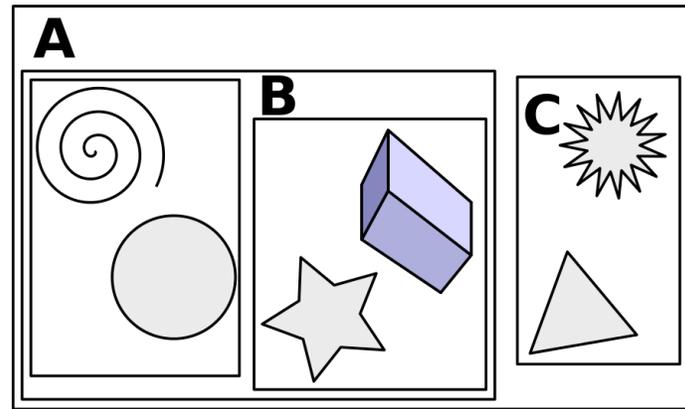
- Each node of the hierarchy has its own bounding volume
- Every node can be
 - An inner node: references child nodes
 - A leaf node: references triangles
- Each node's bounding volume is a subset of its parent's bounding volume (i.e., child nodes are spatially contained by their parents)

bounding
sphere
hierarchy



- The final hierarchy is (again) a tree structure with N leaf nodes

- Leaf nodes can be
 - Individual triangles
 - Clusters (e.g., $\leq 10\Delta$)

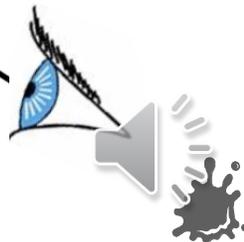
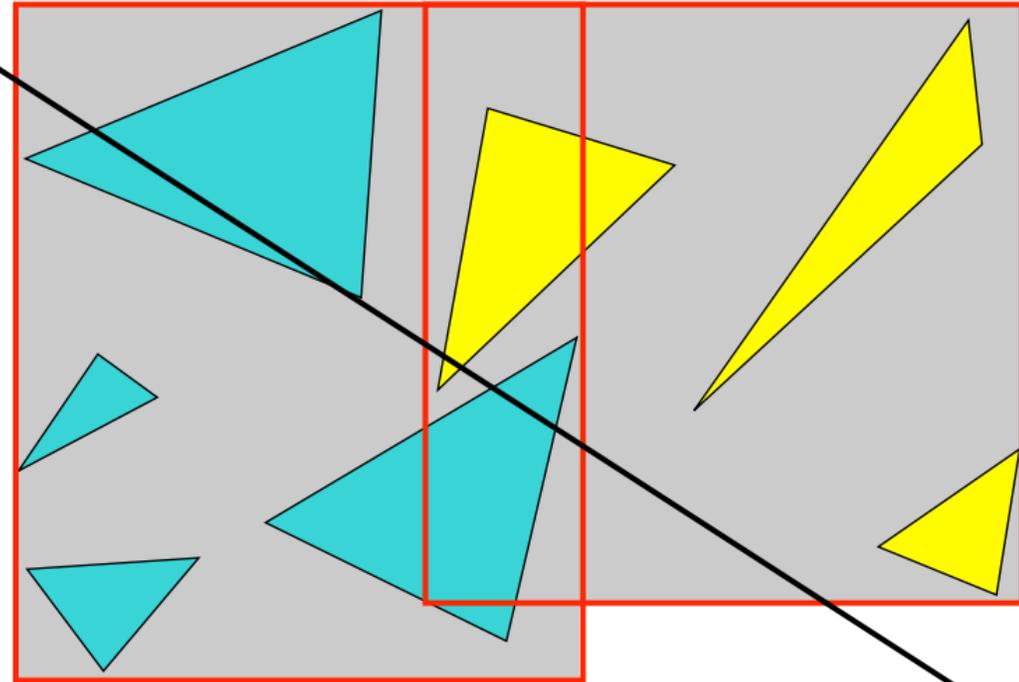


Source: Schreiberx, Wikipedia "Bounding Volume Hierarchy"

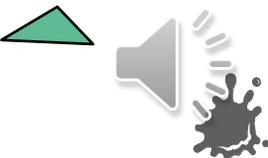
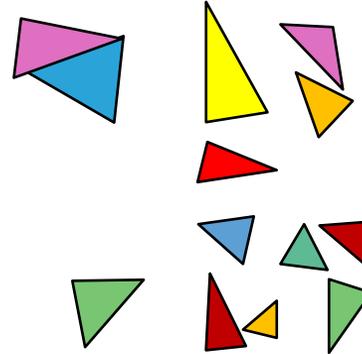
- Total number of nodes for a binary tree: $2N - 1$
 - If balanced, it takes $\sim \log N$ steps to reach a leaf from the root
 - If trees have more than 2 branches, they require fewer nodes



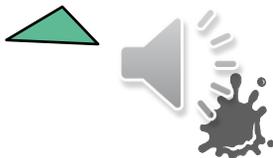
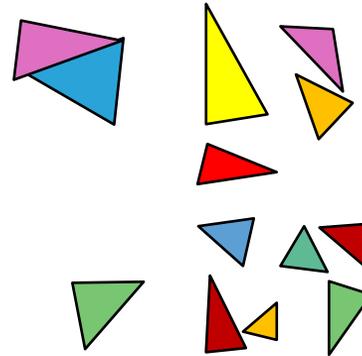
- Important feature: bounding volumes can ***overlap!***
- No duplicate references or split triangles necessary!
- Implicitly limits the amount of memory required



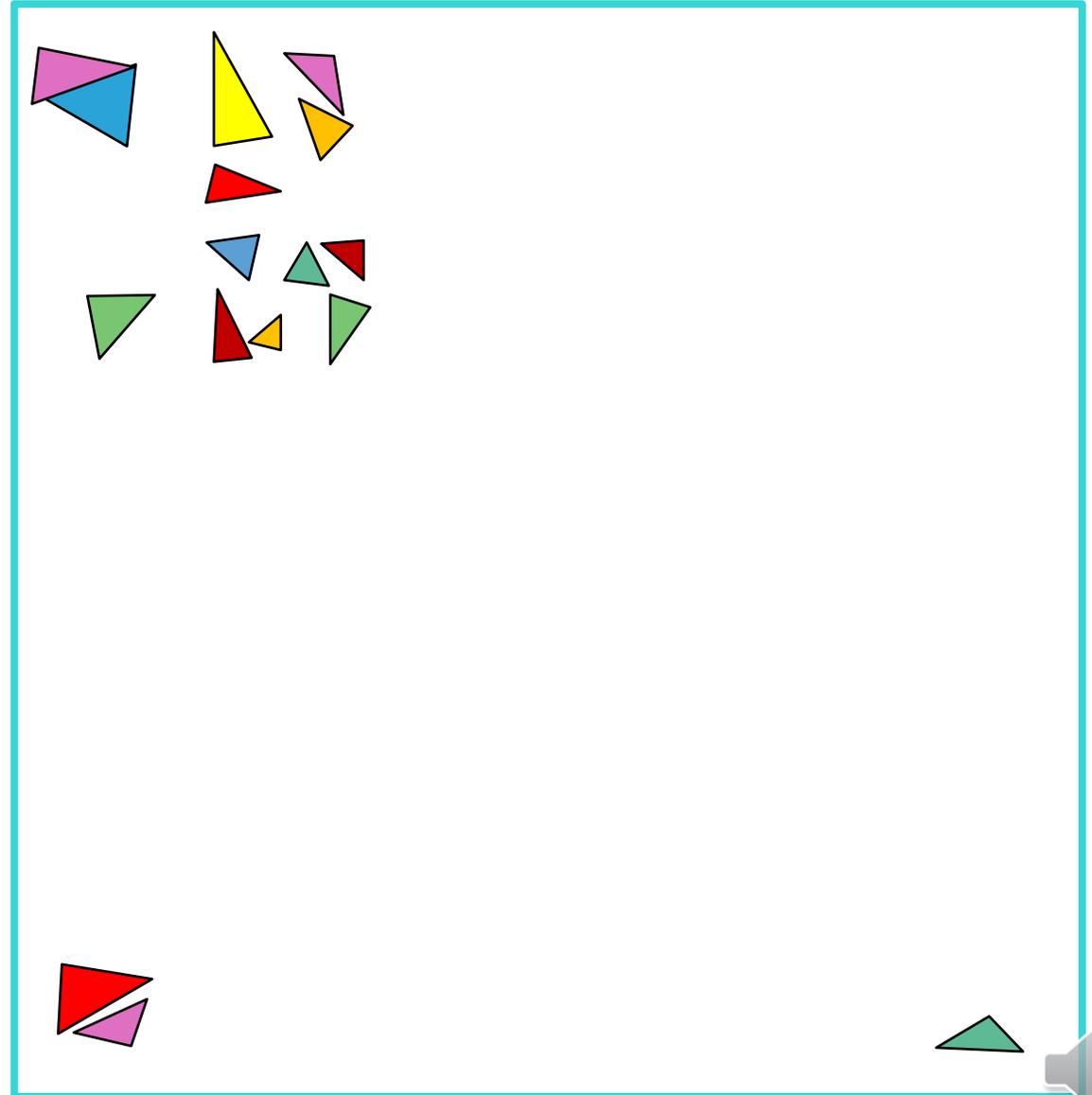
- Generating BVH and tree for input triangle geometry
- CPU: usually top-down
GPU: usually bottom-up
- From here on out, we will consider box BVHs only



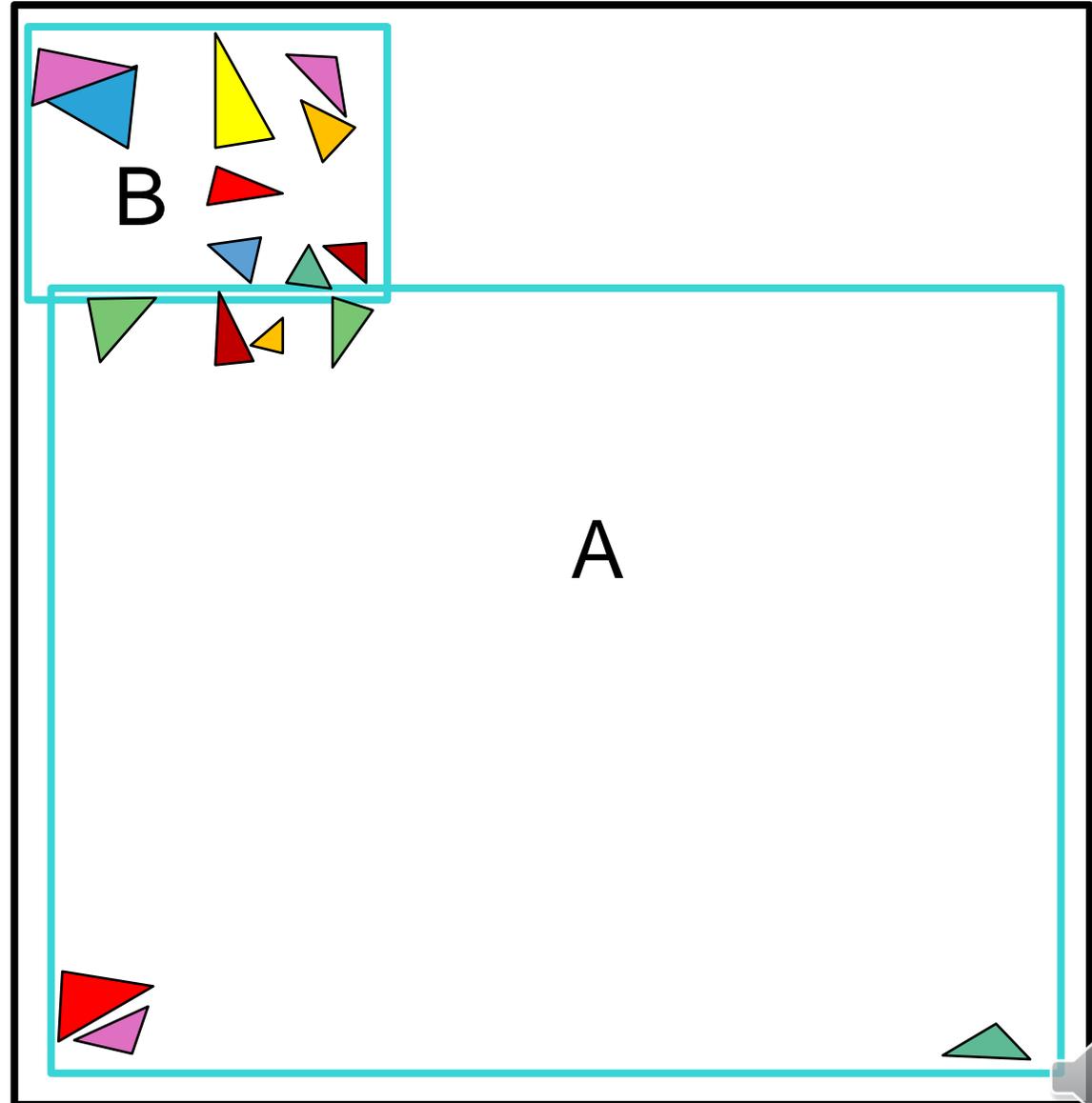
- Define N_{leaf} for leaves
- For each node, do the following:
 - Compute bounding box that fully encloses triangles & store
 - Holds $\leq N_{leaf}$ triangles? Stop.
 - Else, split into child groups
 - Make one new node per group
 - Set them as children of current
 - Repeat with child nodes



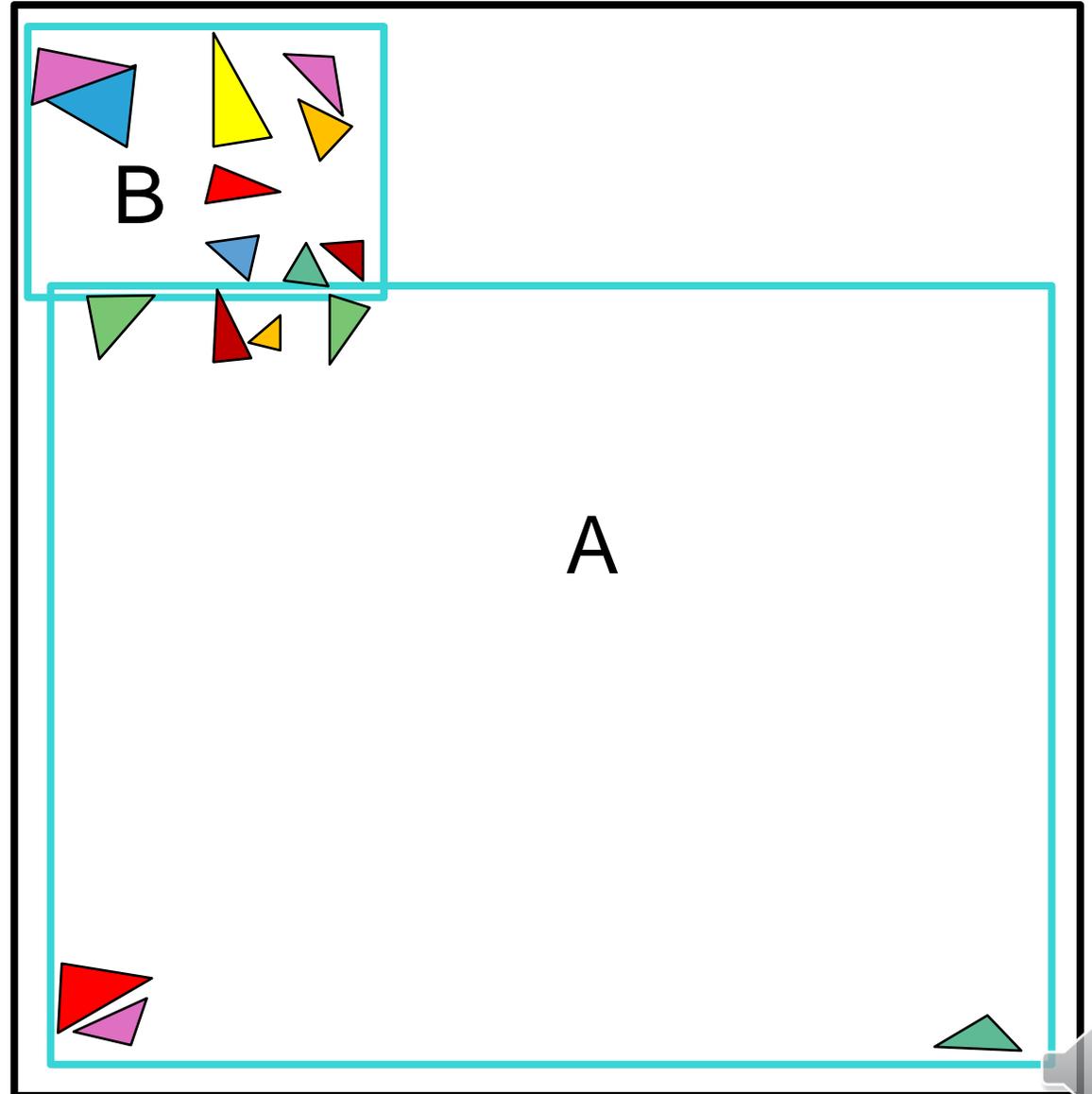
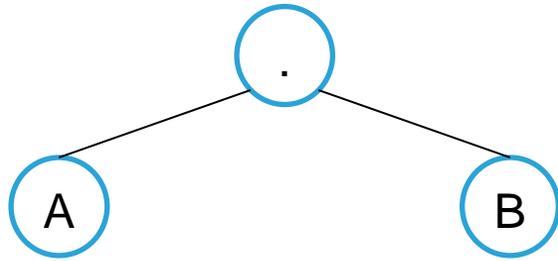
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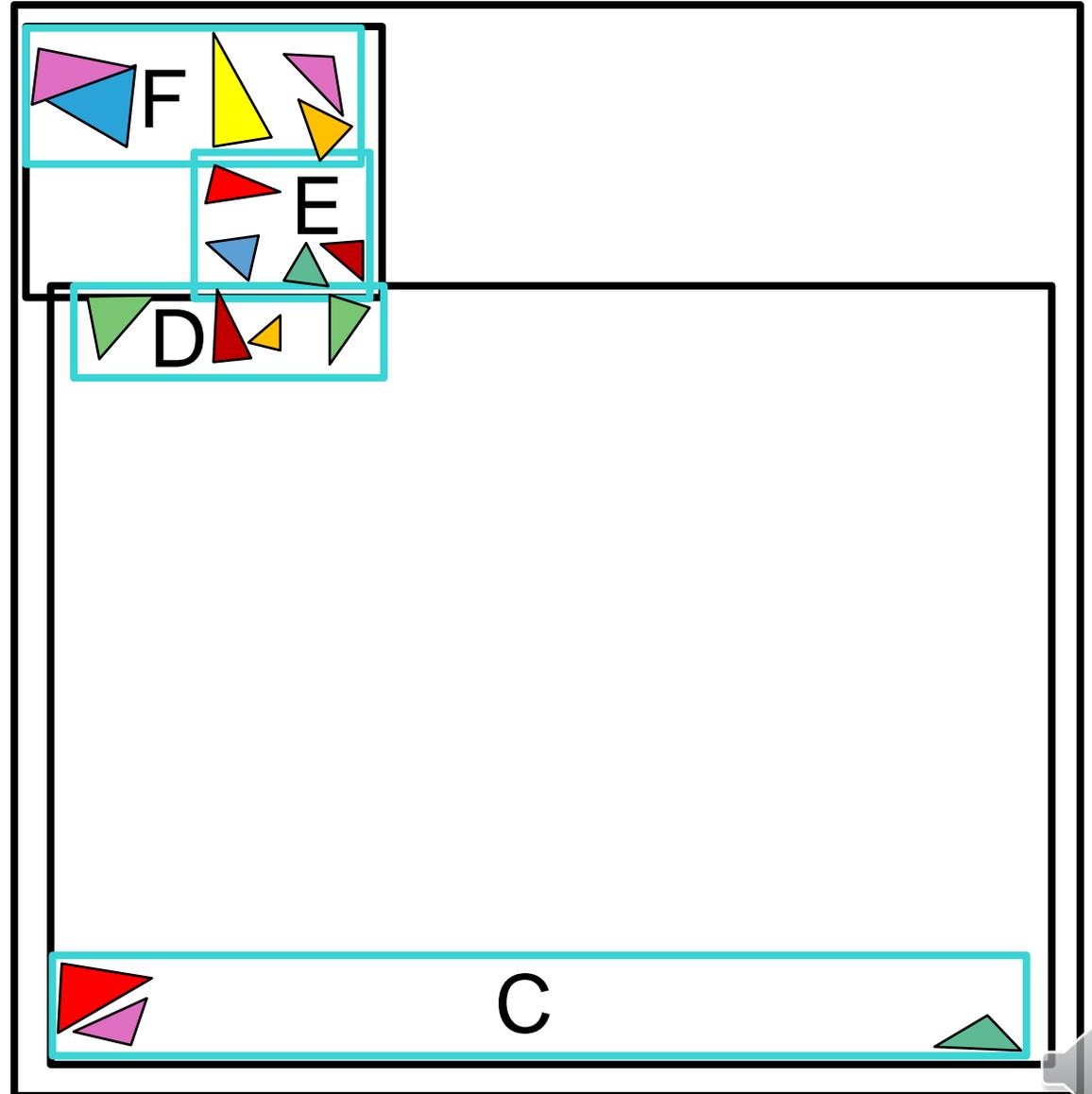
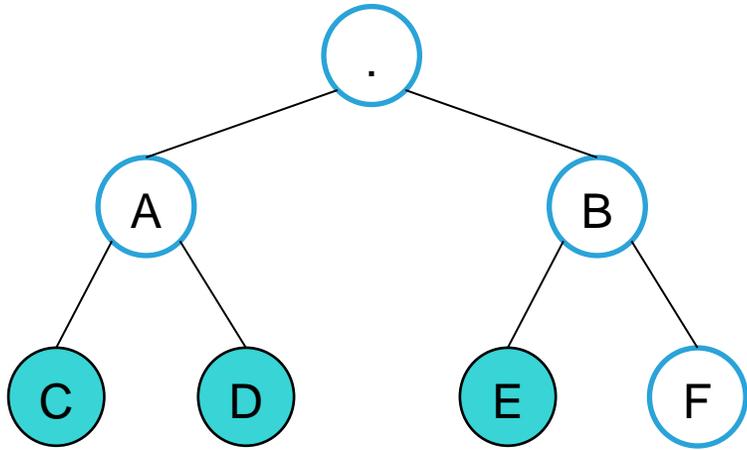
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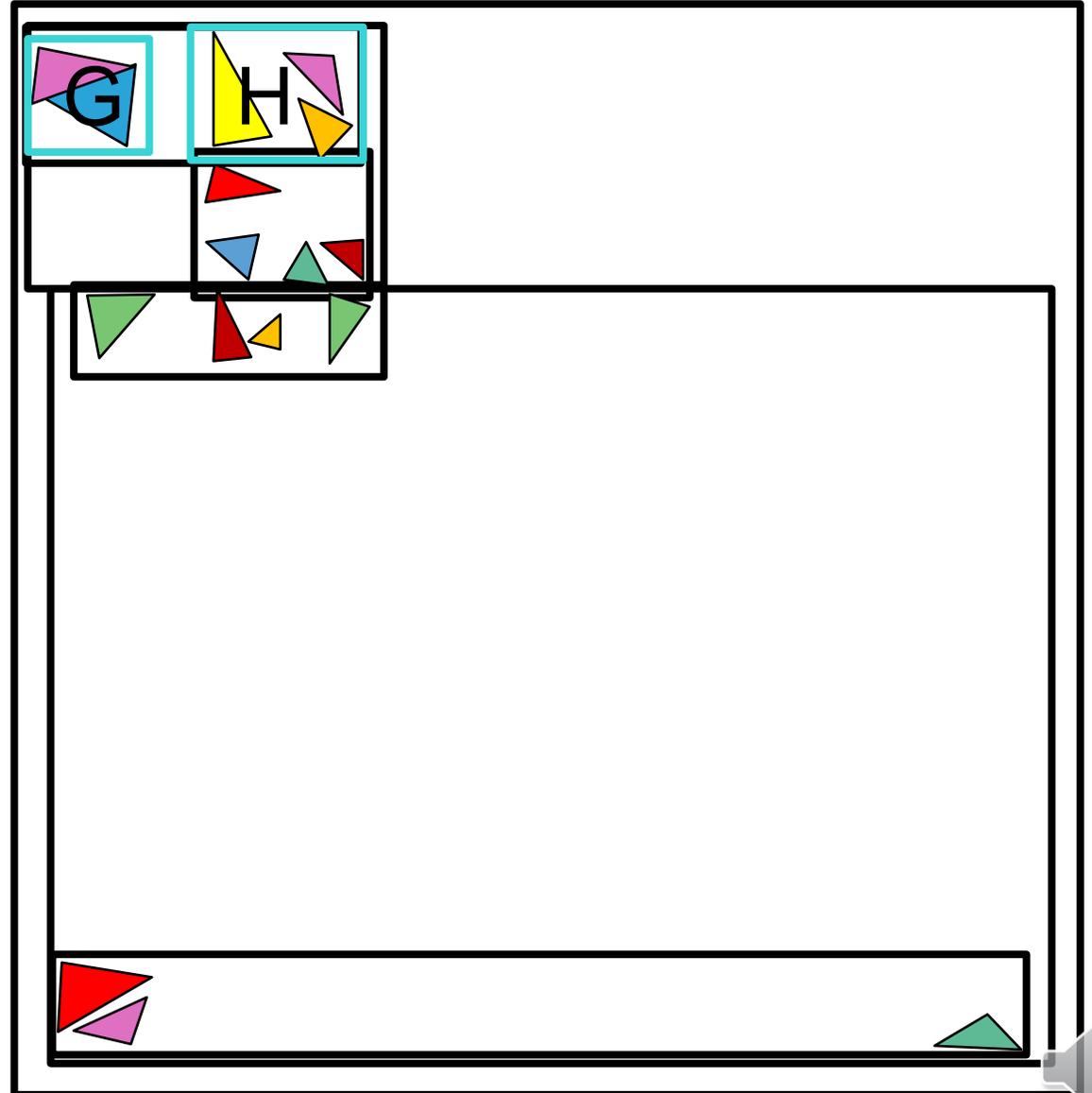
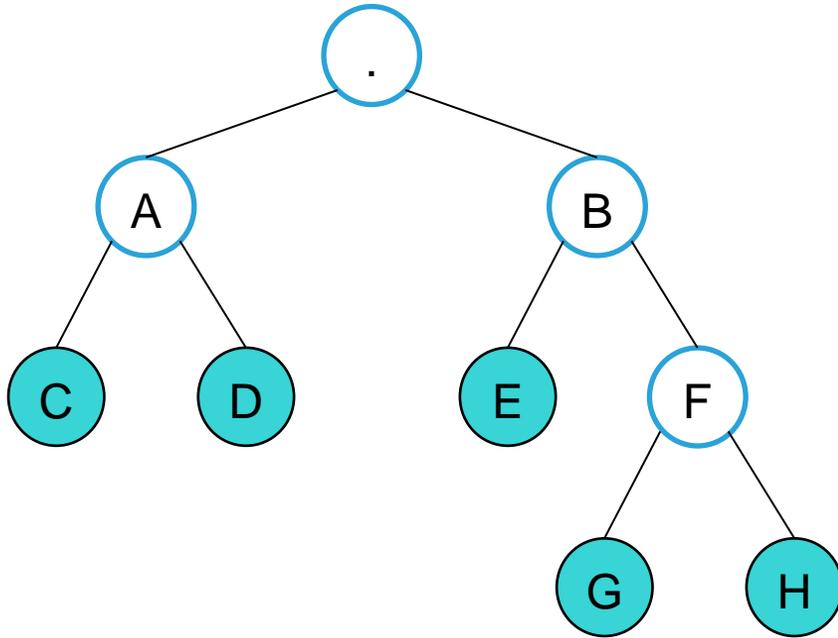
BVH Building, Top-Down, $N_{leaf} = 4$



BVH Building, Top-Down, $N_{leaf} = 4$



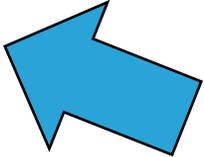
BVH Building, Top-Down, $N_{leaf} = 4$



- Which axes to consider for building bounding boxes/splitting?
 - Basis vectors $(1,0,0)$, $(0,1,0)$, $(0,0,1)$ only
 - Oriented basis vectors only
 - Arbitrary

- Where to split?
 - Spatial median
 - Object median
 - Something more elaborate...

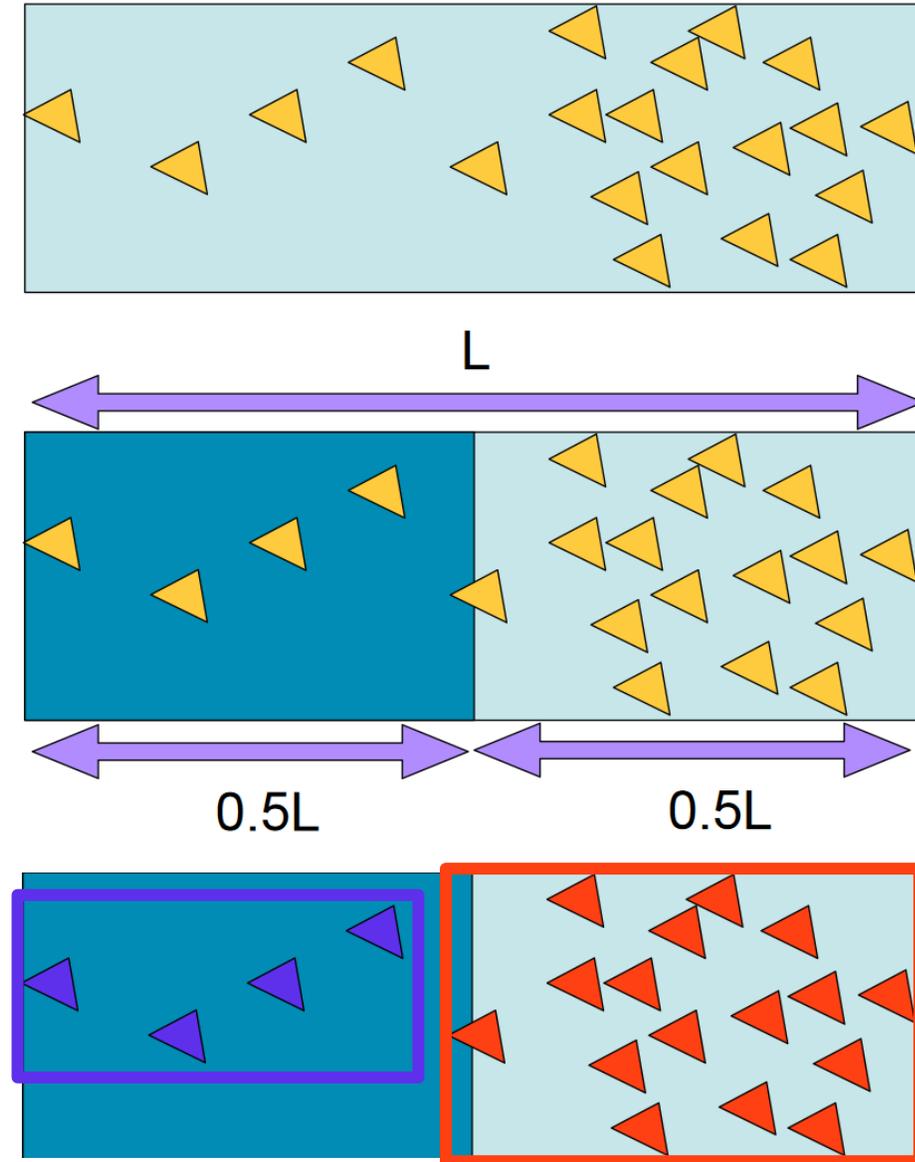


- Which axes to consider for building bounding boxes/splitting?
 - Basis vectors $(1,0,0)$, $(0,1,0)$, $(0,0,1)$ only
 - Oriented basis vectors only
 - **Arbitrary**  Algorithms exist (e.g. “separating axis theorem”), but usually very slow!
- Where to split?
 - Spatial median
 - Object median
 - Something more elaborate...

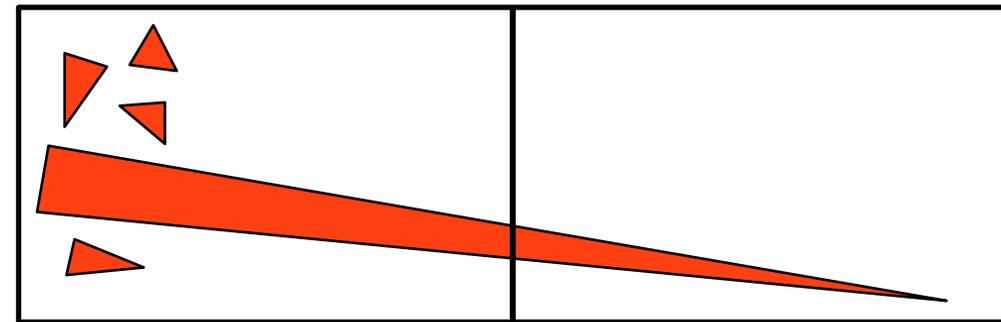
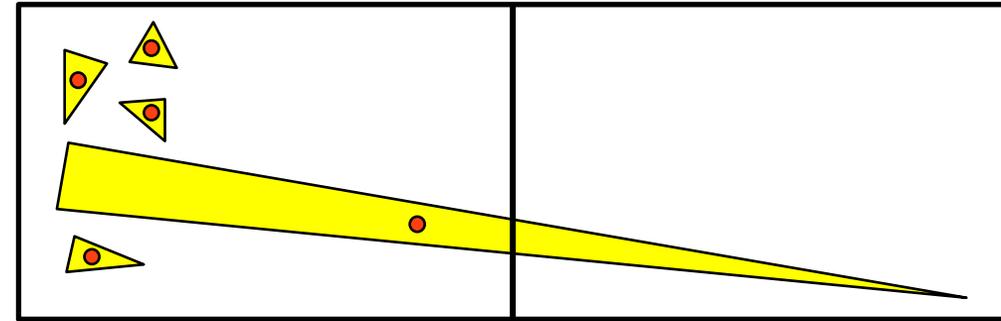
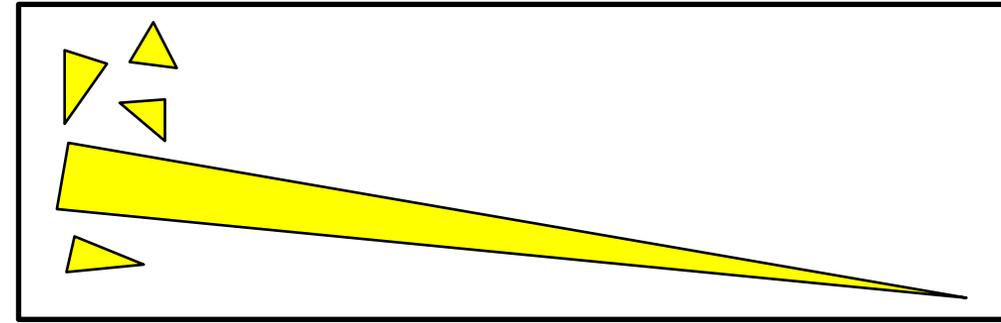


Splitting at spatial median

- Pick the longest axis (X/Y/Z) of current node bounds
- Find the midpoint on that axis
- Assign triangles to A/B based on which side of the midpoint each triangle's *centroid* lies on
- Continue recursion with A/B

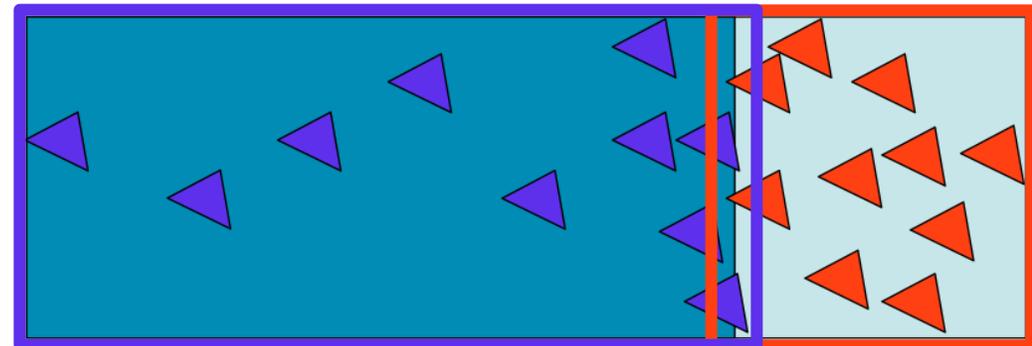
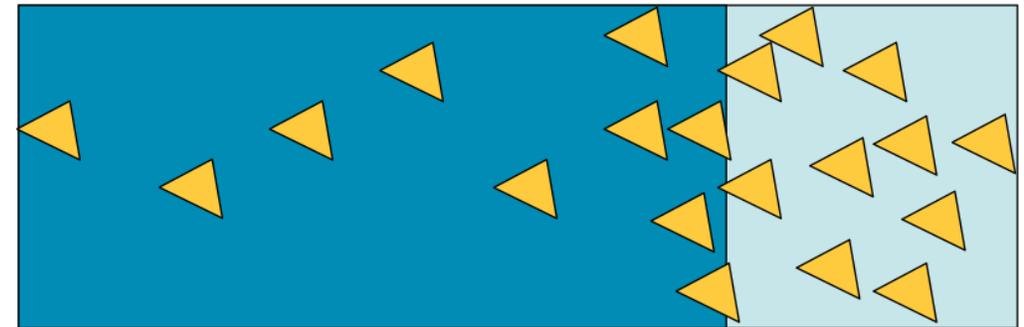
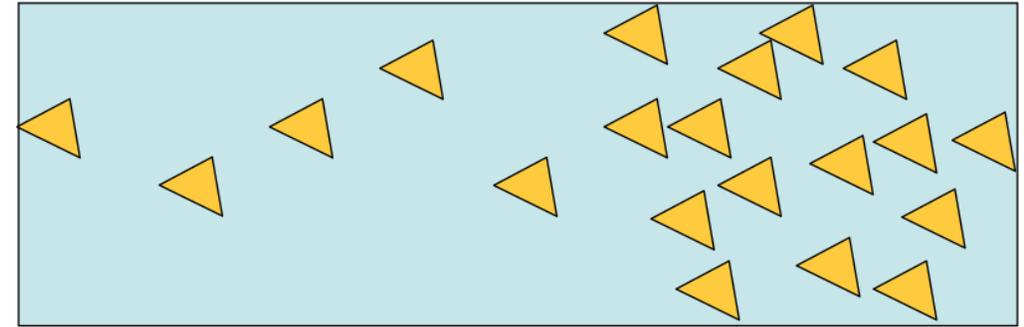


- Careful: can result in infinite recursion!
- All triangles are assigned again to **one node**, none in **the other**
- Can guard against it in several ways
 - Limit max. number of split attempts
 - Try other axes if one node is empty
 - Compute box over triangle centroids and split that on longest axis instead



Splitting at object median

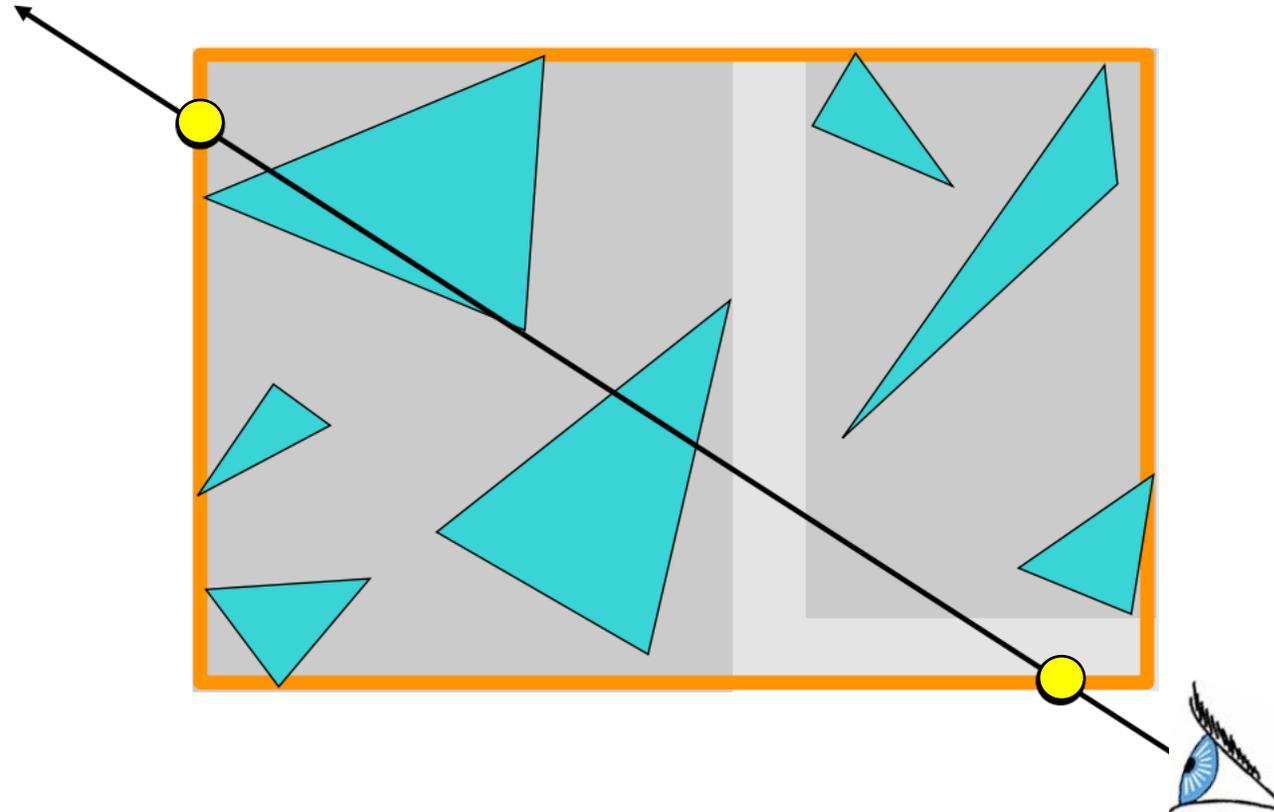
- Pick an axis. Can try them all, don't pick the same every time
- Sort triangles according to their centroid's position on that axis
- Assign first half of the sorted triangles to **A**, the second to **B**
- Continue recursion with **A/B**



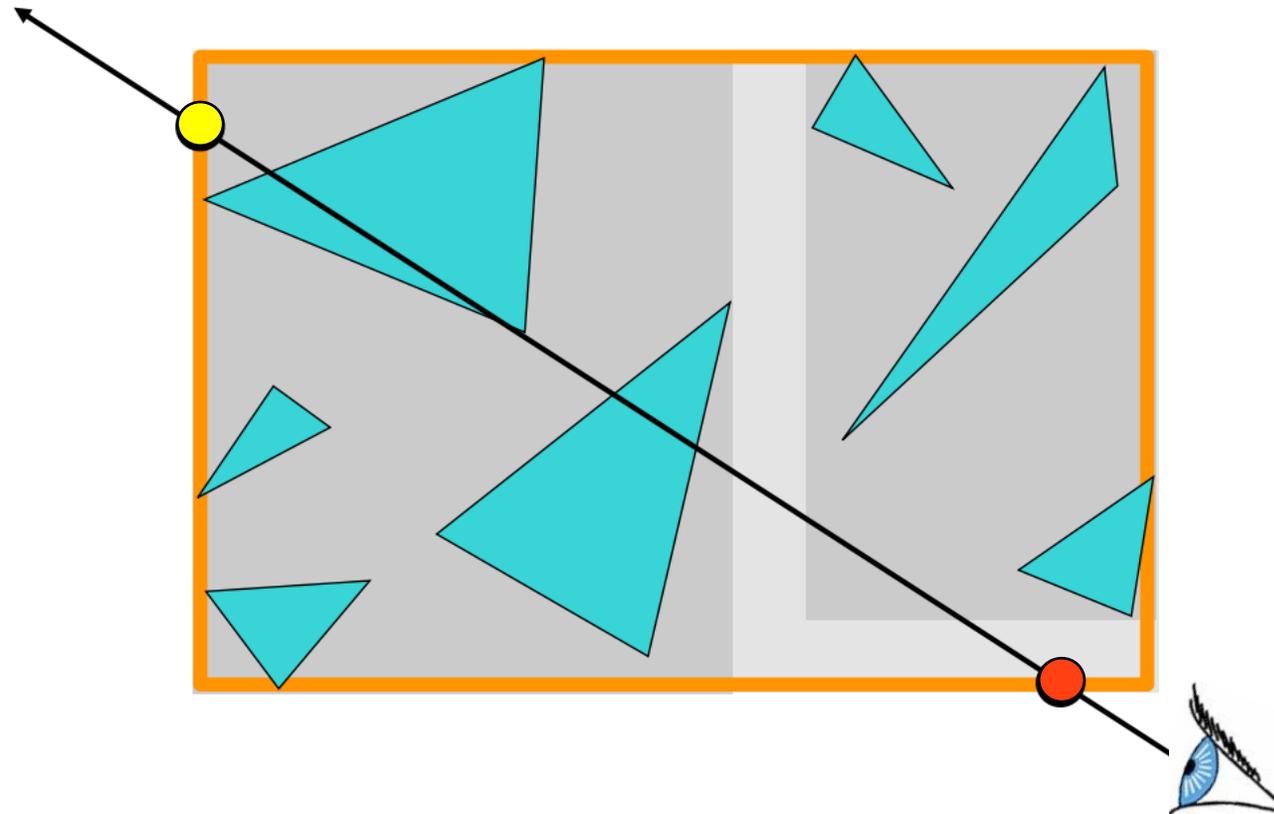
0. Set $t_{min} = \infty$. Start at root node, return if it doesn't intersect ray.
1. Process node if its closest intersection with ray is closer than t_{min}
2. If it's an inner node, run from 1. for child nodes that intersect ray
 - Process the closest node first
 - Keep others on stack to process further ones later (recursion works)
3. If it's a leaf, check triangles and update t_{min} in case of closer hit



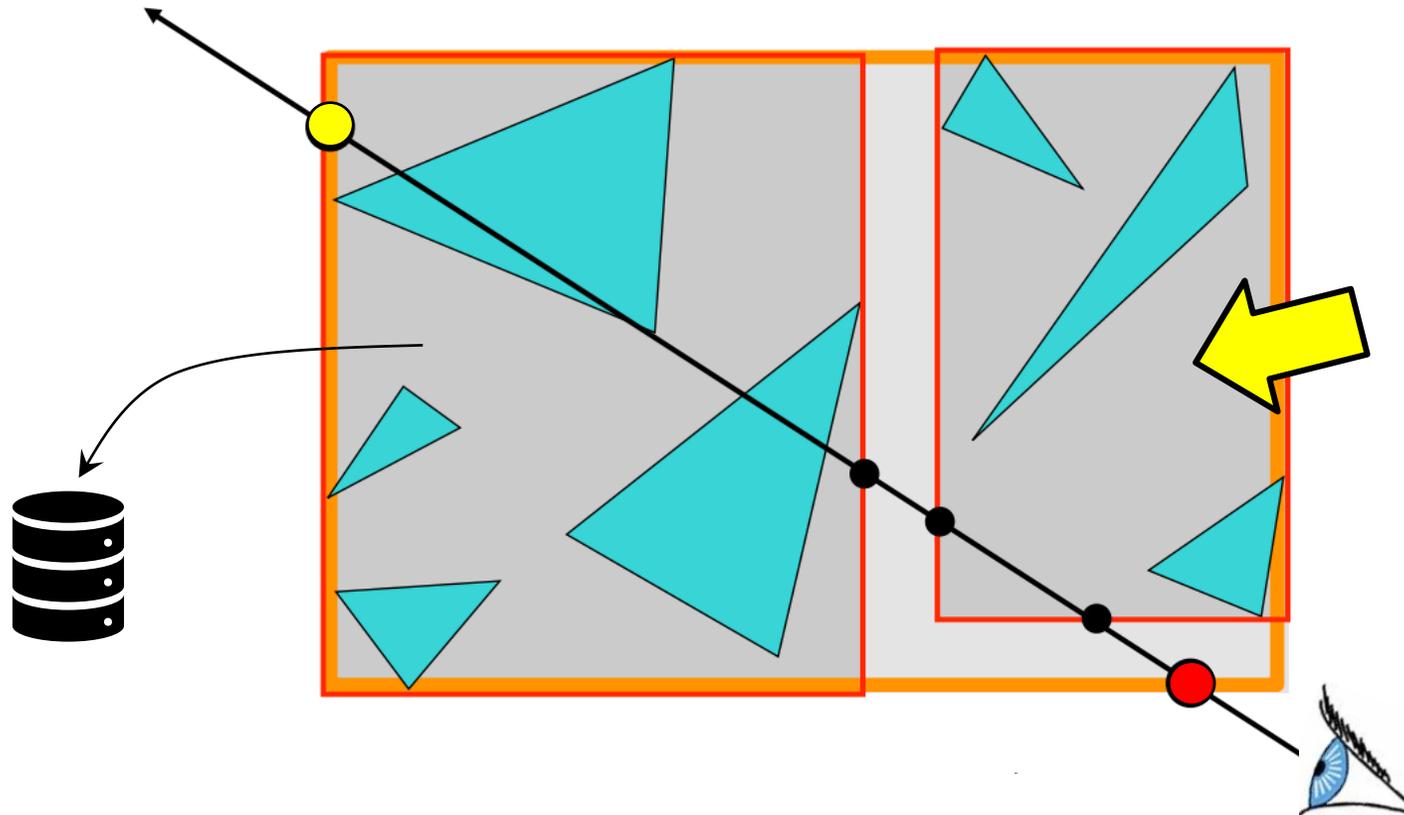
1. Process node if its closest intersection with ray is closer than t_{min}



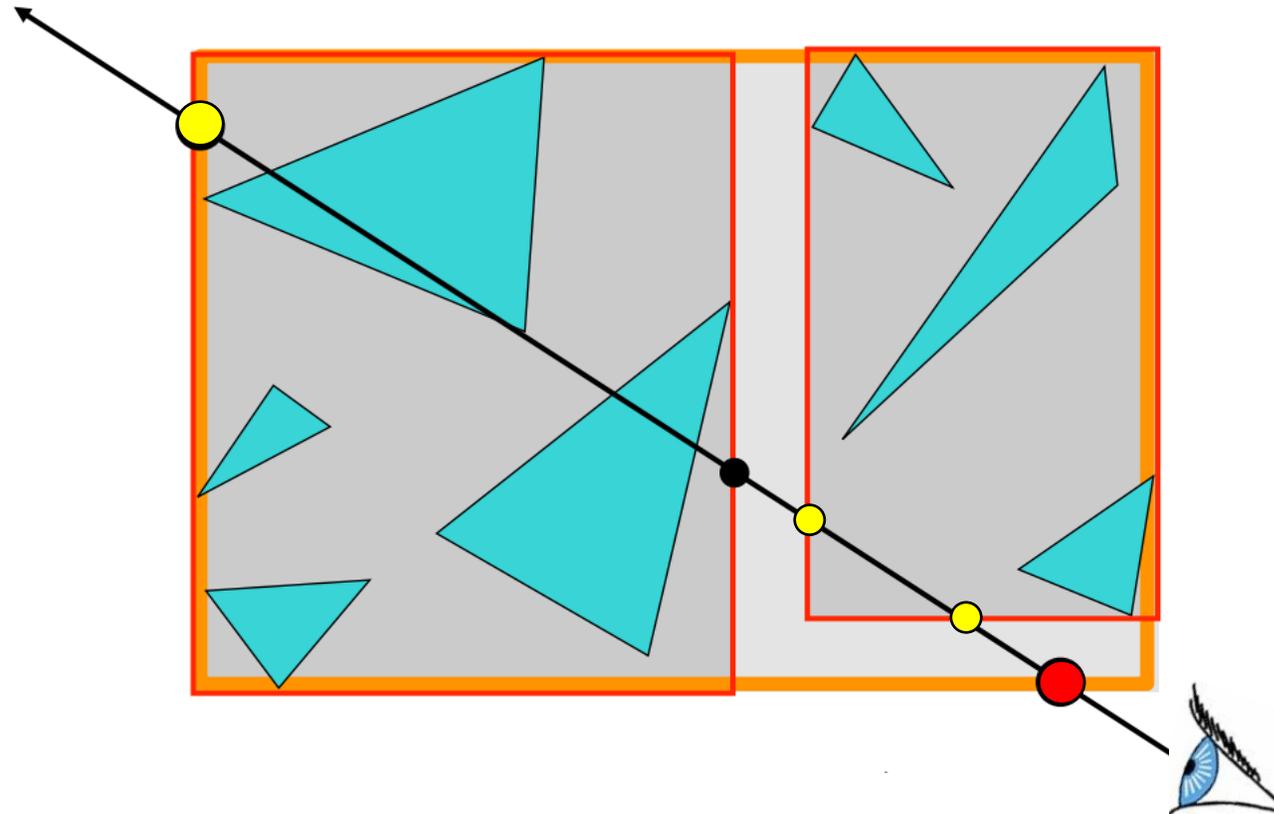
1. Process node if its closest intersection with ray is closer than t_{min}



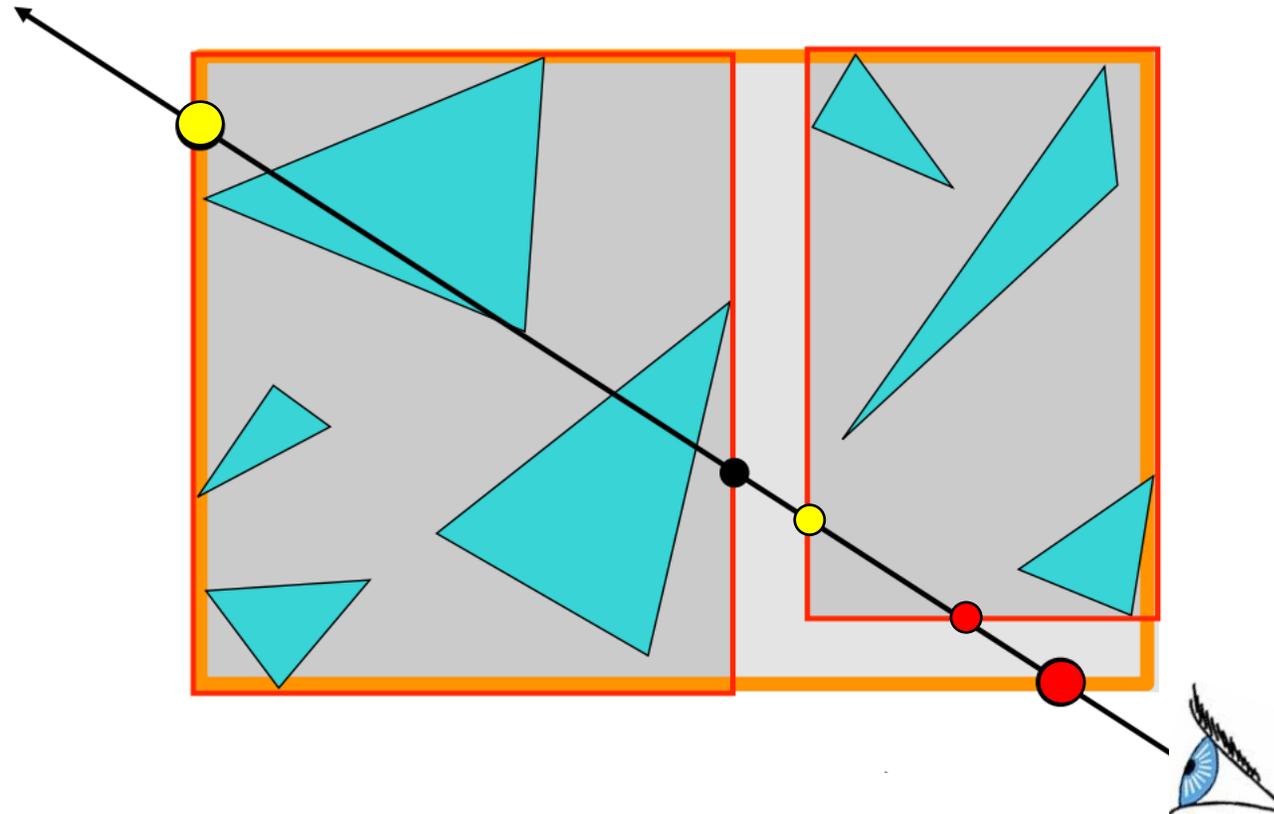
2. If it's an inner node, run from 1. for child nodes that intersect ray
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 - Keep others on stack to process further ones later



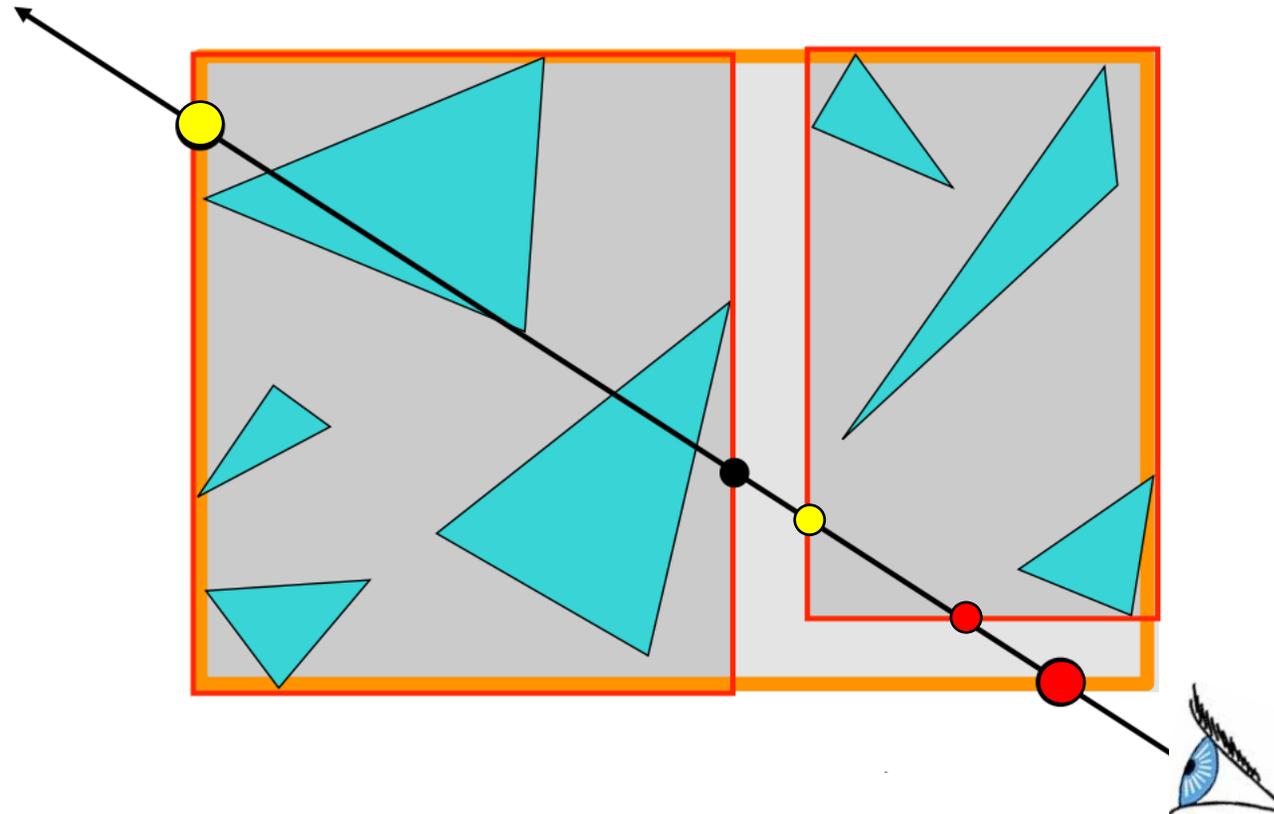
1. Process node if its closest intersection with ray is closer than t_{min}



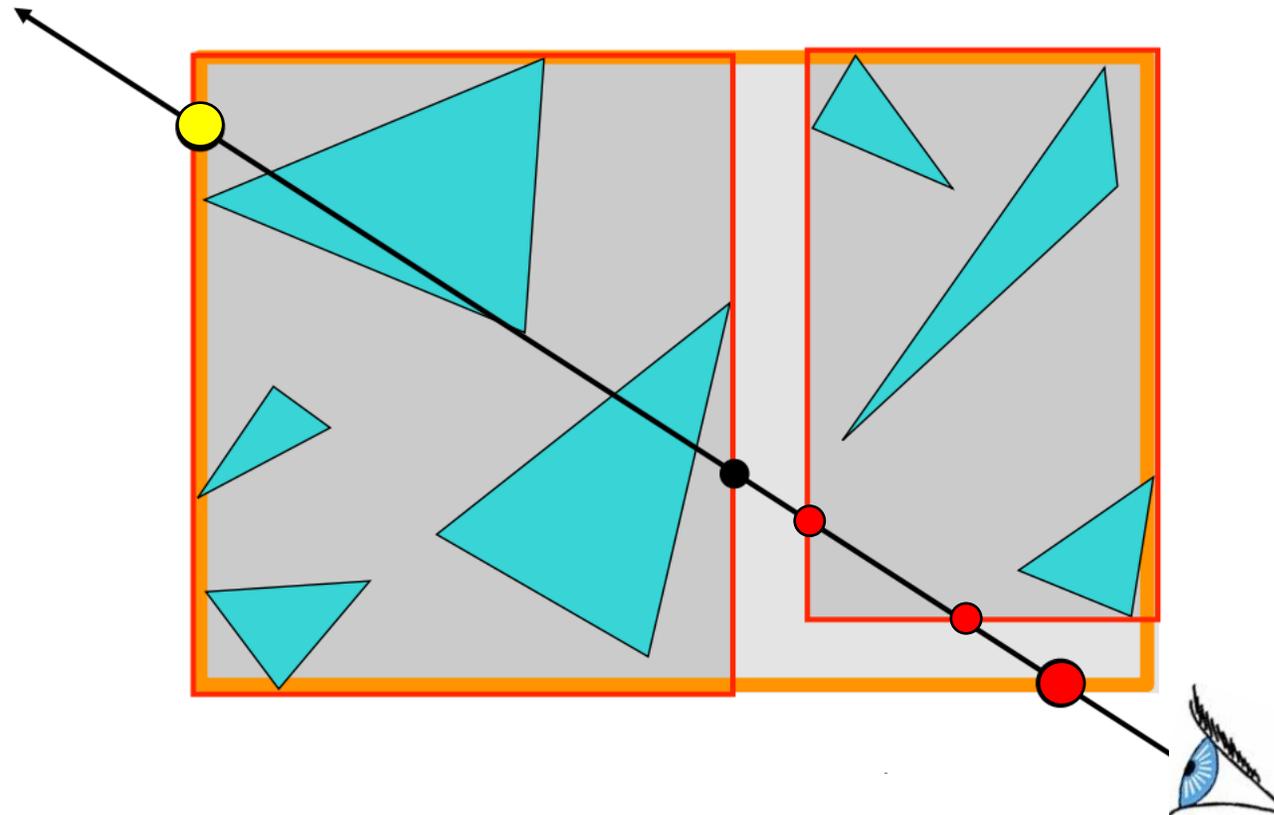
1. Process node if its closest intersection with ray is closer than t_{min}



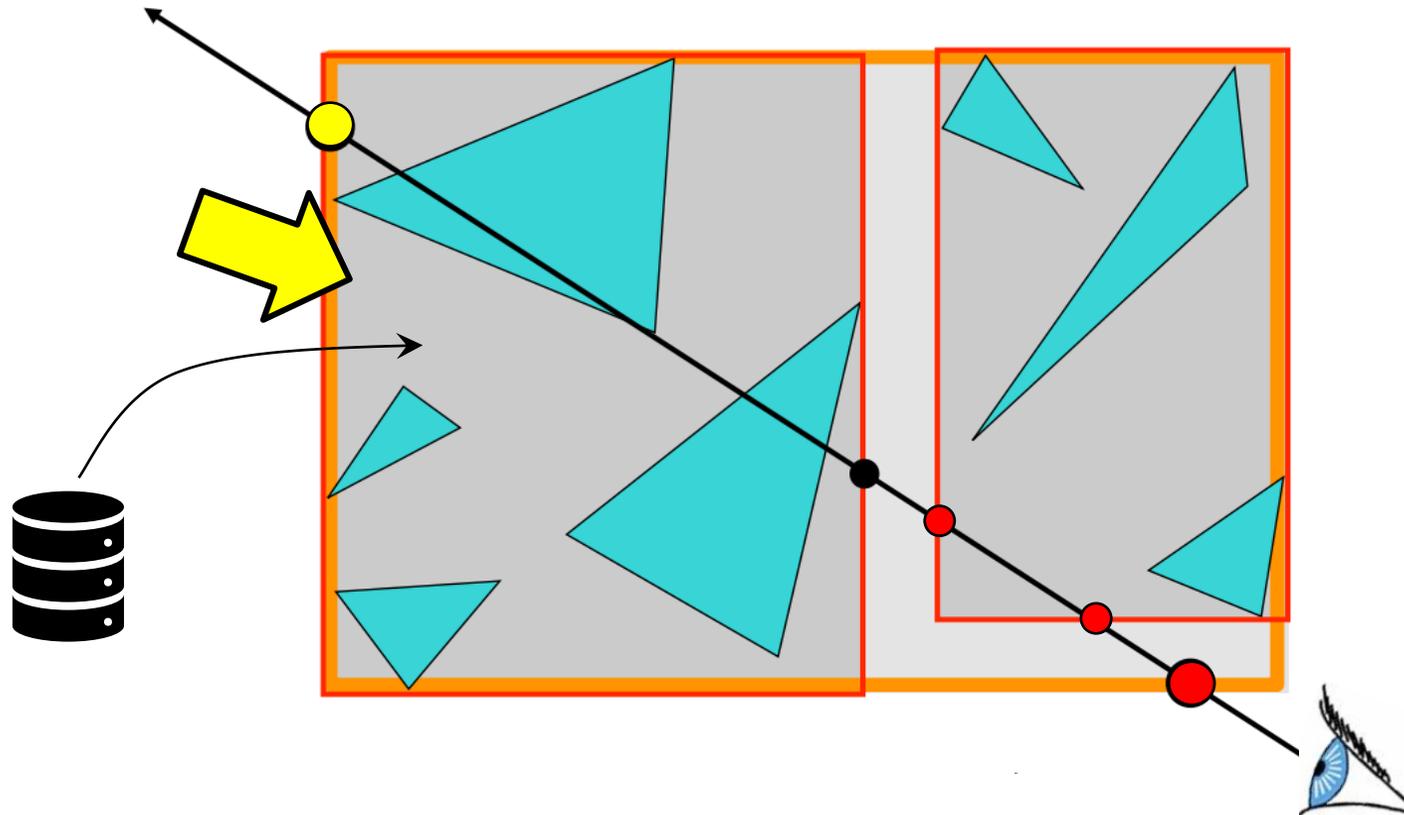
3. If it's a leaf, check triangles and update t_{min} in case of closer hit



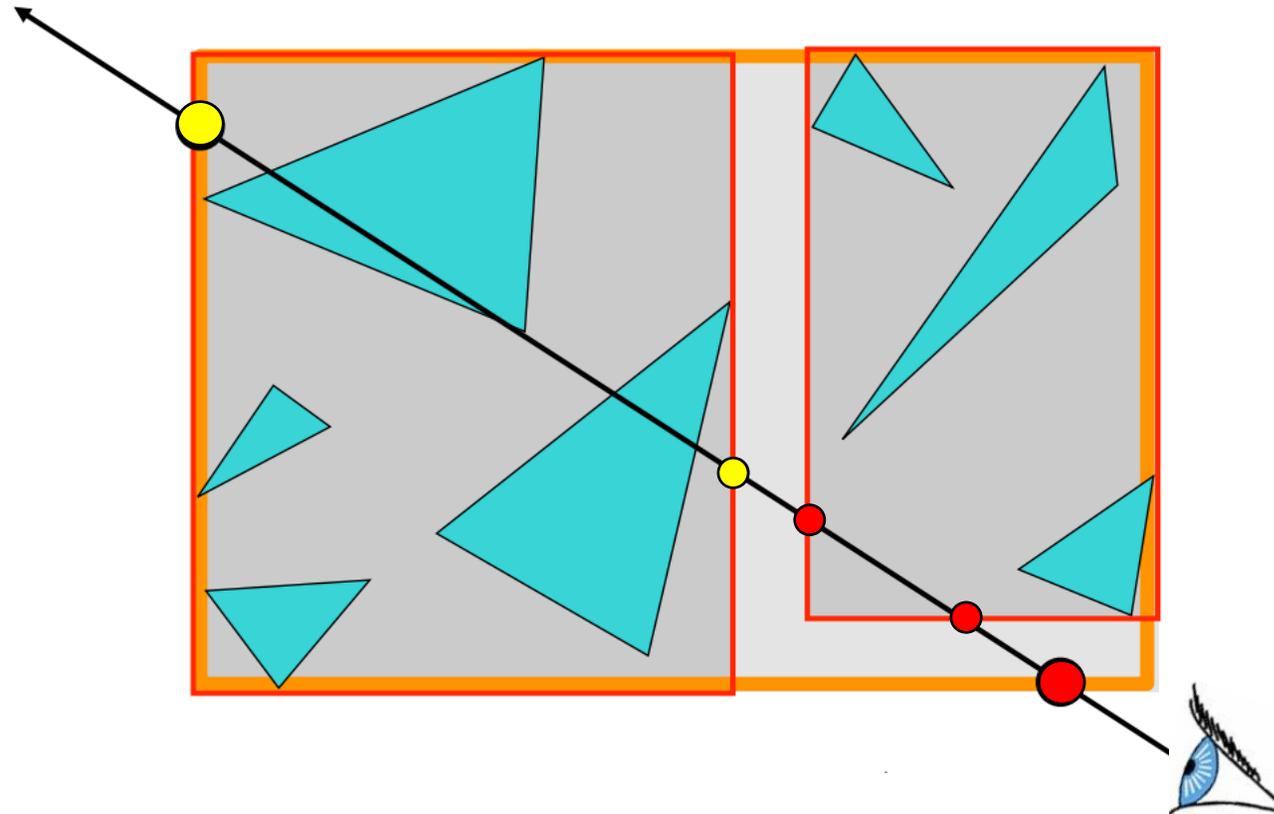
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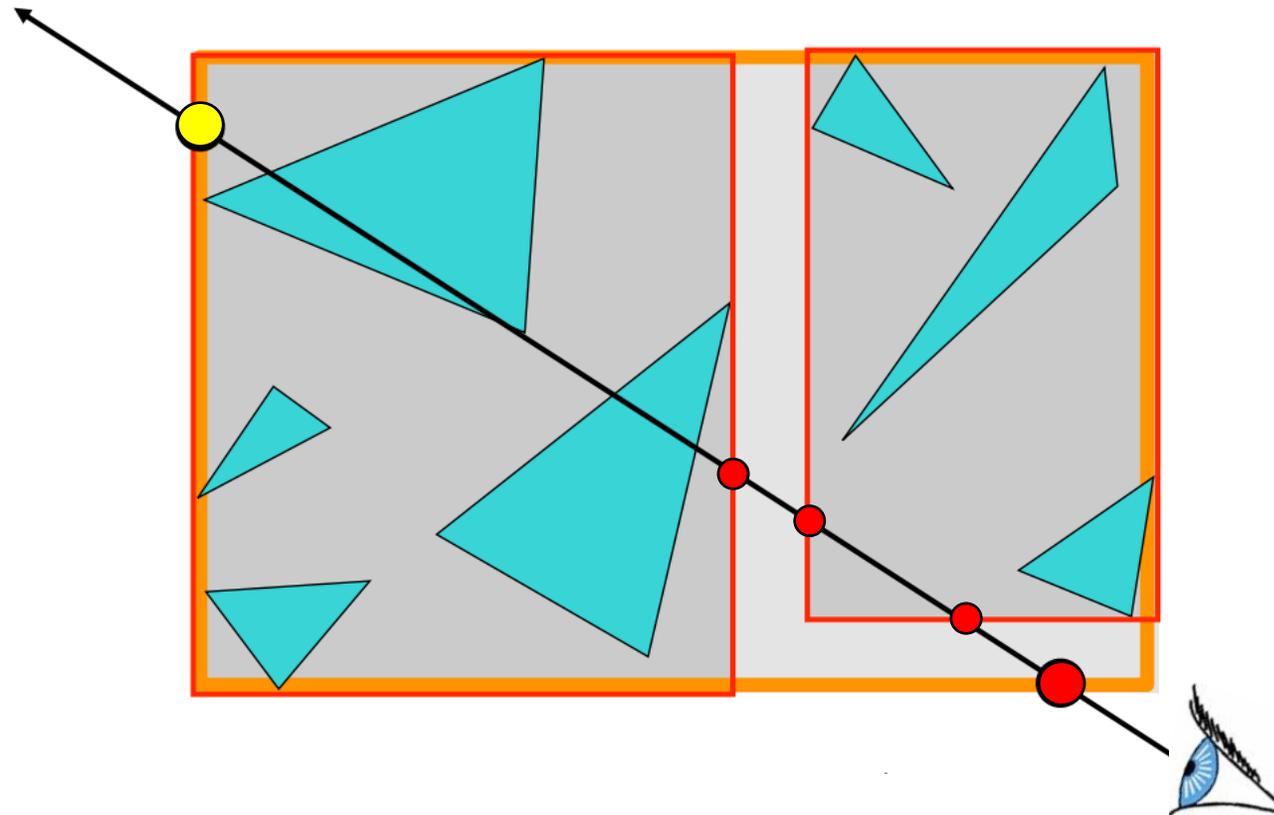
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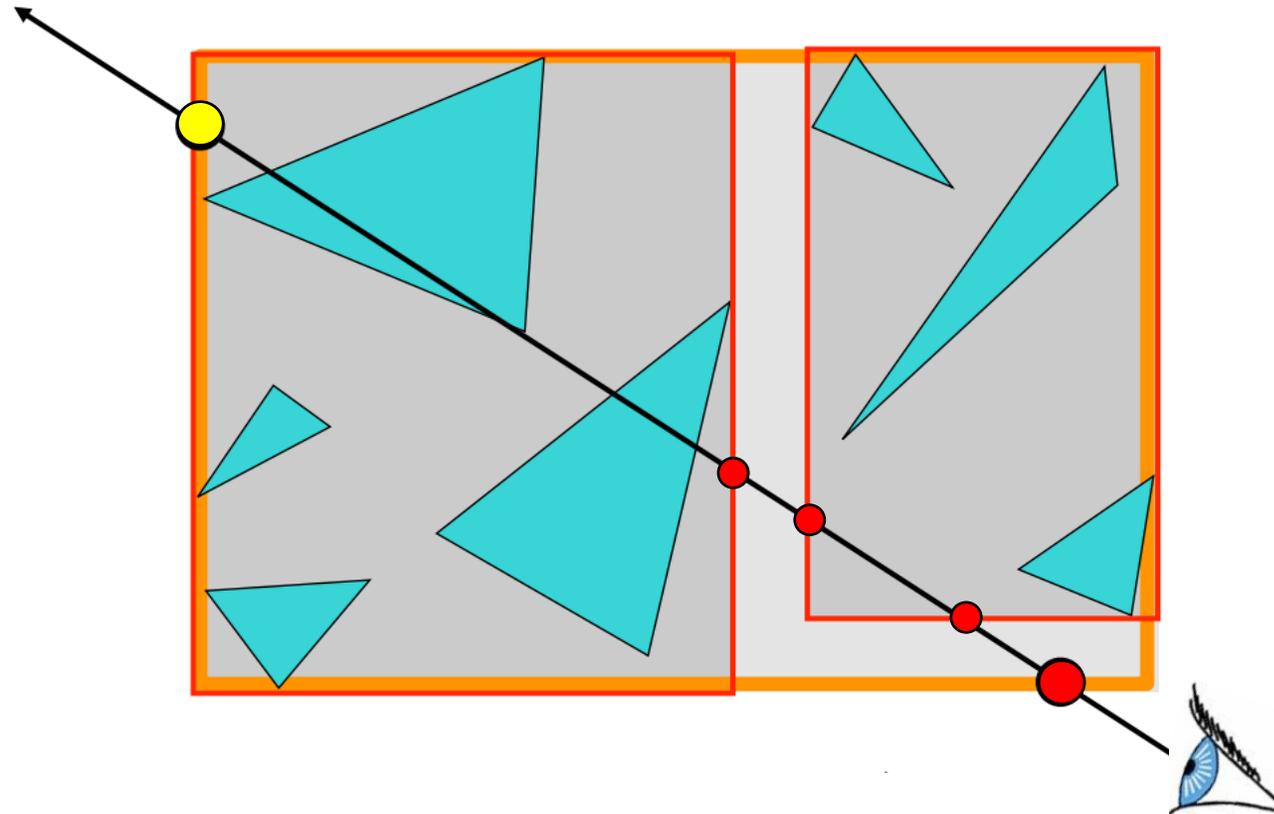
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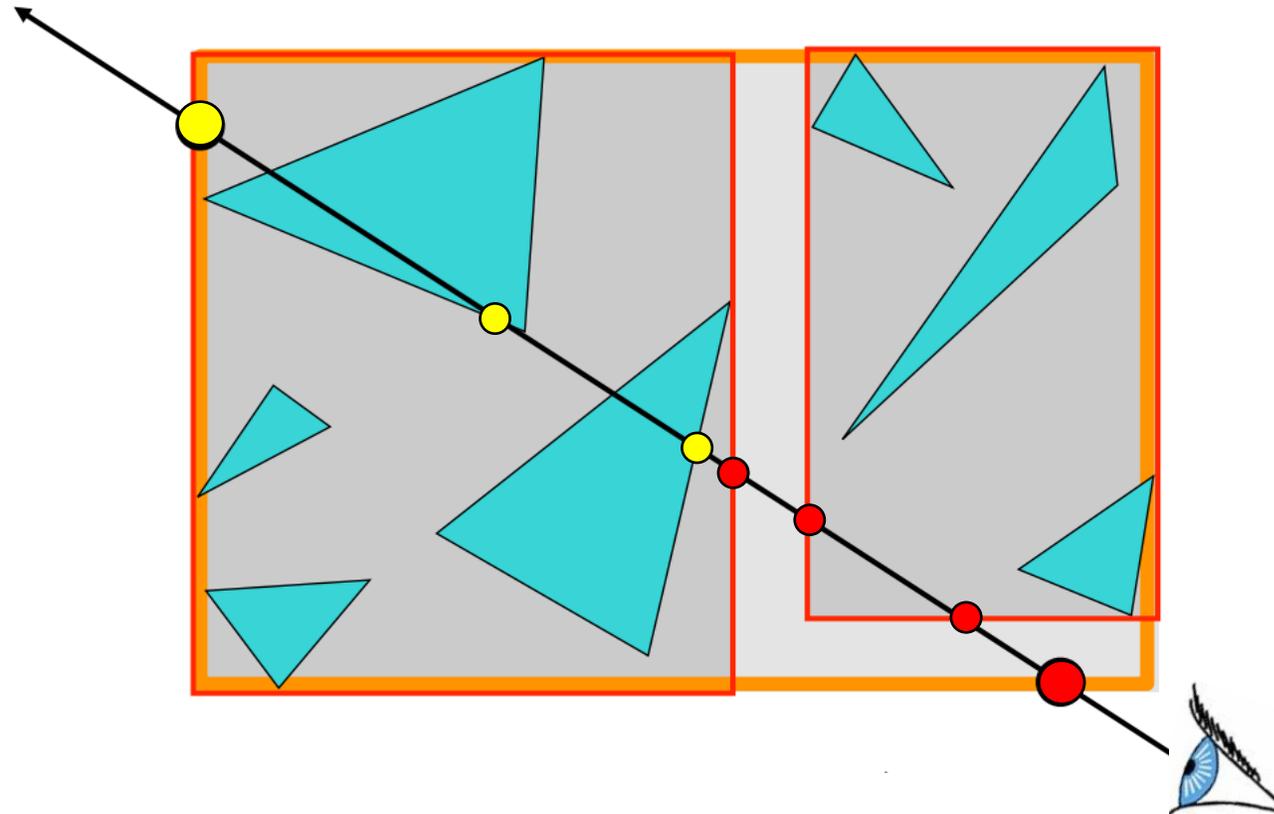
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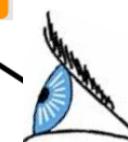
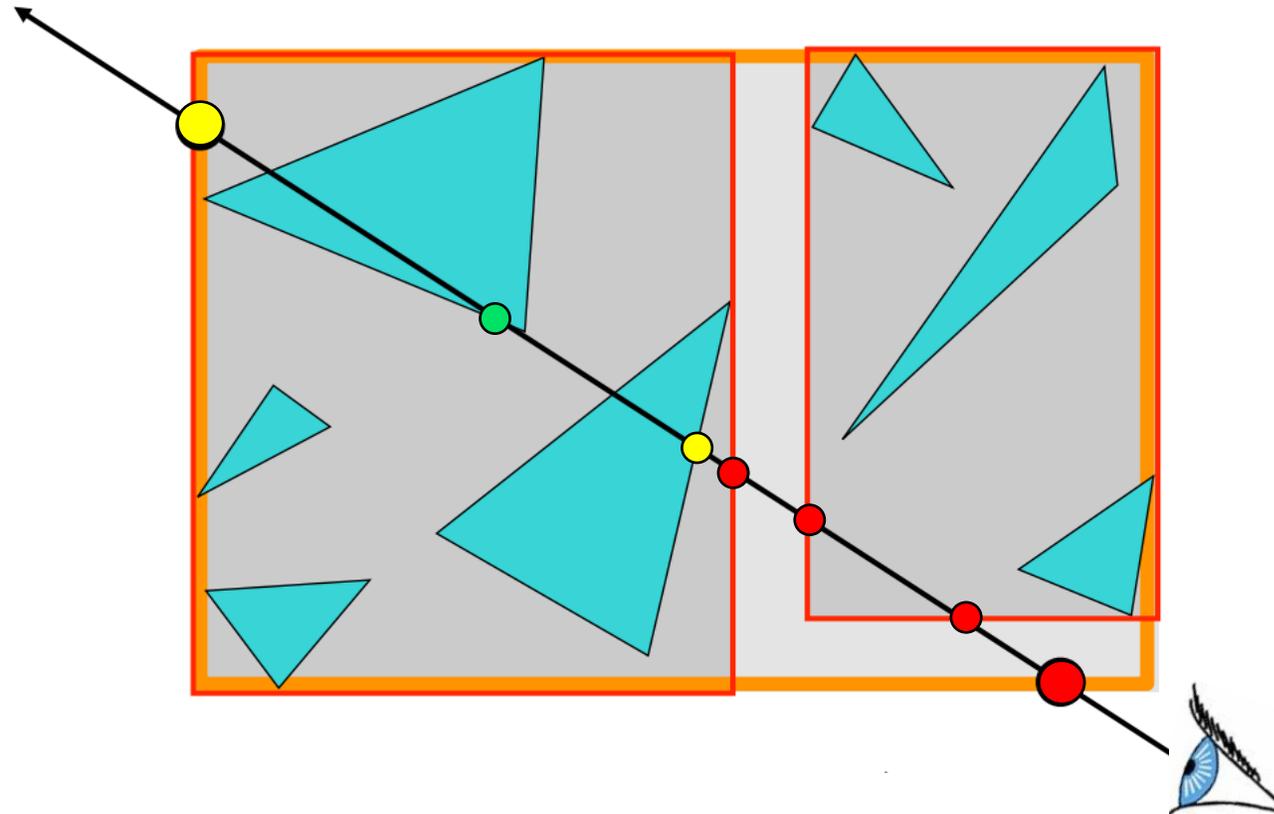
3. If it's a leaf, check triangles and update t_{min} in case of closer hit (●)



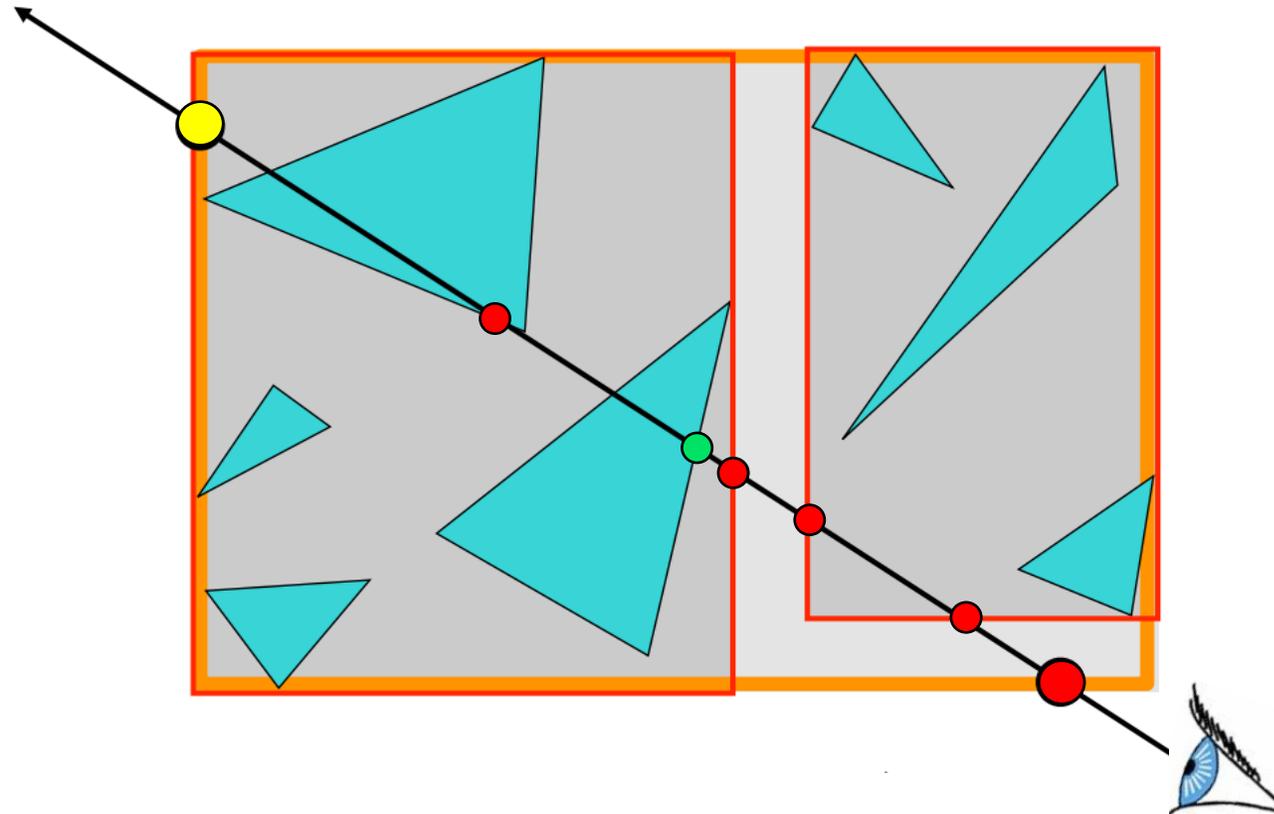
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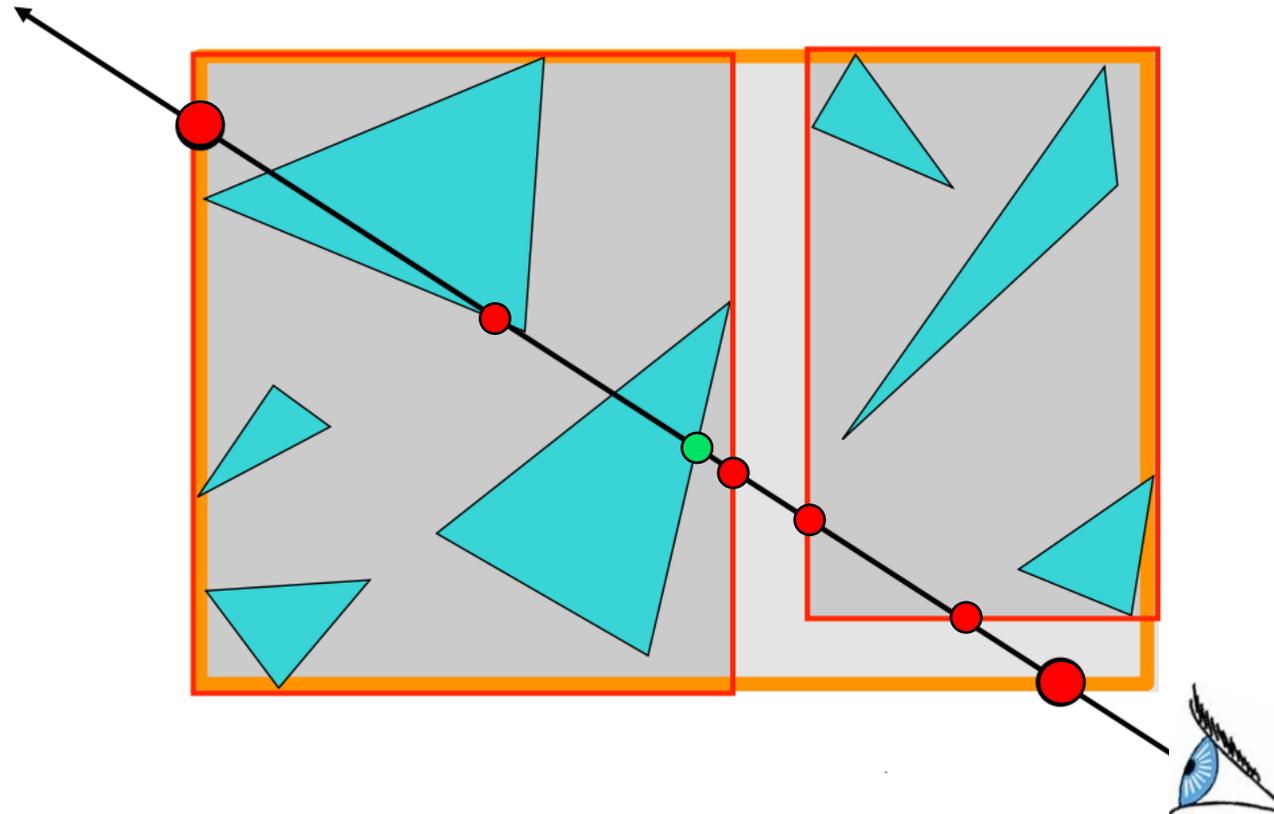
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3. If it's a leaf, check triangles and update t_{min} in case of closer hit (●)



3. If it's a leaf, check triangles and update t_{min} in case of closer hit (●)



- Simple, but powerful heuristic for choosing splits
- Created with traversal in mind, based on the following ideas:
 - Assume rays are uniformly distributed in space
 - Probability of a ray hitting a node is proportional to its **surface area**
 - Cost of traversing it depends on the **number of triangles** in its leaves
 - Hence, **avoid large nodes with many triangles**, because:
 - They have a tendency to get checked often
 - Getting a definite result (reject or closest hit) is likely to be expensive



Goal: To split a node, find the hyperplane b that minimizes

$$f(b) = LSA(b) \cdot L(b) + RSA(b) \cdot (N - L(b)), \text{ where}$$

- $LSA(b)/RSA(b)$ are the **surface area** of the nodes that enclose the triangles whose centroid is on the “left”/“right” of the split plane b
- $L(b)$ is the **number of primitives on the “left”** of b
- N is the **total number of primitives** in the node



- We want to constrain the search space for a good split
- Pick a set of axes to test (e.g., 3D basis vectors X/Y/Z)
- When splitting a node with N triangles, for each axis
 - Sort all triangles by their centroid's position on that axis
 - Find the index i that minimizes

$$f(i) = LSA(i) \cdot i + RSA(i) \cdot (N - i), \text{ where}$$

- $LSA(i)$ is the surface area of the AABB over sorted triangles $[0, i)$
 - $RSA(i)$ is the surface area of the AABB over sorted triangles $[i, N)$
- Select the axis and index i with the best $f(i)$ for the split overall!



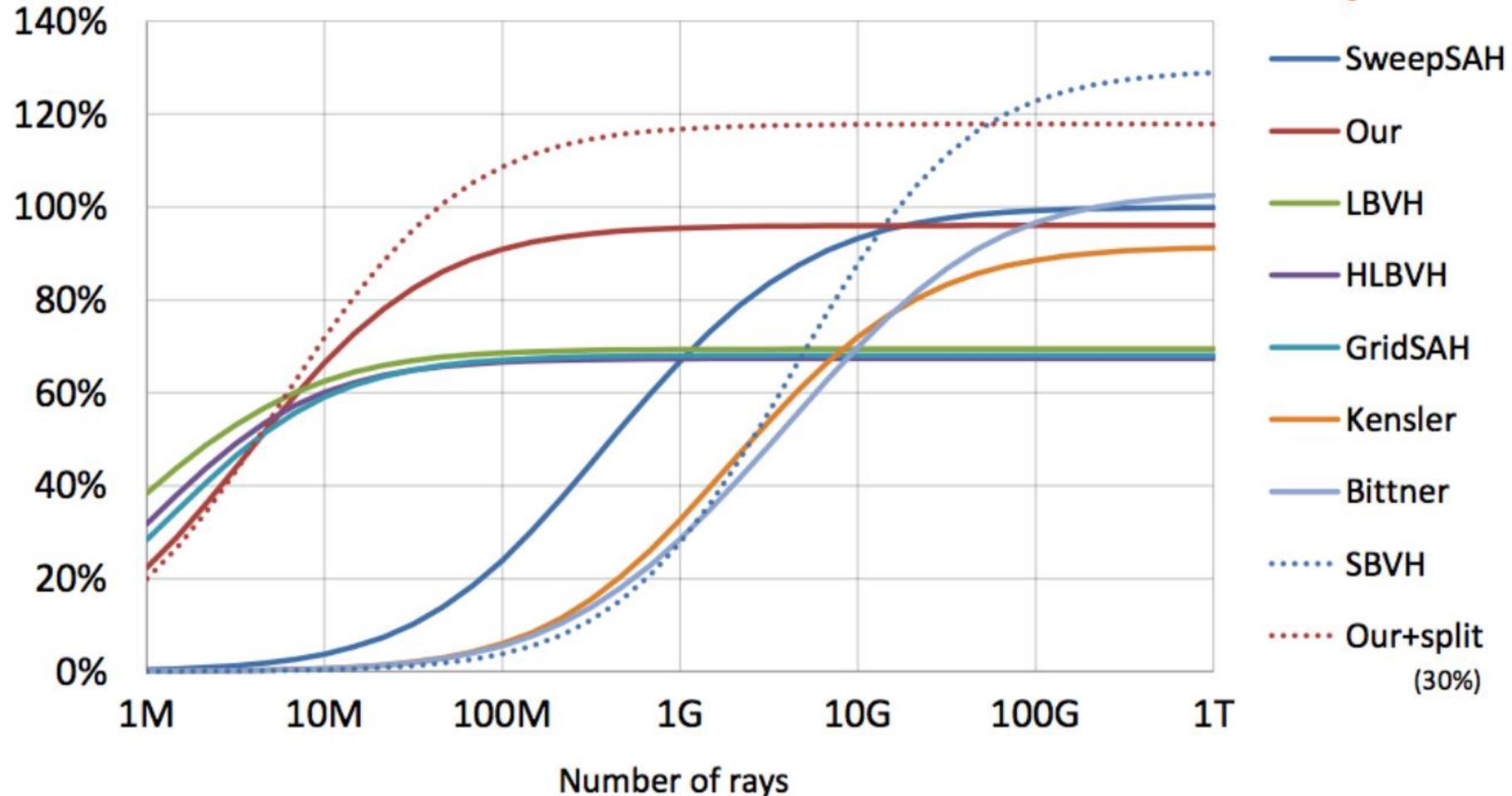
- Important trade-off: building time vs. traversal time
 - Given the same tracing/traversal code, the quality of a BVH tree may have a big impact on performance!
 - Can be as high as 2x compared to naïve splitting
- Benefits depend on the parameters of your rendering scenario
 - How big is your scene and how are triangles distributed?
 - How long will your BVH be valid?
 - What are the quality requirements for your images?



Evaluation of Combined Building + Traversal [2]

MRays/s relative to maximum achievable ray tracing performance of SweepSAH

Efficiency measured as a function of TOTAL WALLCLOCK TIME PER RAY, taking into account both BVH construction and actual tracing.

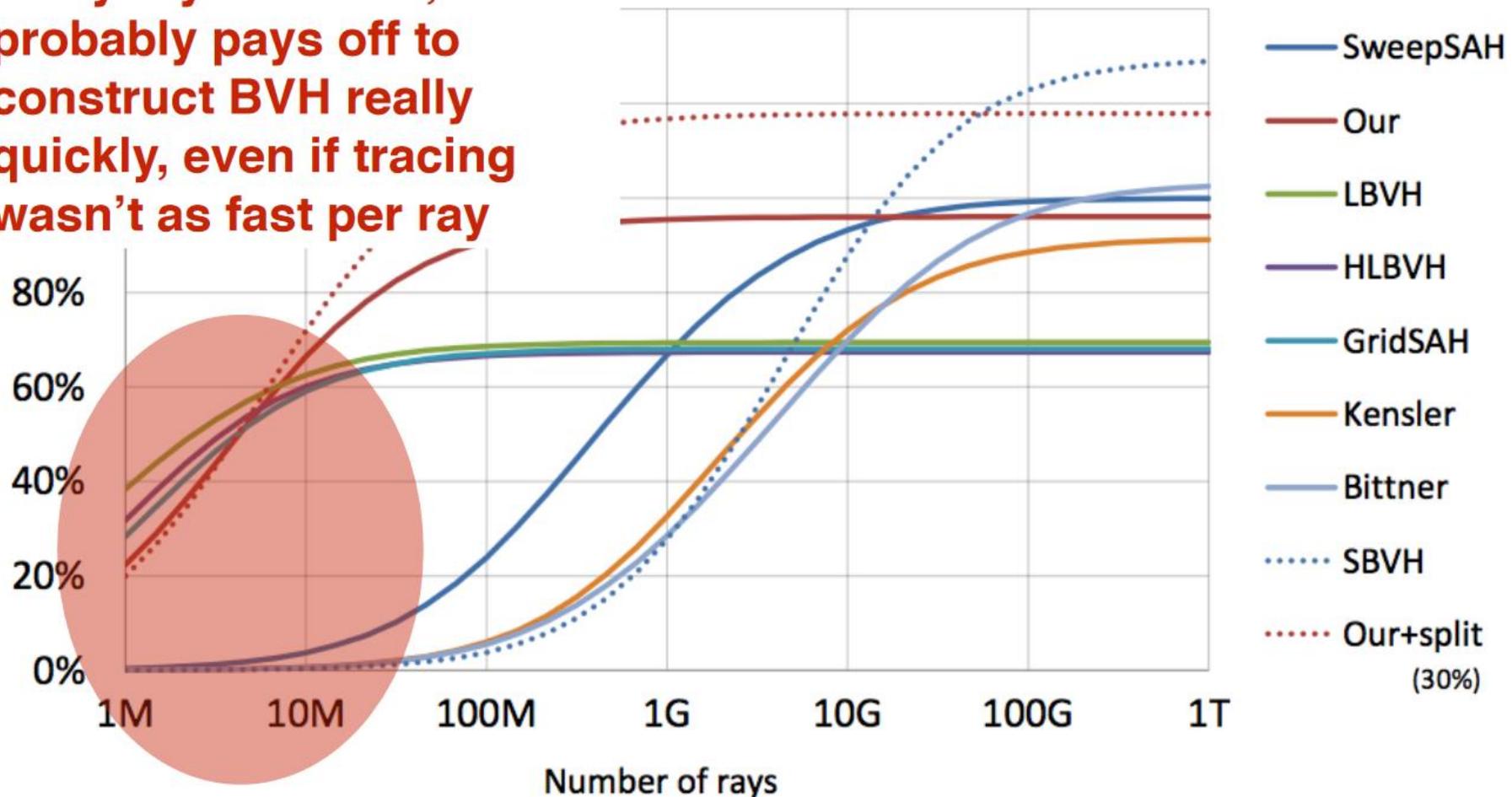


Check out the paper this comparison came from https://users.aalto.fi/~ailat1/publications/karras2013hpg_paper.pdf



If you don't have too many rays to trace, it probably pays off to construct BVH really quickly, even if tracing wasn't as fast per ray

Efficiency measured as a function of TOTAL WALLCLOCK TIME PER RAY, taking into account both BVH construction and actual tracing.



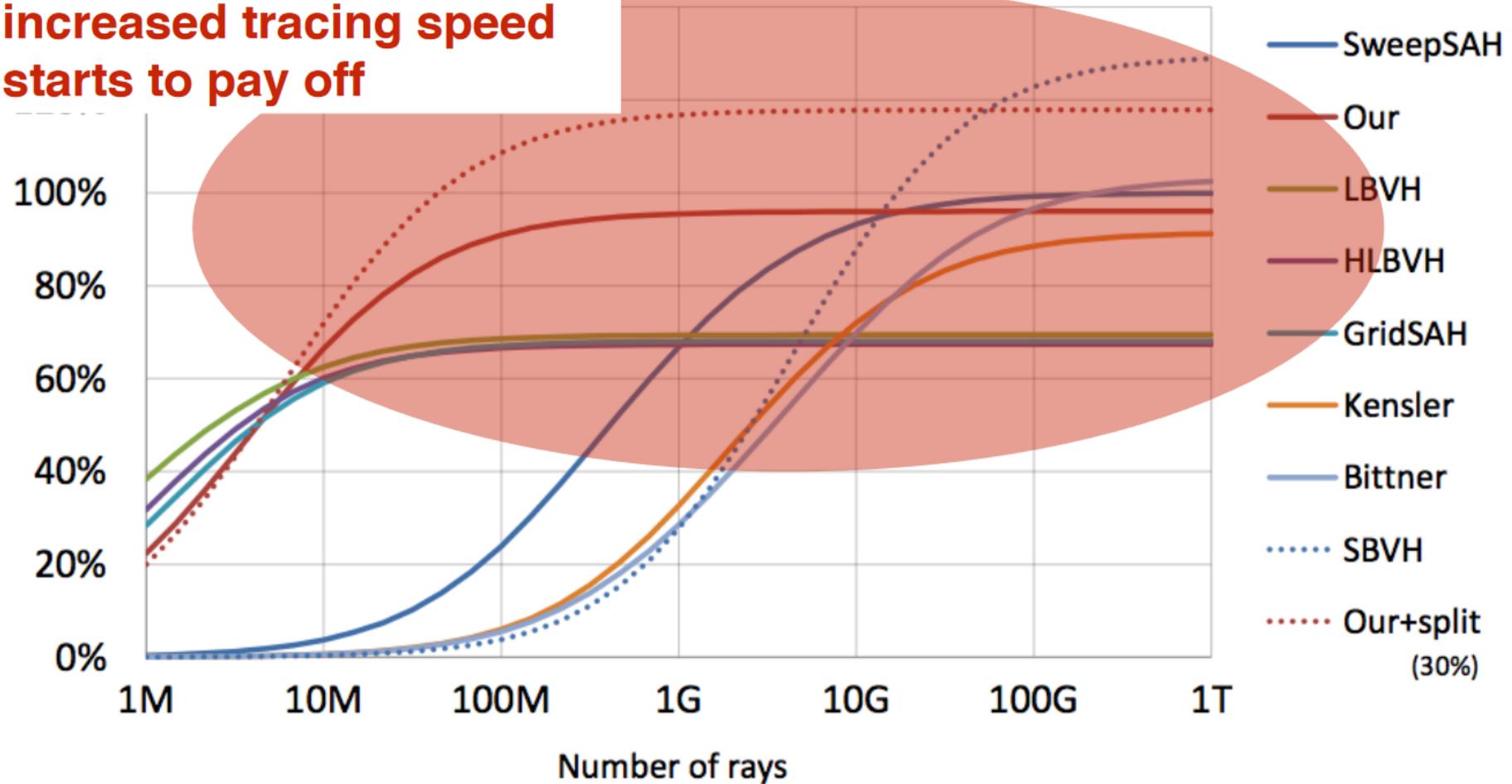
Check out the paper this comparison came from https://users.aalto.fi/~ailat1/publications/karras2013hpg_paper.pdf



After some point a faster but slower-to-build BVH's increased tracing speed starts to pay off

1g

Efficiency measured as a function of TOTAL WALLCLOCK TIME PER RAY, taking into account both BVH construction and actual tracing.



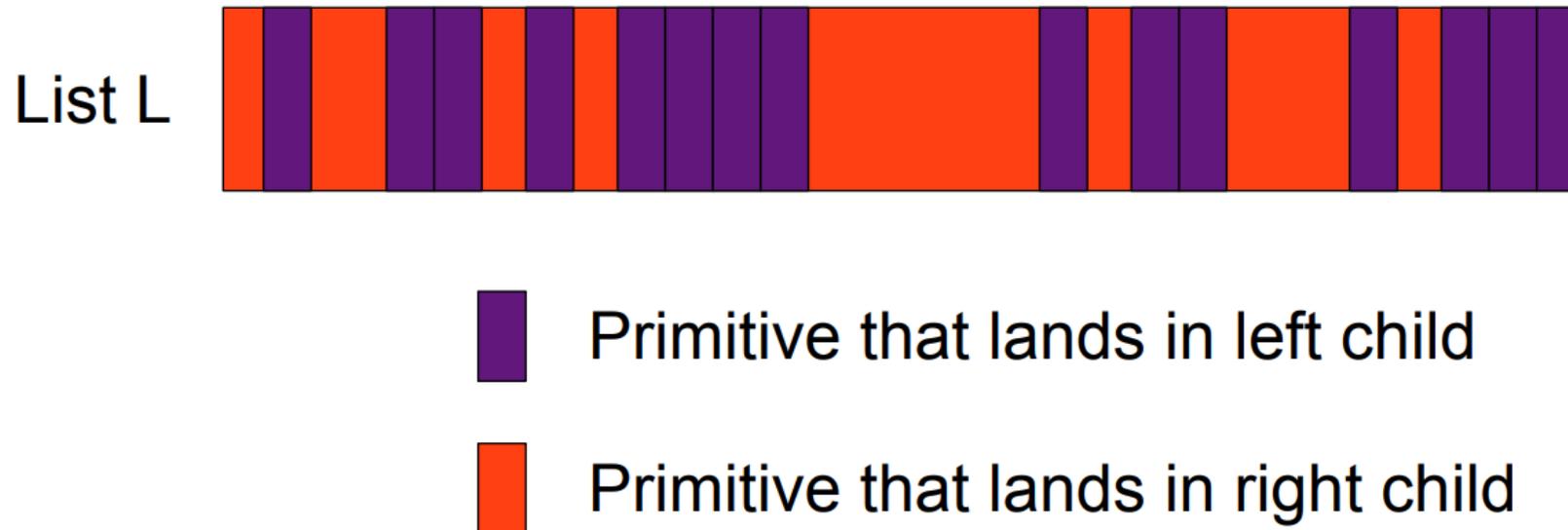
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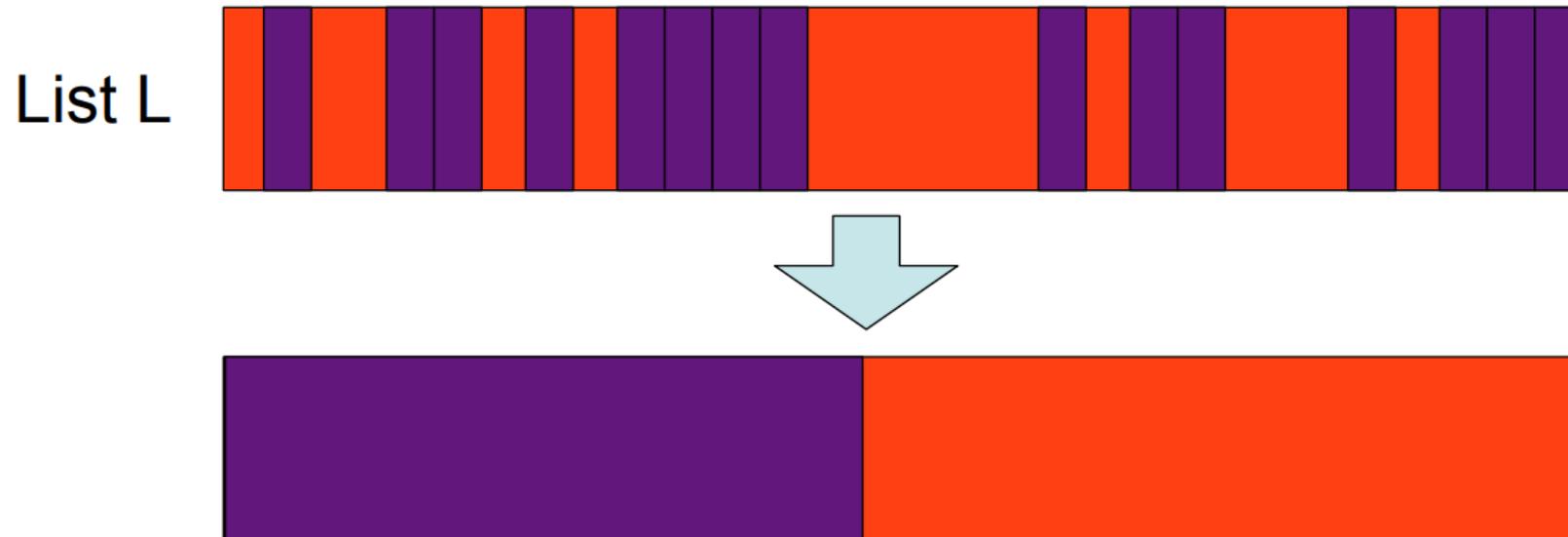
Structure	Memory Consumption	Building Time	(Expected) Traversal Time
none	none	none	abysmal
Regular Grid	low – high (resolution)	low	uniform scene: ok otherwise: bad
Quadtree/Octree	low – high (overlap/uniformity)	low	good
K-d Tree	low – high (overlap)	low – high	good – excellent
BVH	low	low – high	good – excellent



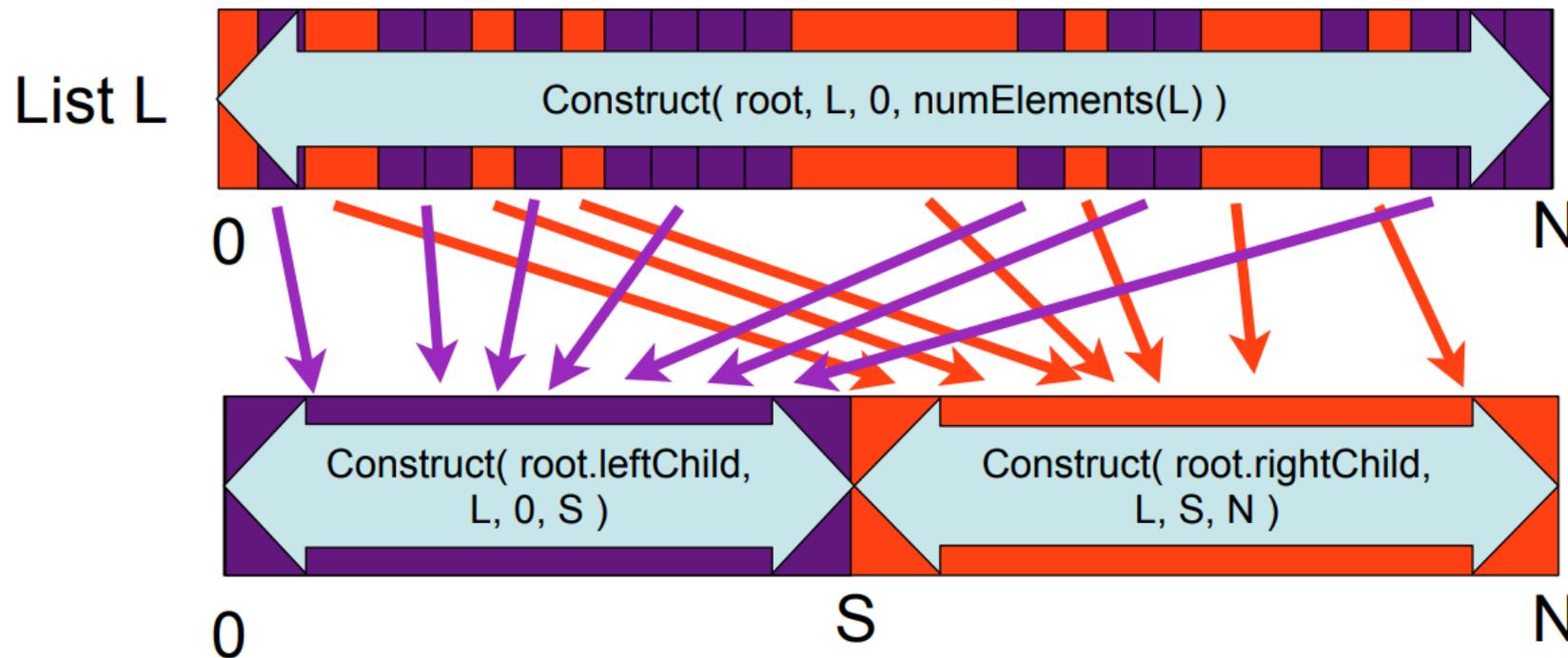
- For each split, sort the node's portion of the triangle list L in-place
- When constructing child nodes, pass them L and *start/end* indices



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- For each split, sort the node's portion of the triangle list L in-place
- When constructing child nodes, pass them L and *start/end* indices



- Don't loop over triangles at each i to get $LSA(i)$ and $RSA(i)$!
- Precompute them once per node and axis instead
 - Create two 0-volume bounding boxes BB_L, BB_R
 - Allocate $N+1$ entries for LSA/RSA , set $LSA(0) = RSA(N) = 0$
 - Iterate i over range $[1, N]$, for each i :
 - Merge BB_L with the AABB of sorted triangle with index $(i - 1)$
 - Store surface area of BB_L as value for $LSA(i)$
 - Merge BB_R with the AABB of sorted triangle with index $(N - i)$
 - Store surface area of BB_R as value for $RSA(N - i)$



- Consider using *stdlib* container (e.g., vector)
- Try to avoid dynamic memory allocation
- $2N - 1$ is an upper bound for the total number of nodes you need
- `std::sort(<first>, <last>, <predicate>)`
- `std::nth_element(<first>, <nth>, <last>, <predicate>)`
 - Can be used for splitting if you don't need exact sorting
 - Reorders the N -sized vector such that:
 - n smallest elements are on the left
 - $N - n$ biggest are on the right
 - Faster than sorting!



- Each have their specializations, strengths and weaknesses
- E.g., K-d Trees with ropes do not require a stack for traversal [5]
- Which acceleration structure is the **best** is contentious
- Currently, BVHs are extremely widespread and well-understood



- Higher child counts (>2) per node, mixed nodes (children + triangles)
- Actually DO split triangles sometimes to get maximal performance
- Build BVHs bottom-up in parallel on the GPU [3]
- In animated scenes, reuse BVHs, update those parts that change
- Actually use built-in traversal logic of GPU hardware (NVIDIA RTX!)



- Interesting topics: BVHs for animation, LBVH, SIMD/packet/stackless traversal, Turing RTX architecture
- [1] *Heuristics for Ray Tracing Using Space Subdivision*, J. David MacDonald and Kellogg S. Booth, 1990
- [2] *On Quality Metrics of Bounding Volume Hierarchies*, Timo Aila, Tero Karras, and Samuli Laine, 2013
- [3] *Parallel BVH generation on the GPU*, Tero Karras and Timo Aila, 2012
- [4] *Fast Parallel Construction of High-Quality Bounding Volume Hierarchies*, Tero Karras and Timo Aila, 2013
- [5] *Stackless KD-Tree Traversal for High Performance GPU Ray Tracing*, Stefan Popov, Johannes Günther, Hans-Peter Seidel and Philipp Slusallek, 2007
- [6] *Realtime Ray Tracing and Interactive Global Illumination*, Phd Thesis, Ingo Wald, 2004
- [7] *Bonsai: Rapid Bounding Volume Hierarchy Generation using Mini Trees*, P. Ganestam, R. Barringer, M. Doggett, and T. Akenine-Möller, 2015

